

Mid Term

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Subject : Structure

Analysis - II

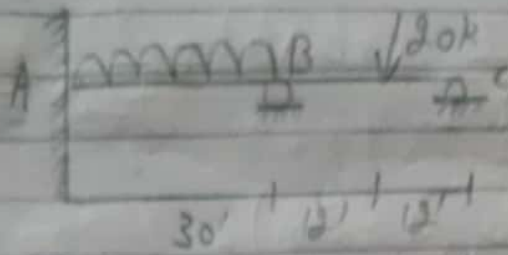
Submitted to : Sir Adeed

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P#01

Q.1

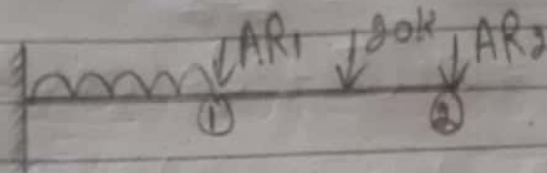
Solution:



$EI = \text{Constant}$

$\delta \cdot I = 2^\circ$

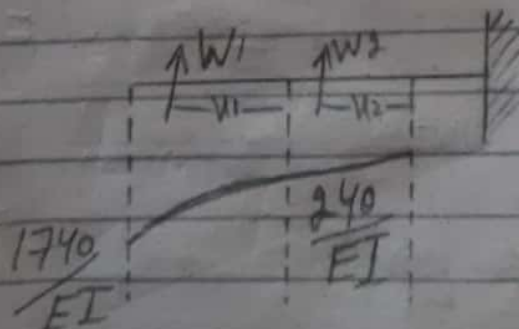
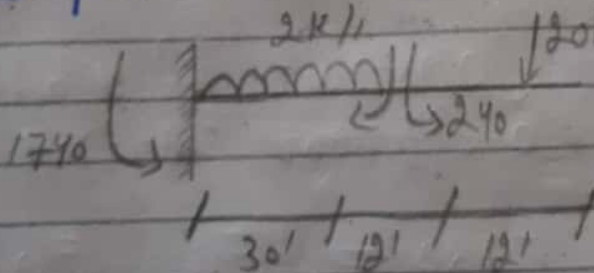
Step# 01: Select redundant actions



$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$[DRS] = [DRL] + F \times AR$$

Step# 02: Compute the value of [DRL]



P#02

$$W_1 = \left( \frac{240 + 0}{2EI} \right) \times 12 = 1440/EI$$

$$W_2 = \frac{1}{n+1} \times (b \times h) = \frac{1}{2+1} \left( \frac{1100}{EI} \right) \times 30 = \frac{11000}{EI}$$

$$u_1 = \frac{L}{3} \left( \frac{a+2b}{a+b} \right)$$

$$u_1 = \frac{12}{3} \left( \frac{240 + 2(0)}{240 + 0} \right) = 4'$$

$$u_2 = \frac{3}{n+2} \times b = \frac{3}{2+2} (30) = 22.5'$$

$$DRL_1 = W_1 (u_1 + 30) = 1440 (4 + 30) = 48960$$

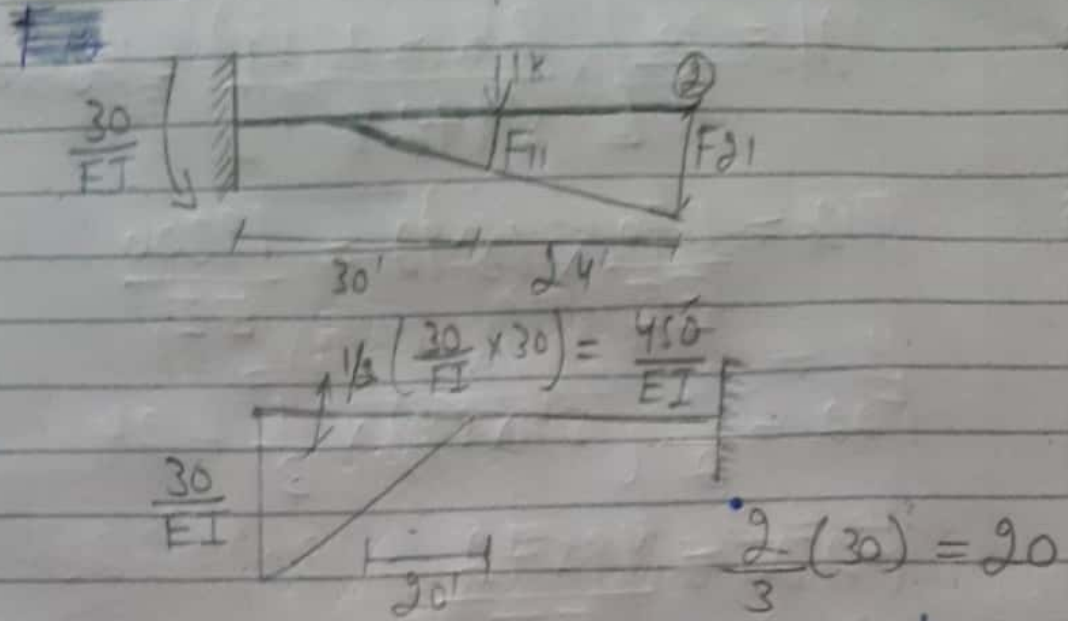
$$\begin{aligned} DRL_2 &= W_1 (u_1 + 40) + W_2 (u_2 + 12) \\ &= 1440 (4 + 40) + 11000 (22.5 + 12) \\ DRL_2 &= 442860 \end{aligned}$$

$$[DRL] = \frac{1}{EI} \begin{bmatrix} 48960 \\ 442860 \end{bmatrix}$$

Step#03 Construct flexibility  
co-efficient matrix

$$F_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

- (a) Apply a unit value of AR<sub>1</sub> at reference point  
(i) Compute the value of F<sub>11</sub> & F<sub>21</sub>

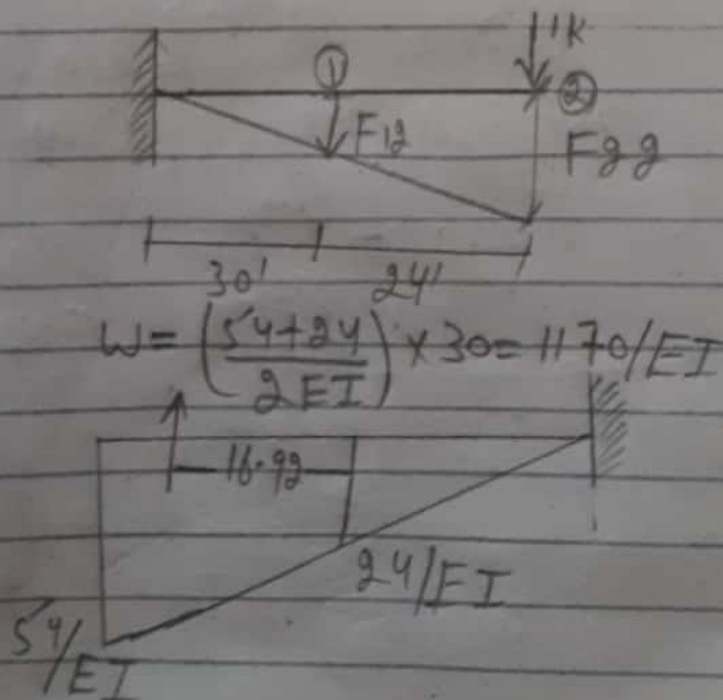


$$F_{11} = \frac{450}{EI} (20) = \frac{9000}{EI}$$

$$F_{21} = \frac{450}{EI} (20 + 24) = \frac{19800}{EI}$$

(b) Apply a unit of  $A_R$  at reference point (2).

(ii) Compute the value of  $F_{12}$  &  $F_{22}$



$$U = \frac{30}{3} \left[ \frac{24 + 2(54)}{54 + 24} \right] = 16.92'$$

$$F_{12} = \frac{1170}{EI} \times 16.92 = \frac{19800}{EI}$$

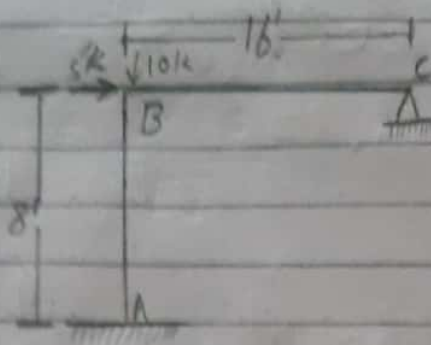
$$F_{22} = \frac{1}{2} (54 \times 54) \times \frac{1}{3} + 24$$

$$F_{22} = \frac{49572}{EI}$$

Answer

Q 3

Solutions:-



$E = \text{constant}$

$I_c = I$

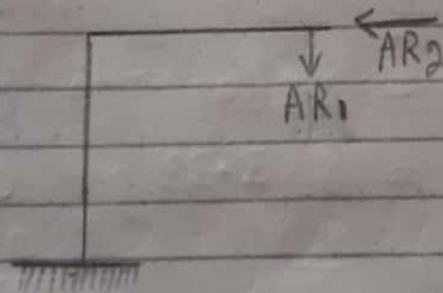
$I_B = 2I$

Total Statical indeterminacy

$\Rightarrow R - 3 = 5 - 3 = 2^{\circ}$

Step # 01

Identify redundant actions



$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \quad \begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Step # 02 Compute value of [DR1]

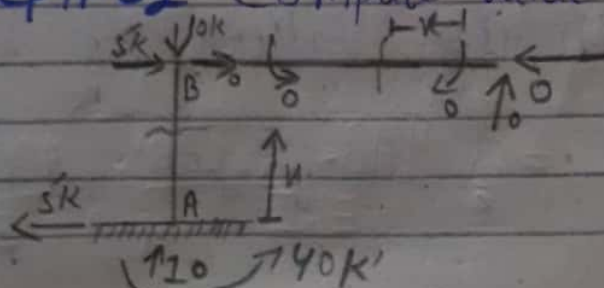


Fig: AML Value (M-values)

P#06

Step# 03:- (F) or (AMR)

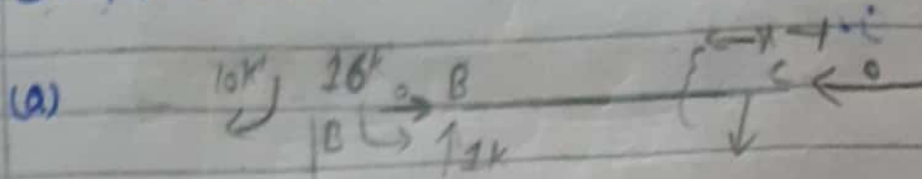


Fig: AMR-values

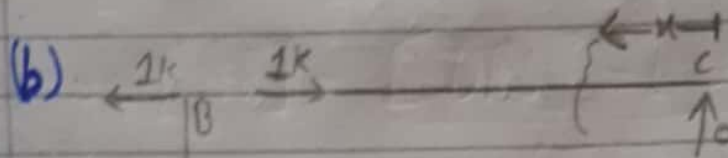
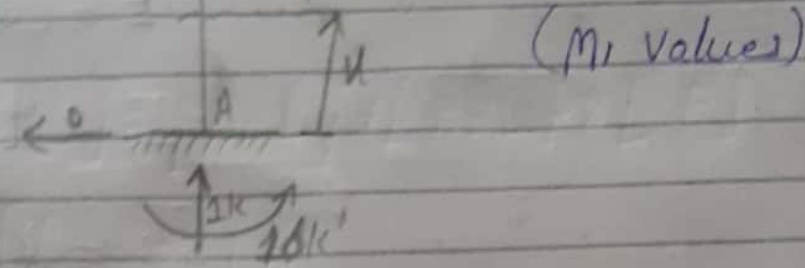
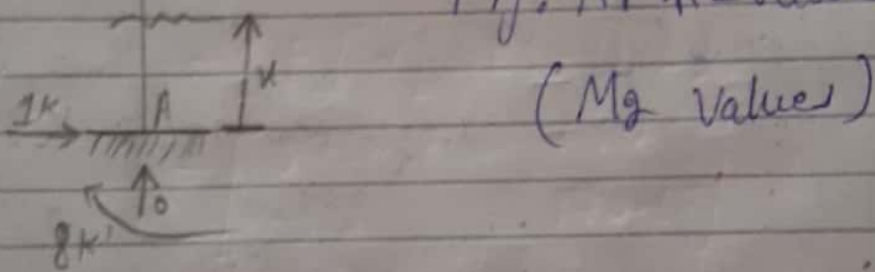


Fig: AMR-value



Member	AB	BC
Origin	A	C
Limits	0-8	0-16
I	I	2I
M	$5x-40$	0
M <sub>1</sub>	-16	16
M <sub>2</sub>	8-16	0

• For finding values of DRL:

$$DRL_1 = \int_0^8 \frac{M_{AB} \cdot M_1(CAB)}{E \cdot I} + \int_0^{16} \frac{M_{BC} \cdot M_2(BC)}{EI}$$

P# 07

$$= \int_0^8 \frac{(5u-40)(-16) du}{EI} + \int_0^{16} \frac{0 \cdot u du}{E(2I)}$$

$$\boxed{DRL_1 = \frac{2560}{EI}}$$

$$DRL_2 = \int_0^8 \frac{(5u-40)(8-u) du}{EI} + \int_0^{16} \frac{0 \cdot 0 du}{E(2I)}$$

$$\boxed{DRL_2 = -\frac{853.33}{EI}}$$

⇒ Compute Flexibility matrix

$$F_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

$$\Rightarrow F_{11} = \int_0^8 \frac{m_1^2(AB)}{EI} + \int_0^{16} \frac{m_2^2(BC)}{EI}$$

$$= \int_0^8 \frac{(-16)^2 du}{EI} + \int_0^{16} \frac{u^2 du}{EI}$$

$$\boxed{F_{11} = \frac{2730.67}{EI}}$$

$$F_{12} = F_{21} = \int_0^8 m_1(AB) \cdot m_2(AB) + \int_0^{16} m_1(BC) \cdot m_2(BC)$$

$$= \int_0^8 \frac{(-16)(8-u) du}{EI} + \int_0^{16} \frac{(u)(0) du}{2EI}$$

$$\boxed{F_{12} = F_{21} = -\frac{512}{EI}}$$



P#08

$$F_{22} = \int_0^8 (m_2)^2 AB \, du + \int_0^{16} (m_2)^2 BC \, du$$
$$= \int_0^8 \frac{(8-u)^2}{EI} \, du + \int_0^{16} \frac{0^2}{2EI} \, du$$

$$F_{22} = 170.67$$

As we know

$$[DRS] = [DRL] + [ARL] \times [F]$$

$$\Rightarrow \cancel{[RR]} \Rightarrow [A]$$

$$\Rightarrow [AR] = \frac{[DRS] - [DRL]}{[F]}$$

$$\Rightarrow [AR] = [F]^{-1} \times [DRS - DRL]$$

$$= \begin{bmatrix} 2730.67 & -512 \\ -512 & 170.67 \end{bmatrix} \times$$

$$\begin{bmatrix} 0 & -2560 \\ 0 & +853.33 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} -0.00005 \\ 4.997 \end{bmatrix} = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$

Answer

Q 2

## ★ Force Method:-

→ In force method forces are redundant or unknowns.

→ Force method starts with equilibrium of forces.

→ Forces found by compatibility equations of displacements.

→ No of redundants =  $D_s$

→ Not suitable for computer

→ It is strain energy method

$$D_s < D_k$$

→ Known as flexibility method.

## ★ Displacement Method:-

→ Also known as stiffness matrix method.

→ Slope deflection method

→ Moment distribution method

$$D_s > D_k$$

→ Displacements are redundants or unknowns.

P #10

→ Starts with complete deformations

→ Displacement found by equilibrium equation of forces.

→ No of redundants = DK

→ Not suitable for truss.

**Suggestion:-**

Displacement method is better and suitable because it is used globally and is very easy too.