

ID. 12595

Date. 29/09/2020

Q2) A signal  $x(t)$  band limited by 250 Hz is sampled by an impulse train angular frequency of  $f_s$

a) Determine the Nyquist rate required for perfect reconstruction of signal.

Solution

Given Data

$$f_m = 250 \text{ Hz} \cdot f_s$$

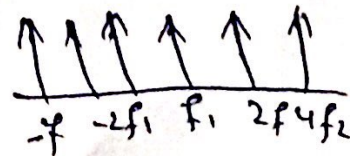
a) Nyquist rate

$$N_p = 2 f_m$$

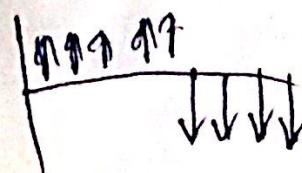
$$= 2 \times 250$$

$$= 500 \text{ Hz}$$

b)



→



(2)

© Cut off frequency

$$f_c = \frac{1}{2\pi RC}$$

$$= \frac{1}{2 \times 3.14 \times 500}$$

$$= 0.0031$$

Q ① ① if the frequency of sampler is  $f_s = 800 \text{ Hz}$ , draw the resulting sampled signal  $s(f)$

Solution

$$f_m = 250 \text{ Hz}$$

$$f_s = 800 \text{ Hz}$$

As we know that

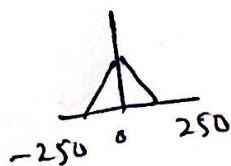
$$f_s = 2f_m$$

So

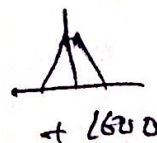
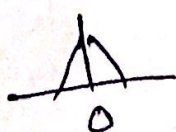
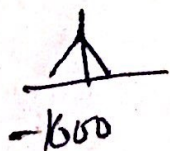
$$800 = 2(250)$$

$$800 = 500$$

$$\text{So } f_s > f_m$$



The resulting sampled signal is





Q2  
Q1 Let  $x(t)$  be a signal with Nyquist rate  $f_s$ . determine the Nyquist rate for following:

(i)  $x(t) + x(t-1)$

Solution

~~Nyquist~~

$$m(t) = x(t) + x(t-1)$$

$$x(t) \rightarrow NR = \omega_s$$

$$m(t) = x(t) + x(t-1)$$

$$x(t) = \omega_s$$

$$x(t-1) = \omega_s$$

It is same Because There is no effect of time shifting on Nyquist rate

$$x(t) \xrightarrow{T_s} x(t-1)$$

These two signal have the same Nyquist rate  $\omega_s$  and to get the Nyquist rate of  $m(t)$  we need to choose the Nyquist rate which is max. But both the

nyquist rate of  $x(t)$  &  $x(t-1)$  are same so by properties of nyquist rate

$$m(t) = x(t) + x(t-1)$$

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \\ \omega_s & \omega_s & \omega_s \end{array}$$

The two nyquist rate are same

so directly the nyquist rate of  $m(t)$  is  $\omega_s$  Answer.

②  $m(t) = \frac{dx(t)}{dt}$

So this time the message signal is equal to 1 time derivative of signal  $x(t)$  and we know the differentiation will not change the nyquist rate so if the original signal is

$$x(t) = \omega_s$$

Then  $\frac{dx}{dt} = \omega_s$

$$m(t) = \frac{dx(t)}{dt}$$

$$\downarrow$$

$$\omega_s = \omega_s$$

(6)

Q2(B)

Given Data

$$m(t) = 10 \sin 400\pi t$$

$$\omega_m = 400\pi \frac{\text{rad}}{\text{Sec}}$$

$$f_m = \frac{\omega_m}{2\pi}$$

$$= \frac{400\pi}{2\pi}$$

$$f_m = 200 \text{ Hz}$$

$$f_s = 300 \text{ Hz}$$

$$f_c = 150 \text{ Hz}$$

Required

what are the frequencies present in the reconstructed signal

$y(t)$

All frequencies are checked and only -150 to +150 Hz range frequencies are passed

so our answer is 100 Hz

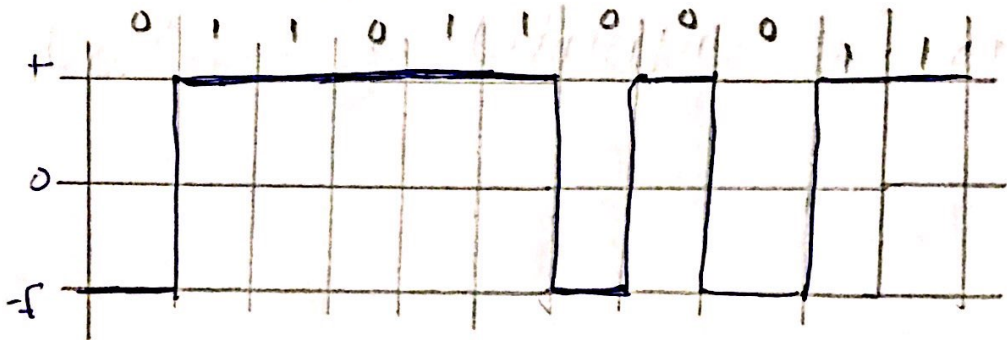


(7)

Q3) Consider the bit sequence (01101100011) and draw the PCM waveform the following modulation schemes:

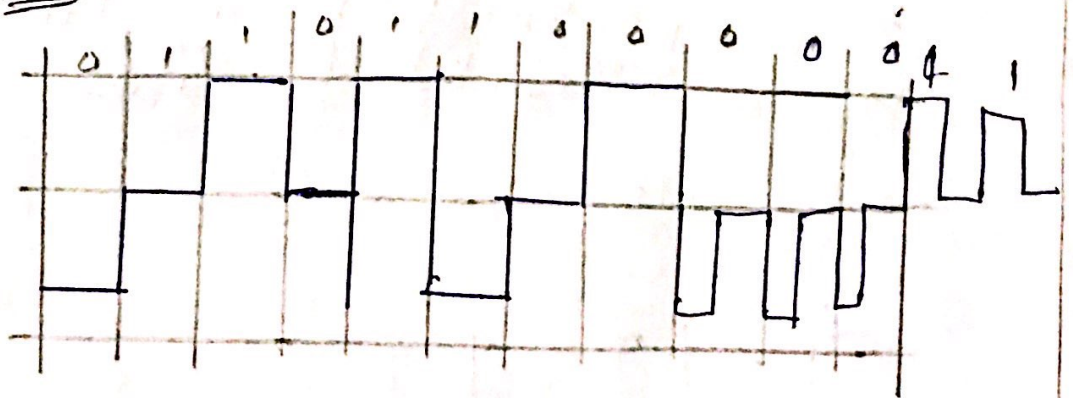
a) NRZ-S

(01101100011)



one is represented by a no change in level.  
"Zero" is represented by a change in level.

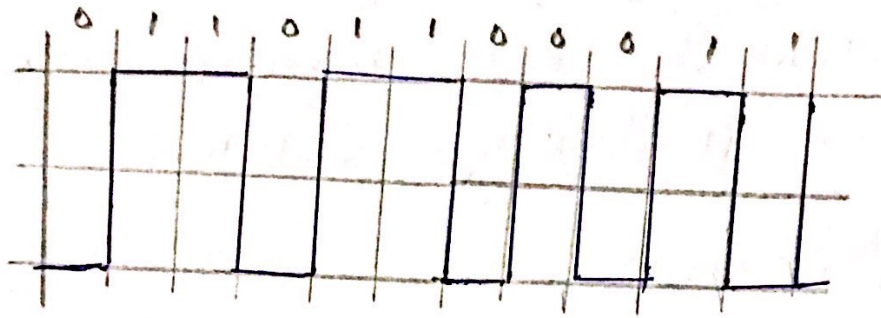
b) Polar-RZ



"one" and "Zero" are represented by opposite level Polar pulses that are one half-bit in width.

(8)

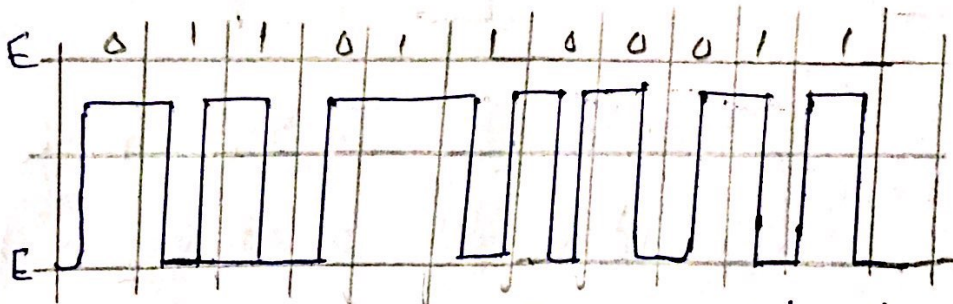
© Split Phase Manchester



One is represented by a 10

Zero is represented by a 01

© Bi-φ-L

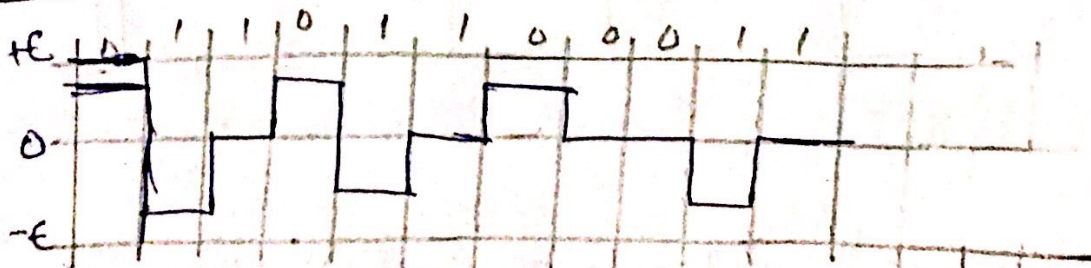


Bi-φ-L (Bi phase level or split phase (1+180))

"one" is represented by a 10

"zero" is represented by a 01

© Dicode-NRZ



Dicode Non-Return To Zero

A "one" to "zero" or "zero" to "one" change polarity otherwise a "zero" is sent.



Q4(a)

(9)

Solution

$$m = 0.5$$

$$E_c = 7.5$$

$$E_c = 7.5 \text{ volt}$$

Let us consider  $E_m$  from  $E_c$  since

$$m = \frac{E_m}{E_c}$$

Therefore

$$E_m = m \times E_c$$

$$= 0.5 \times 7.5$$

$$= 3.75 \text{ V}$$

$$E_{\text{max}} = E_c \times E_m$$

$$= 7.5 \times 3.75$$

$$= 11.25 \text{ Hz}$$

$$E_{\text{min}} = \frac{E_c - E_m}{7.5 - 3.75}$$

$$= 3.75 \text{ V}$$

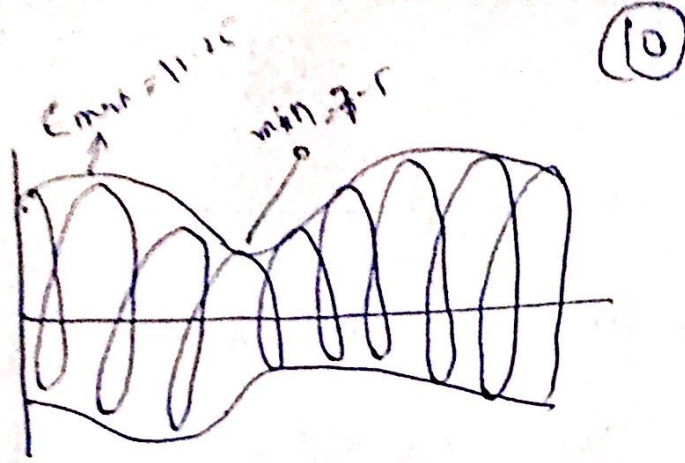
Modulated waveform

So As we know

$$m = 0.5$$

$$E_{\text{max}} = 11.25$$

$$E_{\text{min}} = 3.75$$



(b) (2) (4)

Solution

Depth of modulation

$$m = \frac{E_m}{E_c}$$

$$m = \frac{10V}{5V} = 2V$$

Transmission efficiency

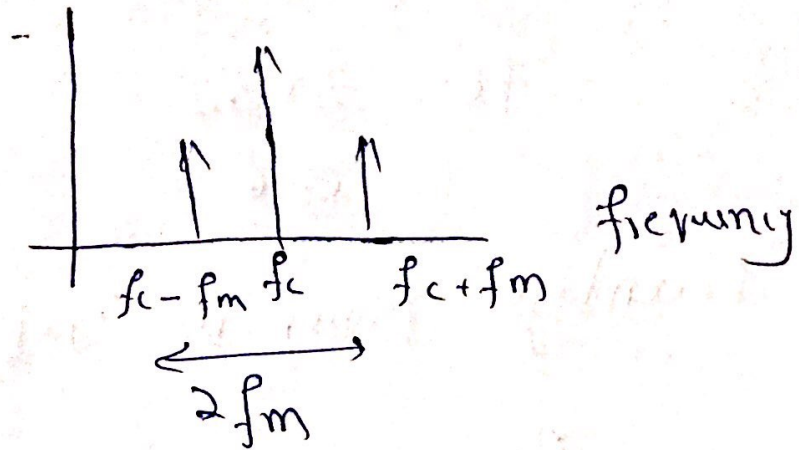
$$\eta_f = \frac{m^2}{2+m^2}$$

$$\eta_f = \frac{(2)^2}{2+(2)^2}$$

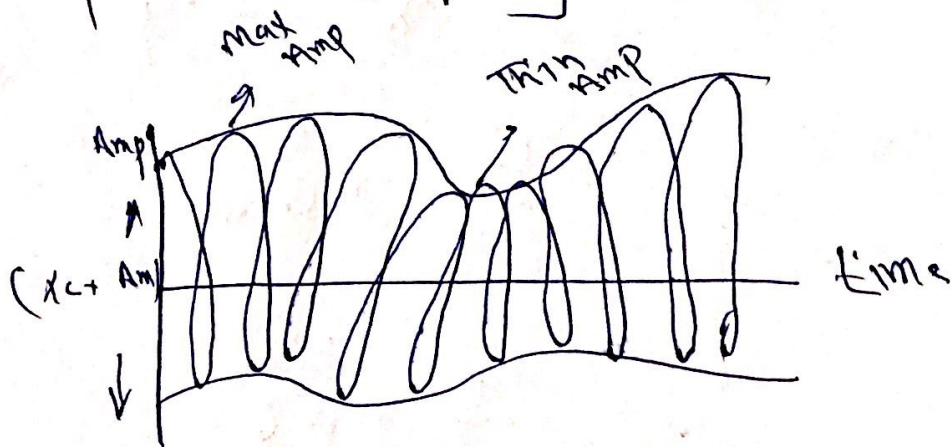
$$\eta_f = \frac{4}{2+4} = \frac{4}{6} = \frac{2}{3}$$

(b)

(11)



Amplitude Frequency



(c) Power in Spectra

$$P_c = \frac{E_c^2}{2 \times R} = \frac{(5)^2}{2 \times 50} = \frac{2}{100} = \frac{1}{4}$$

and total power  $P_t \left(1 + \frac{m^2}{2}\right) P_c$

$$P_t = \left(1 + \frac{(2)^2}{2}\right) \times 0.2$$

$$P_t = \left(1 + \frac{4}{2}\right) \times 0.2$$



(12)

$$P_t = (1+2) \times 0.2$$

$$P_t = 3 \times 0.2 \\ = 0.6$$

(d) Percentage power in USB

$$P_{USB} = \frac{m^2 E_c^2}{8} = \frac{m^2 P_c}{4}$$

$$= \frac{(2)^2}{4} \times 0.6$$

$$= \frac{4}{4} \times 0.6$$

$$= 0.6 = 60\%$$