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Section

A

Subject

Applied Calculs

Sub to

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Find:-

$$\text{Q1:- } \int_0^1 \frac{4t^3 - 2t^2 + 3t - 1}{2t^2 + 1} dt$$

$$\text{Sol:- } \int_0^1 \frac{4t^3 - 2t^2 + 3t - 1}{2t^2 + 1} dt$$

$$= \int_0^1 \frac{4t^3 + 3t - 2t^2 - 1}{2t^2 + 1} dt$$

$$= \int_0^1 \frac{t(4t^2 + 3) - (2t^2 + 1)}{2t^2 + 1} dt$$

$$= \int_0^1 \frac{t(4t^2 + 3)}{2t^2 + 1} dt - \int_0^1 \frac{2t^2 + 1}{2t^2 + 1} dt$$

$$= \int_0^1 \frac{t(4t^2 + 3)}{2t^2 + 1} dt - \int_0^1 1 dt$$

$$= \int_0^1 \frac{t(4t^2 + 3)}{2t^2 + 1} dt [1-0]$$

$$= \int_0^1 \frac{t(4t^2 + 3)}{2t^2 + 1} dt - 1 \rightarrow \text{①}$$

Now:

$$\text{Let } 2t^2 + 1 = y \Rightarrow 2t^2 + 1 = y$$

$$\text{At } t = 1 \Rightarrow y = 3 \Rightarrow 2t^2 = y - 1$$

$$t \rightarrow 0 \Rightarrow y = 1 \Rightarrow 4t^2 = 2y - 2$$

$$4t^2 + 3 = 2y - 2 + 3$$

Now Diff

$$4t = \frac{dy}{dt} \quad 4t^2 + 3 = 2y + 1$$

$$dt = \frac{dy}{4t}$$

$$= \int_1^3 \left( \frac{2y+1}{4} \right) \frac{dy}{4t} - 1$$

$$= \int_1^3 \frac{2y+1}{4y} dy - 1$$

$$= \frac{1}{4} \left[ \int_1^3 \frac{2y}{y} dy + \int_1^3 \frac{1}{y} dy \right] - 1$$

$$= \frac{1}{4} \left[ \int_1^3 2 dy + \int_1^3 \frac{1}{y} dy \right] - 1$$

$$\Rightarrow \frac{1}{4} \left[ 2y \Big|_1^3 + 1 \times y \Big|_1^3 \right] - 1$$

$$\Rightarrow \frac{1}{4} [2(3) - 2(1) + \ln(3) - \ln(1)] - 1$$

$$= \frac{1}{4} [6 - 2 + 1.0986] - 1$$

$$= \frac{1}{4} [5.0986] - 1$$

$$\Rightarrow 1.27465 - 1$$

$$= \boxed{0.2746} \text{ Ans}$$

$$\textcircled{Q}2:- \int_2^3 t \sin t^2 dt$$

Sol:- let  $t^2 = y$   
Diff w.r.t  $t^2$   $t^2 = y$   
 $2t = dy/dt$   $(3)^2 = 9$   
 $dt = dy/2t$   $(2)^2 = 4$

Now

As  $t \rightarrow 3$  then  $y = 9$   
As  $t \rightarrow 2$  then  $y = 4$

$$\begin{aligned} \text{So } &= \int_2^3 t \sin t^2 dt = \int_4^9 \cancel{t} \sin y \frac{dy}{\cancel{2t}} \\ &= \int_4^9 \sin y dy \\ &= -\cos y \Big|_4^9 \\ &= -[\cos(9) - \cos(4)] \end{aligned}$$