

Mid Term Paper.

Subject:- Advance Design of Reinforced
Concrete Structure.

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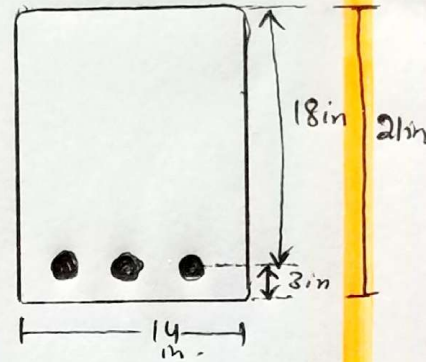
PESHAWAR.

$$f_d = 75,000 \text{ psi}$$

$$f_c' = 5,000 \text{ psi}$$

Required

(i) $E_t = ?$ (ii) $\phi = ?$ (iii) ϕ (Mn?)



(i) $E_t \rightarrow$

$$E_t = \frac{d-c}{c} (0.003) \quad \text{--- (A)}$$

First we will find "c"

$$a = \frac{A_s f_d}{0.85 f_c' b} = \frac{4.68 \times 75}{0.85 \times 5 \times 14} = 5.899 \text{ in.}$$

$\beta_1 = 0.80$ for $f_c' = 3000 \text{ psi}$ Concrete.

$$c = a / \beta_1 = \frac{5.899}{0.8} = 7.37 \text{ in.}$$

Now
(A) $\Rightarrow E_t = \left(\frac{d-c}{c} \right) (0.003) = \left(\frac{18-7.37}{7.37} \right) (0.003)$

$$\boxed{E_t = 0.00432}$$

$$E_t > 0.004$$

$$E_t < 0.005$$

Hence the beam is in transition zone.

(ii) $\phi = ?$

$$\phi = 0.65 + (E_t - 0.002) \frac{250}{3}$$

$$\phi = 0.65 + (0.00432 - 0.002)$$

$$\boxed{\phi = 0.836}$$

(iii) $\phi M_n = ?$

first we check the steel.

$$\rho = \frac{A_s}{bd} = \frac{4.68}{14 \times 18} = 0.0185$$

From table "A.7" in Appendix "A"

$$\rho > \rho_{min} = 0.0028$$

$$\rho < \rho_{max} = 0.0194$$

(ok)

So

$$\phi M_n = A_s f_y (d - \frac{a}{2}) = 4.68 \times 75 (18 - \frac{5.899}{2})$$

$$\phi M_n = 5282.72 \text{ in-k}$$

$$\phi M_n = 440.229 \text{ ft-k}$$

Now

$$\phi M_n = 0.836 \times 440.229$$

$$\boxed{\phi M_n = 368.029}$$

~~The value of strain is greater than the yield strain~~

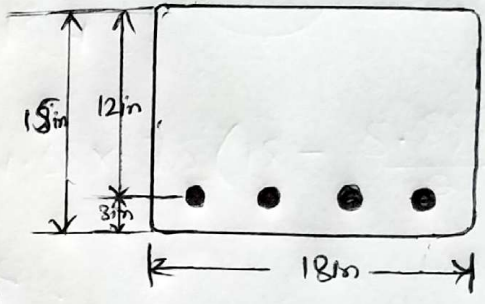
The value of strain is greater than the yield strain 0.002 but less than 0.005.

This indicates the beam is in transition zone. To make more safer the value of ϕ should be calculated which change. Now the steel is well into its yield plateau before concrete crushes.

P.T.O

→ The value of f is greater than f_{min} & less than f_{max} . so As per ACI Code the reinforcement is $\phi 12$ the steel will be yield first & give a warning sign before failure.

$f_y = 60,000 \text{ psi}$
 $f_c' = 4,000 \text{ psi}$



$$E_t = \left(\frac{d-c}{c} \right) (0.003) \text{ --- (B)}$$

$$\Rightarrow a = \frac{A_s f_y}{0.85 f_c' b} = \frac{5.06 \times 60}{0.85 \times 4 \times 18} = 4.96 \text{ in}$$

$\beta_1 = 0.85$ for $f_c' = 4,000 \text{ psi}$

$$c = a / \beta_1 = \frac{4.96 \text{ in}}{0.85} = 5.835 \text{ in.}$$

Now

$$\text{(B)} \Rightarrow E_t = \left(\frac{12 - 5.835}{5.835} \right) (0.003)$$

$$E_t = 0.003$$

$E_t \leq 0.004$

So the above section is not ductile & may not be used as per ACI Section 10.3.5

(B) Sol Given Data:

$$M_D = \text{Reg NO} = 152 \text{ ft-k}$$

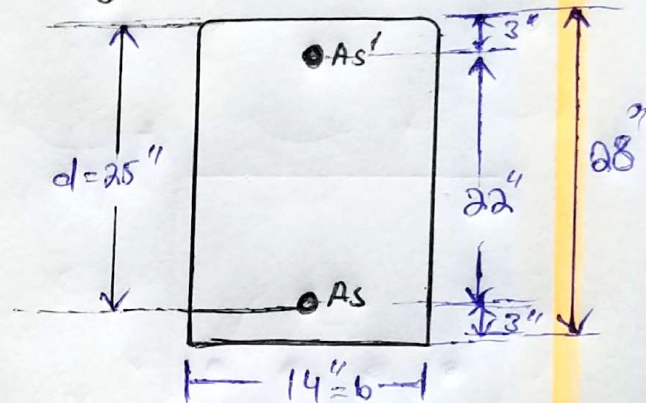
$$M_L = 400 \text{ ft-k}$$

$$f_c' = 4,000 \text{ psi}$$

$$f_y = 60,000 \text{ psi}$$

Sol

Section:-



(1) Factored Moment:- \rightarrow

$$M_u = 1.2 M_D + 1.6 M_L$$

$$= 1.2 \times 152 + 1.6 \times 400 = 822 \text{ ft-k}$$

$$\boxed{M_u = 822 \text{ ft-k}}$$

(2) Nominal Moment:-

$$M_n = \frac{M_u}{\phi} = \frac{822}{0.9}$$

$$\boxed{M_n = 913.3 \text{ ft-k}}$$

Assuming maximum possible tensile steel with no compression steel & computing beams nominal strength moment.

ρ_{max} (from table A.7, Appendix A) = 0.0181

$$A_{s1} = \rho_{max} b d = 0.0181 \times 14 \times 25$$

$$A_{s1} = 6.335 \text{ in}^2$$

For $\rho_{max} = 0.0181$ $m_u / \phi b d^2 = 912 \text{ psi}$
(From Table A.13).

$$\Rightarrow M_{u1} = 912 \times \phi b d^2 = 912 \times 0.9 \times 14 \times (25)^2$$

$$M_{u1} = 7182000 \text{ in-lb} = \frac{7182000}{12} \text{ ft-k}$$

$$M_{u1} = \frac{7182000}{12 \times 1000} \text{ ft-k}$$

$$M_{u1} = 598.50 \text{ ft-k}$$

Now $M_{n1} = \frac{M_{u1}}{\phi} = \frac{598.5}{0.9} = 665 \text{ ft-k}$

$$M_{n1} = 665 \text{ ft-k}$$

$$M_{n2} = M_n - M_{n1} = 913.3 - 665 = 248.3$$

$$M_{n2} = 248.3 \text{ ft-k}$$

(3) Theoretical $A_{s'}$ required:

$$A_{s'} = \frac{M_{n2}}{f_y (d-d')} = \frac{248.3 \times 12}{60 (25-3)} = 12.26 \text{ in}^2$$

Fy 3# 8 bars 2.35 in² Table A.4

Consider $f_s' = f_y$

$$A_s' f_s' = A_{s2} f_y$$

$$A_{s2} = \frac{A_s' f_s'}{f_y} = \frac{2.35 \text{ in}^2 \times 60}{60} = 2.35 \text{ in}^2$$

$$\boxed{A_{s2} = 2.35 \text{ in}^2}$$

$$A_s = A_{s1} + A_{s2} = 6.335 + 2.35 = 8.685 \text{ in}^2$$

$$\boxed{A_s = 8.685 \text{ in}^2}$$

try 7 #10 bars (8.86 in²)
(Table A.4)

Checking

Assuming $f_s' = f_y$.

$$(i) \frac{(A_s - A_s') f_y}{0.85 f_c' b \beta_1} = \frac{(8.685 - 2.35) \times 60}{0.85 \times 14 \times 4 \times 0.85} = 9.39 \approx 9.4 \text{ in}$$

$$(ii) \epsilon_s' = \left(\frac{c - d'}{c} \right) (0.003) = \left(\frac{9.4 - 3.}{9.4} \right) (0.003) = 0.002067 \epsilon_y$$

$$\boxed{\epsilon_s' > \epsilon_y}$$

$$(iii) \epsilon_t = \left(\frac{d - c}{c} \right) (0.003) = \left(\frac{25 - 9.4}{9.4} \right) (0.003)$$

$$\boxed{\epsilon_t = 0.00497 < 0.005}$$

So Calculate the value of ϕ again
because $\phi \neq 0.9$

$$\phi = 0.65 + (0.00497 - 0.002) \left(\frac{250}{3} \right)$$

$$\boxed{\phi = 0.8975}$$

$$A_{s2} = \frac{A_s' f_s'}{f_y} = \frac{2.35 \times 60}{60}$$

$$\boxed{A_{s2} = 2.35 \text{ in}^2}$$

$$A_{s1} = A_s - A_{s2} = \overset{8.86}{\cancel{8.86}} - 2.35 = 6.51 \text{ in}^2$$

$$\boxed{A_{s1} = 6.51 \text{ in}^2}$$

$$M_{n1} = A_{s1} f_y \left(d - \frac{a}{2} \right)$$

$$= 6.51 \times 60 \left(25 - \frac{0.85 \times 9.4}{2} \right) = 8204.553 \text{ ft-k}$$

$$\boxed{M_{n1} = 683.71 \text{ ft-k}}$$

$$M_{n2} = A_{s2} f_y (d - d') = (2.35)(60)(25 - 3)$$

$$= 3102 \text{ ft-k}$$

$$\boxed{M_{n2} = 258.5 \text{ ft-k}}$$

$$M_n = M_{n1} + M_{n2}$$

$$M_n = M_{n1} + M_{n2} = 683.71 + 258.5$$

$$M_n = 942.21 \text{ ft-k}$$

$$\phi M_n = 0.89 \times 942.21$$

$$\phi M_n = 845.63 \text{ ft-k}$$

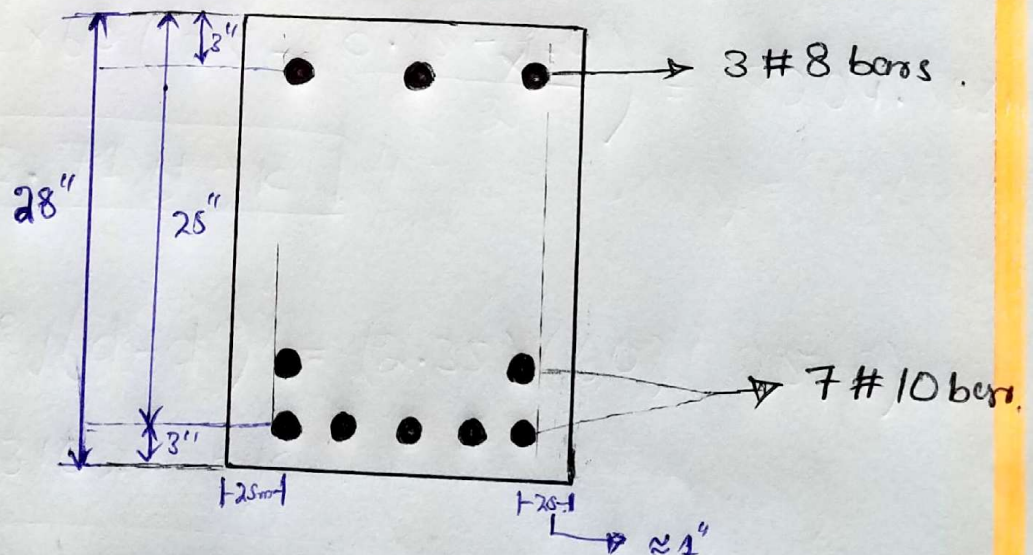
$$M_u = 822 \text{ ft-k}$$

so

$$\phi M_n > M_u \quad \text{OK}$$

$$A_s' = 2.35 \text{ in}^2 \quad (3 \# 8 \text{ bars})$$

$$A_s = 8.86 \text{ in}^2 \quad (7 \# 10 \text{ bars}) \quad (\text{Table A.4})$$



As per ACI Code ^{Side} clear cover 25mm - 35mm.

So take 25mm side clear cover.

Design of Square Column.

9

Q2

Given data.

$$P_u = 152 \text{ k}$$

$$P = \text{Reg No} = 152 \text{ k}$$

$$M_u = 152 \text{ ft-k}$$

$$\text{Reg No} = 15274$$

$$f_c' = 4,000 \text{ psi}$$

$$f_y = 60,000 \text{ psi}$$

Sol

Short Square Column.

Assuming the column will have an average compression stress = about $0.6f_c' = 0.6 \times 4000$

$$= 2400 \text{ psi} = 2.4 \text{ ksi}$$

$$A_{g(\text{reqd})} = \frac{P_u}{0.6f_c'}$$

$$A_{g(\text{reqd})} = \frac{152}{2.4} = 63.34 \text{ in}^2$$

As per ACI recommendation the minimum size of column is $12" \times 12"$

So Try $12" \times 12"$ ($A_g = 256 \text{ in}^2$)

Now

$$e = \frac{M_u}{P_u} = \frac{12 \times 15}{152} = \frac{180}{152}$$

$$e = 1.184 \text{ in.}$$

$$P_n = \frac{P_u}{\phi} = \frac{152}{0.65} = 233.84 \text{ k}$$

$$k_n = \frac{P_n}{f_c' A_g} = \frac{233.84}{4 \times 12 \times 12} = 0.405$$

$$|k_n = 0.405|$$

$$R_n = \frac{P_n e}{f_c' A_g h} = \frac{233.84 \times 1.184}{4 \times 12 \times 12 \times 12}$$

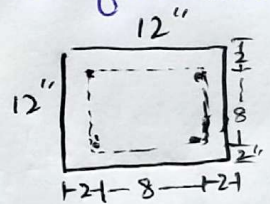
$$|R_n = 0.0400|$$

$$y = \frac{8 \text{ in.}}{12 \text{ in}}$$

$$|y = 0.667|$$

As per ACI Code
 C.C._{min} = 40 mm = 1.575 in
 for Column

So selu clear cov
 2" from each side.



From Graph "6" & "7" Appendix A.

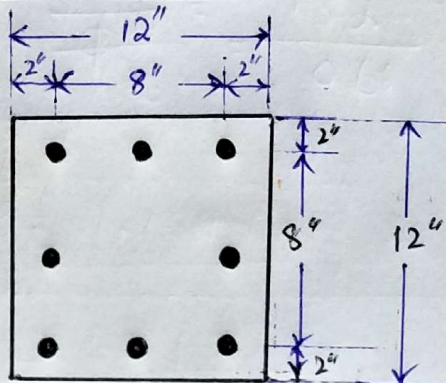
γ	0.6	$ 0.667 $	0.7
ρ_g	0.025	$ 0.0235 $	0.024

By using interpolation
 we got 0.0235

$$\Rightarrow A_s = (0.0235)(12)(12)$$

$$|A_s = 3.384 \text{ in}^2|$$

use 8 #6 bars = 3.53 in²



Q3.3

For $P_u = \text{Ref No } \notin \text{first floor}$ ~~the~~ $\text{eligid} = 1527 \text{ psf}$ (which not possible)

$$c = 16" \times 16"$$

$$P_D = 152 \text{ k}$$

$$P_L = 160 \text{ k}$$

Depth 5 ft

$$q_a = 1527 \text{ psf}$$

$$f_y = 60 \text{ ksi}$$

$$f_c' = 30 \text{ ksi}$$

Sol

$$h = 24"$$

$$\text{dage} = 20"$$

$$b_o = 4(c + \text{dage}) = 4 \times (16 + 20) = 144$$

Now $q_e = 1527 - 600 = 927 \text{ psf} = 0.952 \text{ ksf}$

$$A_{reqd} = \frac{152 + 160}{0.952} = 328 \text{ ft}^2$$

sol select $19 \text{ ft} \times 19 \text{ ft}$

⇒ So for $16" \times 16"$ column ($19 \text{ ft} \times 19 \text{ ft}$) foundation/footing is not possible.

⇒ So I solve this question with selecting a proper value of " q_u "

$$\boxed{q_u = 3804 \text{ psf}}$$

So the question solve on other page

Q3

- : Given Data: -

$$\text{Column} = 16" \times 16"$$

$$P_D = 152k$$

$$P_L = 160k$$

$$\text{Depth} = 5 \text{ ft}$$

$$\text{Soil wgh} = 100 \text{ lb/ft}^2$$

$$f_y = 60,000 \text{ psi}$$

$$f_c' = 3000 \text{ psi}$$

$$\text{Bars} = \#8$$

$$\{a = 3804 \text{ psi} \rightarrow (\text{Selected properly})$$

Sol

$$\text{Assum} = \text{height of footing} = h = 24" = 2'$$

$$d_{avg} = h - 3" - 1" = 24 - 3 - 1 = 20"$$

$$b_o = 4(c + d_{avg})$$

$$\boxed{b_o = 4(16 + 20) = 144 \text{ in}}$$

$$W = \text{Pressure of Soil} + \text{pressure of RC}$$

$$= \gamma_{su}(z-h) + \gamma_c h$$

$$= 100(5-2) + 150(2)$$

$$= 300 + 300 = 600$$

Now

$$P_e = P_a - W = 3804 - 600$$

$$\boxed{P_e = 3804 - 600 = 3204 \text{ psf}}$$

$$\phi_c = 3.204 \text{ Ksf}$$

$$A_{reqd} = \frac{\text{Total load}}{\phi_c} = \frac{152 + 160}{3.204}$$

$$A_{reqd} = 97.37 \text{ in}^2$$

$$B \times B = A_{reqd} = 97.37 \text{ in}^2$$

$$\Rightarrow \boxed{B \approx 10 \text{ ft}^2}$$

$$\Rightarrow \boxed{A = 100 \text{ ft}^2}$$

Bearing pressure.

$$\phi_u = \frac{1.2(P_D) + 1.6(P_L)}{A_{area}}$$

$$= \frac{1.2 \times (152) + 1.6(160)}{10 \times 10} = 4.384 \text{ Ksf}$$

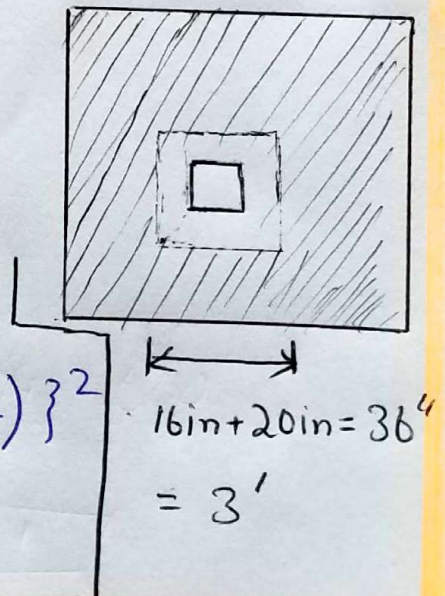
Now Punching Shear

$$b_o = 144 \text{ in}$$

$$V_{u2} = \phi_u A - \phi_u (C + \text{dangle})$$

$$= 4.384 \times 100 - 4.384 \left\{ \left(\frac{16+20}{12} \right) \right\}^2$$

$$\boxed{V_{u2} = 398.944 \text{ k}}$$



Check

$$d = \frac{V_{u2}}{0.75 \times 4 \sqrt{f_c'} \times b_o}$$

$$= \frac{398090}{0.75 \times 4 \sqrt{30000} \times 144} = 17.05 \text{ in} < 20 \text{ in}$$

OK

$$d = \frac{V_{u2}}{0.75 \left(\frac{40 \times d}{b_o} + 2 \right) \sqrt{f_c'} \times b_o}$$

$$= \frac{398090}{0.75 \times \left(\frac{40 \times 20}{144} + 2 \right) \sqrt{30000} \times 144}$$

$$d = \frac{V_{u2} = 398.944 \times 1000}{0.75 \left(\frac{40 \times 20}{144} + 2 \right) \sqrt{30000} \times 144}$$

$$d = 9.02 \text{ in} < 20 \text{ in} \quad \text{OK}$$

So both "d" < 20" so punching shear is "OK"

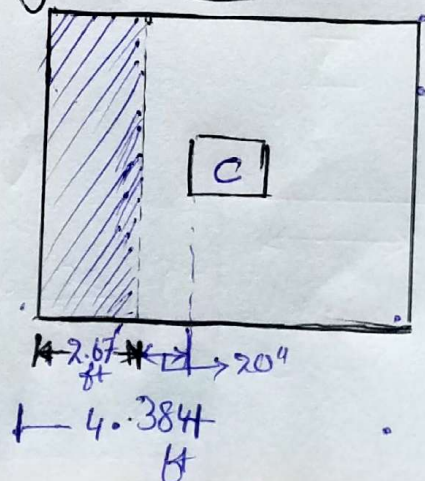
Depth required for one way shear

$$V_{u1} = (10 \text{ ft}) (2.67) (4.384) \text{ from } 6 \text{ ft}$$

$$V_{u1} = 117.0528$$

$$d = \frac{117052}{0.75 \times 2 \sqrt{30000} \times 120}$$

$$d = 11.87" < 20" \quad \text{OK}$$



$$M_u = (4.33)(10)(4.884) \times \left(\frac{4.33}{2}\right)$$

$$\boxed{M_u = 410.97 \approx 411 \text{ ft-k}}$$

$$\frac{M_u}{\phi b d^2} = \frac{12 \times 411000}{0.9 \times 120 \times 20^2} = 114.1667 \text{ psi}$$

Now from Appendix "A"

$$\rho = 0.0021 < \rho_{\text{min}} \text{ for flexure.}$$

use large ρ of bonding

$$\rho = \frac{200}{60,000} = 0.0033.$$

$$\text{or } \frac{3\sqrt{3000}}{60,000} = 0.00274.$$

So

$$A_s = 0.0033(120)(20) = 7.2 \text{ in}^2$$

$$\boxed{A_s = 7.2 \text{ in}^2}$$

use 6 #10 bars. in Both Dir.

Development length:

$$\psi_c = \psi_e = \psi_s = \lambda = 1.0$$

Assuming bars spaced 16 in on center,
being 6 in on side.

$$C_b = \text{bottom cover} = 3.5 \text{ in.}$$

$$C_b = \frac{1}{2}(16 \text{ in}) = 8 \text{ in}$$

Letting $k_{tr} = 0$

$$\frac{C_b + k_{tr}}{d_b} = \frac{3.5 + 0}{1.0 \text{ in}} = 3.5 > 2.5$$

$$\frac{l_d}{d_b} = \frac{3}{40} \cdot \frac{f_y}{\lambda \sqrt{f_c} \cdot \frac{C_b + k_{tr}}{d_b}} = \frac{3}{4} \times \frac{60000}{(1) \sqrt{3000}} \times \frac{1 \times 1 \times 1}{2.5}$$

used 2.5

$$= 32.86 \text{ diameters}$$

$$\frac{l_d}{d_b} \frac{A_{s reqd}}{A_{s fun}} = 32.86 \left(\frac{7.2}{7.59} \right) = 31.30 \text{ diameters}$$

$$l_d = 31.30(1) = 31.30 \approx 32 \text{ in.}$$

< available $l_d = 4 \text{ ft } 6 \text{ in} - \frac{20}{2} = 3 \text{ in}$

