

Name

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Tariq Mehmood

Submitted To :-

Sir Fawad Ahmad

Submitted by :-

7834

Subject :-

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Hydraulic Engineering

Semester

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Q no 1

Ans The pressure drop Δp is expected to be depend upon the gate opening h , The overall depth d , The velocity v , density ρ , and viscosity μ .

⇒ List the relevant variable

$\Delta p, h, d, v, \rho, \mu$

Dimension

Δp $ML^{-1}T^{-2}$

h L

d L

v LT^{-1}

ρ ML^{-3}

μ $ML^{-1}T^{-1}$

number of variable = $n = 6$

number of Independent dimension $m = 3 (M, L, T)$

number of non-dimensional group $n - m = 3$

→ choose $m (= 3)$ scaling variable; geometric (d); Kinematic / Time-dependent (v); dynamic/mass-dependent (ρ)

From dimensionless group by non-dimensionalising the remaining variable: ΔP , h , and μ

$$\pi_1 = \Delta P d^a v^b \rho^c$$

$$\begin{aligned} M^0 L^0 T^0 &= (ML^{-1}T^{-2})(L)^a (LT^{-1})^b (ML^{-3})^c \\ &= M^{1+c} L^{-1+a+b-3c} T^{-2-b} \end{aligned}$$

$$M: 0 = 1+c \quad \Rightarrow c = -1$$

$$T: 0 = -2-b \quad \Rightarrow b = -2$$

$$L: 0 = -1+a+b-3c \quad \Rightarrow a = 1+3c-b = 0$$

$$\Rightarrow \pi_1 = \Delta P v^{-2} \rho^{-1} = \frac{\Delta P}{\rho v^2}$$

Now $\pi_2 = \frac{h}{d}$ (by inspection, since h is the length)

$$\pi_3 = \mu d^a v^b \rho^c$$

$$\begin{aligned} M^0 L^0 T^0 &= (ML^{-1}T^{-1})(L)^a (LT^{-1})^b (ML^{-3})^c \\ &= M^{1+c} L^{-1+a+b-3c} T^{-1-b} \end{aligned}$$

$$M: 0 = 1+c \quad \Rightarrow c = -1$$

$$T: 0 = -1-b+0 \quad \Rightarrow b = -1$$

$$L: 0 = -1+a+b-3c \quad \Rightarrow a = 1+3c-b = -1$$

$$\Rightarrow \pi_3 = \mu d^{-1} v^{-1} \rho^{-1} = \frac{\mu}{\rho v d}$$

Recognition of the Reynold number suggest that we replace π_3 by $\pi'_3 = (\pi_3)^{-1} = \frac{\rho v d}{\mu}$

Hence dimensional analysis yields,

$$\text{i.e. } \pi_1 = f(\pi_2, \pi_3')$$

$$\frac{\Delta P}{\rho V^2} = f\left(\frac{h}{d}, \frac{\rho V d}{\mu}\right)$$

(a) Dynamic similarity requires that all non-dimensional groups be the same in model and prototype: i.e.

$$\pi_1 = \left(\frac{\Delta P}{\rho V^2}\right)_p = \left(\frac{\Delta P}{\rho V^2}\right)_m$$

$$\pi_2 = \left(\frac{h}{d}\right)_p = \left(\frac{h}{d}\right)_m \quad (\text{similar shape i.e. geometric similarity})$$

$$\pi_3' = \left(\frac{\rho V d}{\mu}\right)_p = \left(\frac{\rho V d}{\mu}\right)_m$$

From the last, we have a velocity ratio.

$$\frac{V_p}{V_m} = \frac{(\mu/\rho)_p}{(\mu/\rho)_m} \frac{d_m}{d_p} = \frac{0.002/800}{1.0 \times 10^{-6}} \times \frac{1}{5} = 0.5$$

$$\text{Thus; } V_m = \frac{V_p}{0.5} = \frac{3.0}{0.5} = 6 \text{ m/s}$$

The ratio of the quantities of flow is

$$\frac{Q_p}{Q_m} = \frac{(\text{velocity} \times \text{area})_p}{(\text{velocity} \times \text{area})_m} = \frac{V_p}{V_m} \left(\frac{d_p}{d_m}\right)^2 = 0.5 \times 5^2 = 12.5$$

(c) Finally, for the pressure drop,

$$\begin{aligned} \pi_1 &= \left(\frac{\Delta P}{\rho v^2} \right) \rho = \left(\frac{\Delta P}{\rho v^2} \right)_m \Rightarrow \frac{(\Delta P)_p}{(\Delta P)_m} = \frac{\rho_p}{\rho_m} \left(\frac{v_p}{v_m} \right)^2 \\ &= \frac{800}{1000} \times 0.5^2 = 0.2 \end{aligned}$$

Thus

$$\Delta P_p = 0.2 \times \Delta P_m = 0.2 \times 60$$

$$\boxed{\Delta P_m = 12.0 \text{ kPa}}$$

Q No 2

Sol

$$T = 783$$

$$G = 2.4$$

$$C_u = 0$$

$$(1) H_{\text{limiting}} = \frac{G_{\text{all}}}{\gamma_w (G - C_u + 1)} = \frac{120 \times 783 \times 1000}{1000 (2.4 - 0 + 1)} = 27635.29 \text{ m}$$

$$\text{Let } H_w = 26000 \text{ m}$$

$$\text{Thus } 27635.29 > H_w = 26000$$

So it is low gravity dam.

(2) Top width "a"

(5)

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$$\text{Free board} = 1.5 h_{\text{wave}} = 1.5 \times 26000$$

$$\boxed{F.B = 39000 \text{ m}}$$

$$\begin{aligned} \text{Height of Dam} = H_D &= H_w + F.B \\ &= 26000 + 39000 \end{aligned}$$

$$\boxed{H_D = 65000 \text{ m}}$$

$$a = 14\% \text{ of } H_D$$

$$= 0.14 \times 65000 \Rightarrow \boxed{a = 9100}$$

(3) Base width "b" (with out offset)

(i) For No sliding criteria

$$b' = \frac{H_w}{\mu G} = \frac{26000}{0.7 \times 2.4} = 15476.19$$

$$\boxed{b' \approx 15477 \text{ m}}$$

(ii) for no tension criteria

$$b' = \frac{H_w}{\sqrt{G}} = \frac{26000}{\sqrt{2.4}} = 16782.92 \text{ m}$$

$$\boxed{b' \approx 16783 \text{ m}}$$

4) Depth of vertical portion on u/s side

$$h' = 2a\sqrt{G-C}$$

$$h' = 2 \times 9100 \sqrt{2.4 - 0}$$

$$h' = 28195.31 \text{ m}$$

$$\boxed{h' \approx 28195 \text{ m}}$$

(5) Upstream off set = $\frac{a}{16} = \frac{9100}{16} = 568.75 \text{ m}$

(6) Depth below the water level to the end of inclined portion in u/s = $3.14 a \sqrt{G}$

$$= 3.14 (9100) \sqrt{2.4}$$

$$= 44266.65 \text{ m}$$

(7) Total width of the base of the Dam

$$b = b' + \frac{a}{16} = 16783 + \frac{9100}{16}$$

$$\boxed{b = 17351.75 \text{ m}}$$

(8) $\tan \theta = \frac{b'}{H} = \frac{16783}{26000}$

$$\theta = \tan^{-1} \left(\frac{16783}{26000} \right) \approx 32.84^\circ$$

$$\boxed{\theta = 32.84^\circ}$$

(9) Depth of vertical portion on D/S

$$\tan \theta = \frac{a}{d'} = \frac{9100}{d'}$$

$$\left(\frac{16783}{26000} \right) d' = 9100$$

$$d' = \frac{9100 \times 26000}{16783}$$

$$d' = 14097.59 \text{ m}$$

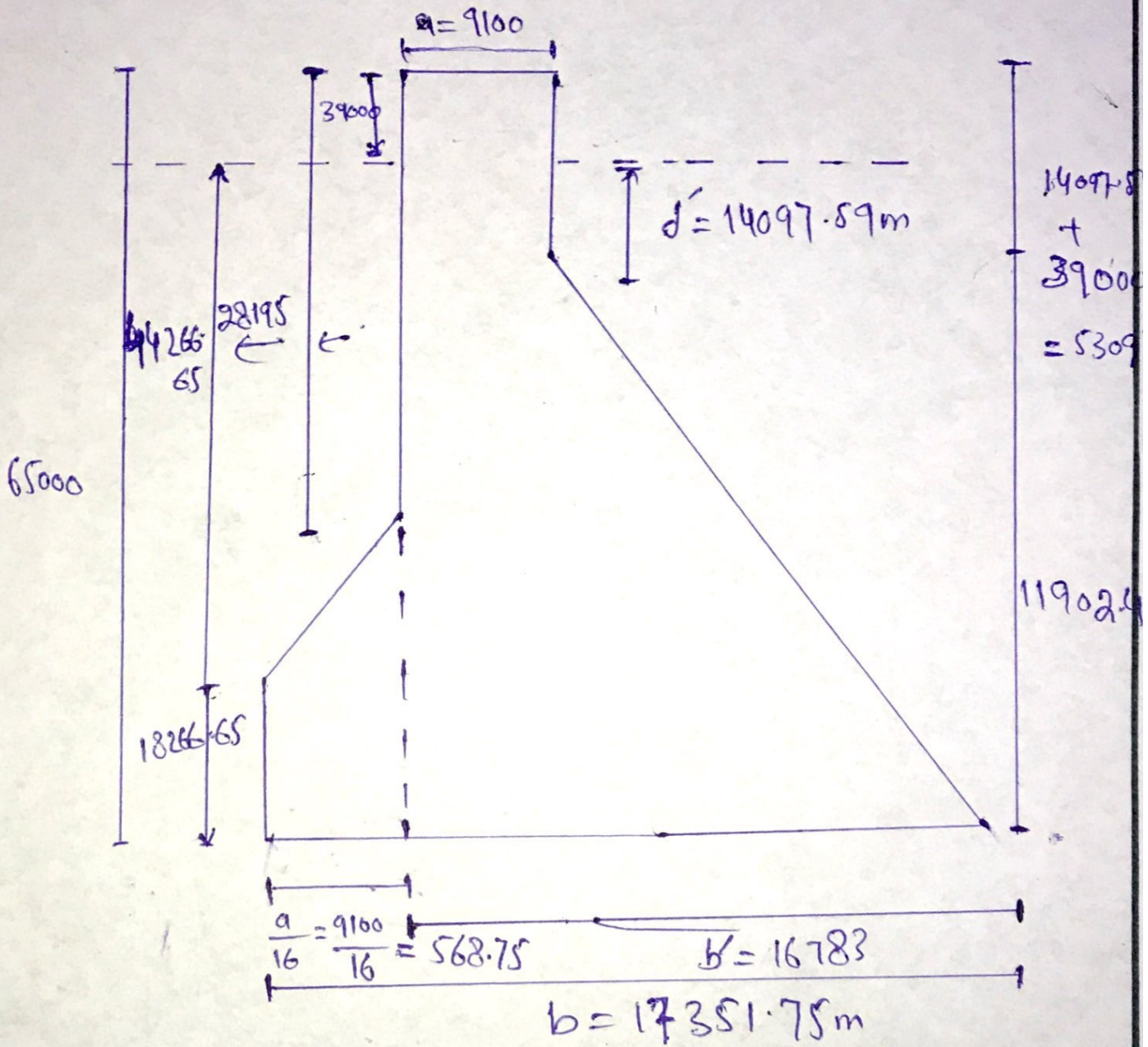
depth of vertical portion

$$d = d' + F.B = 14097.59 + 39000$$

$$d = 53097.59 \text{ m}$$

Diagram is on next page.

Diagram



QNO 3

Dimensional Analysis:

⇒ is the analysis of the relationships between different physical quantities by identifying their base quantities (such as length, mass, time and electric charge) and units of measures (such as miles vs. kilometers, or pounds vs. kilograms) and ~~taking~~ tracking these dimensions as calculations or comparisons are performed.

⇒ Dimensional analysis or more specifically the factor-label method also known as the unit factor method

Example

$$\frac{24 \text{ hr}}{1 \text{ day}} \times \frac{60 \text{ min}}{1 \text{ hr}} \times \frac{60 \text{ s}}{1 \text{ min}} = \frac{86,400 \text{ s}}{\text{day}}$$

Similitude

is used to express measurement on laboratory can be used to

describe the behaviour of other systems outside of laboratory

Hydraulic Model

There are two main types of hydro turbine, impulse and reaction.

The type of hydropower turbine selected for a project is based on the height of standing water - referred to as "head" and the flow or volume of water at the site

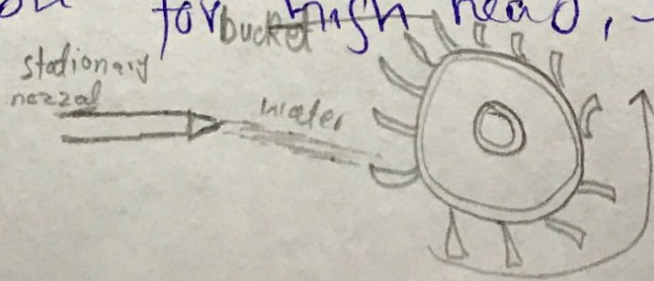
⇒ Model about the Impulse Turbine

The impulse turbine generally uses the velocity of the water to move the runner and discharges to atmospheric pressure.

The water stream hits each bucket on the runner.

There is no suction on the down side of the turbine and the water flow out the bottom of the turbine housing after hitting the runner.

An impulse turbine is generally suitable for high head, low flow applications.



Q No 4

(1) Particle diameter

The diameter of the particle is directly proportional to the fall velocity because greater the size of particle so it will tend to move faster as compared to the particle of small size thus there will be more gravitational force on particle of greater size so it will fall quickly due to its weight.

(2) Particle density

⇒ Density of the particle is directly proportional to the rate of fall velocity since particle with high density tends to settle down early compared with particle of low density.

(3) Particle concentration

Concentration of particle size will considerably affect its fall velocity as the section having greater concentration will be settled

down at the place thus causing more fall velocity comparing with section of low concentration.

(4) Particle shape

Particles having regular shapes tends to be effected more than irregular shapes since regular shapes particles have even surface which offers very little or no friction while particles with irregular shape offers more friction, as the particle with smaller surface area are more likely to be effected due to their less resistance.

(5) Viscosity of water

From the experimental study we can see that parameter such as temperature and pressure changes the magnitude of viscosity so the section of water having more temperature and pressure will fall objectively more due to increase in the kinetic energy so fall velocity will be more.

Turbulence of water

Turbulence of water depends upon the different factors such as velocity.

It will affect the fall velocity because of its zigzag motion thus the velocity varies at every point which is why it affects the fall velocity. Moreover increase in the kinetic energy tends to affect the fall velocity compared with steady fluid.

The End.