

Final term Paper

Discrete maths

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Q1

Ans = Bipartite Graphs:

Sometimes a graph has the property that its vertex set can be divided into two disjoint subsets such that each edge connects a vertex in one of these subsets to a vertex in the other subset. For example,

Consider the graph representing marriages between men and women in a village, where each person is represented by a vertex and a marriage is represented by an edge.

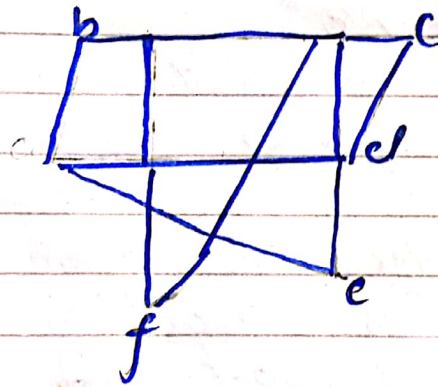
In this graph, each edge connects a vertex in the subset of vertices representing males and a vertex in the subset of vertices representing females. This leads us to

A simple graph G is called bipartite if its vertex set V can be partitioned into two disjoint sets V_1 and V_2 such that every edge in the graph connects a vertex in V_1 and a vertex in V_2 . So that no edge connects a vertex in the subset vertices in V_1 or two vertices in V_2 when this condition holds, we call the pair (V_1, V_2) bipartition.

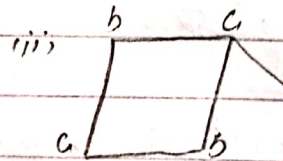
Graphs Bipartite:

Part a,

i) graph is not a bipartite graph because its vertex set cannot be partitioned into two mutually disjoint non empty subsets A and B such that the vertices in A may be connected to vertices in B, but no vertices in A are connected to vertices in A and no vertices in B are connected to vertices in B.

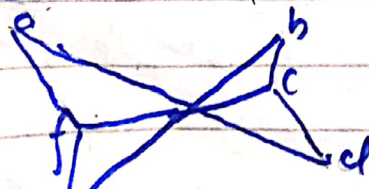


The graph is not bipartite.



ii. Part b:

graph is not a bipartite graph because its vertex set cannot be partitioned into two mutually disjoint non empty subsets A and B such that the vertices in A may be connected to vertices in A and no vertices in B are connected to vertices



Question: 2

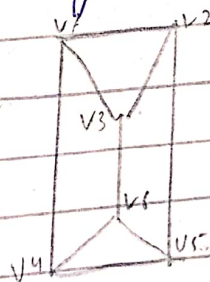
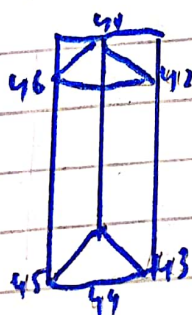
Determine whether the given pair of graph is to isomorphic.

Ans

Let G be a directed graph with ordered vertices v_1, \dots, v_n . The adjacency matrix of G is the $n \times n$ matrix $A = (a_{ij})$ over the set of nonnegative integers such that a_{ij} is the number of arrows from v_i to v_j for all $i, j = 1, 2, \dots, n$.

Note that nonzero entries along the main diagonal of an adjacency matrix indicate the presence of loops, and entries larger than 1 corresponding to parallel edges. Moreover, if the vertices of a directed graph are reordered then the entries in the rows and columns of the corresponding adjacency matrix are moved around.

Example - The two directed graphs shown below differ only in the ordering of their adjacency matrix.

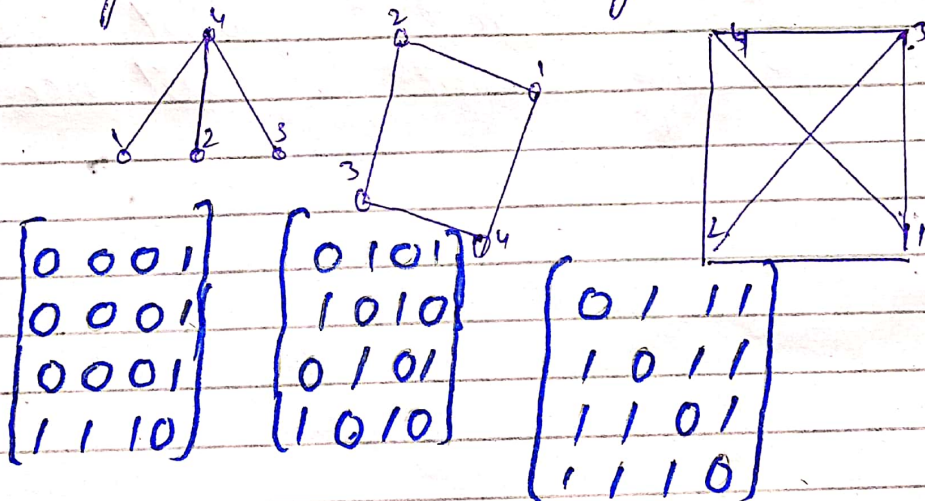


Question 3

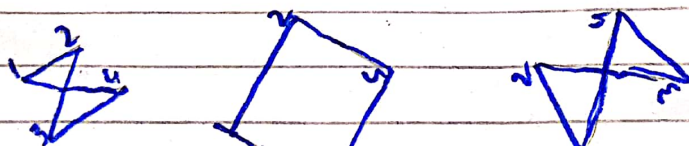
Ans:

Adjacency matrices isomorphic

The adjacency matrices, sometimes also called the connection matrix of a simple labeled graph is a matrix with rows and columns labeled by graph vertices, with a 1 or 0 in position according to whether and are adjacency or not. For a simple graph with no self-loops, the adjacency matrix must have 0s on the diagonal. For an undirected graph, the adjacency matrix is symmetric.



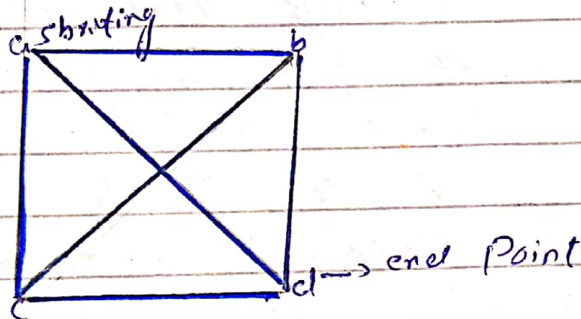
The illustration above shows adjacency matrices for particular labelings of the star graph, cycle graph, and complete graph.



Question-4

Ans:

Determine whether the given has an Euler Circuit. Construct such a Circuit when one exists. Determine whether the graph has an Euler path and construct such a path if one exists.



Euler path $a, b, c, b, d, c, a, e, c$
 This is not Euler path Circuit because starting point and ending point is not same.

Q5

