

**Department of Computer Science**  
**Mid Term Assignment**  
**Date: 13/04/2020**  
**Course Details**

**Course Title:** Radar & Satellite Communication  
**Instructor:** DR, Naeem Ahmad Jan

**Module:**  
**Total Marks:** 30

**Student Details**

**Name:** Farhan Ali

**Student ID:** 12761

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|----|-----|---|---------|
| Q1 | (a) | Find and explain Track and Search Radar Range equation  | Marks 6 |
|    | (b) | Explain working principle of Satellite communications system (GPS), and difference between triangulation & Trilateration? | Marks 4 |
| Q2 | (a) | Draw and Explain Radar Block Diagram  | Marks 6 |
|    | (b) | Find the escape velocity of satellite?  | Marks 4 |
| Q3 | (a) | Find out the orbital speed & Time period of satellite?  | Marks 6 |
|    | (b) | Explain different types of radar systems  | Marks 4 |

(Q1)

(a) Find and explain Track and Search Radar Range equations.

(Ans) Power density from radiating antenna

$$\frac{P_t}{4\pi R^2} \quad \because P_t \text{ Peak Transmitter Power}$$
$$\quad \quad \quad \because R = \text{distance from radar.}$$

Power density from directive antenna

$$\frac{P_t G_t}{4\pi R^2} \quad \because G_t \text{ transmit gain}$$

Power of reflected signal as target.

$$\frac{P_t G_t \sigma}{4\pi R^2} \quad \because \sigma = \text{radar cross section units}$$

Power density of reflected signal at the radar

$$\frac{P_t G_t}{4\pi R^2} \quad \sigma$$

Power of reflected signal from target  
and received by radar

$$P_r = \frac{P_t G_t}{4\pi R^2} \frac{\sigma A_e}{4\pi R^2} \quad \because P_t \text{ Power received}$$

$\because A_e \text{ effective area.}$

Power density by reflected signal is

$$P_r = \left( \frac{P_t G_t}{4\pi R^2} \right) \times \frac{1}{4\pi R^2}$$

$$= \frac{P_t G_t}{(4\pi R^2)^2}$$

If effective area of antenna  $A_e$ , received power.

$$P_r = \frac{P_t G_t A_e}{(4\pi R^2)^2}$$

For max range  $R_{max}$  received signal

$$P_r = S_{min}$$

$$S_{min} = \frac{P_t G_t A_e}{(4\pi)^2 R_{max}^4}$$

$$R_{max} = \left[ \frac{P_t G_t A_e}{(4\pi)^2 S_{min}} \right]^{\frac{1}{4}}$$

for Parabolic Antenna

$$G = \frac{4\pi A_e}{\lambda^2}$$

Hence

$$\Rightarrow R_{max} = \left[ \frac{P_t (4\pi A_e) \sigma A_e}{(4\pi)^2 S_{min}} \right]$$

$$R_{max} = \left[ \frac{P_t A_e \sigma}{4\pi \lambda^2 S_{min}} \right]^{1/4}$$

The noise power at the receiver is given by

$$N = k B_n T_s \quad \because \text{System Noise Temperature.}$$

$k$  = Boltzmann constant

$B_n$  = Noise bandwidth of receiver

\* signal power reflected from target and received by radar.

$$P_r = \frac{P_t G_t}{4\pi R^2} \frac{\sigma A_e}{4\pi R^2}$$

\* Average noise power.

$$N = k T_s B_n$$



\* Signal to Noise Ratio

$$S/N = P_r/N$$

$$S/N = \frac{P_t G^2 \lambda^2 \sigma}{(4\pi)^3 R^4 k T_s B_n L}$$

\* Track Radar Equation.

$$S/N = \frac{P_t G^2 \lambda^2 \sigma}{(4\pi)^3 R^4 k T_s B_n t}$$

=> when the location of a target is known and the antenna is pointed toward the target

\* Search Radar Equation

$$S/N = \frac{P_{av} A_e \sigma \Omega_s \sigma}{4\pi \Omega R^4 k}$$

=> when the target location is unknown and the radar has the search a target angular region to find it.

(Q 1)

(b) Explain working principle of satellite communication system (GPS) and difference between triangulation and trilateration?

(Ans) Principle of satellite communication

⇒ A satellite is a body that moves around another body in a mathematically predictable path called an orbit.

⇒ A repeater is a circuit which increase the strength of the signal it receives and retransmits it.

⇒ The frequency with which is sent into the space is called ~~Downlink~~ uplink frequency.

⇒ The frequency with which it is sent by the transponder is called downlink frequency.

⇒ GPS satellite circle the earth twice a day in a very precise orbit and transmit signal information to earth.

\* Difference Triangulation Vs Trilateration

Triangulation

- (1) All angles are measured in triangulation.
- 2) Distance of baseline is measured
- (3) Multiple bearing on an unknown target.
- 4) Reading taken from unknown location
- (5) The side length are computed on the basis of measured angle applying sine

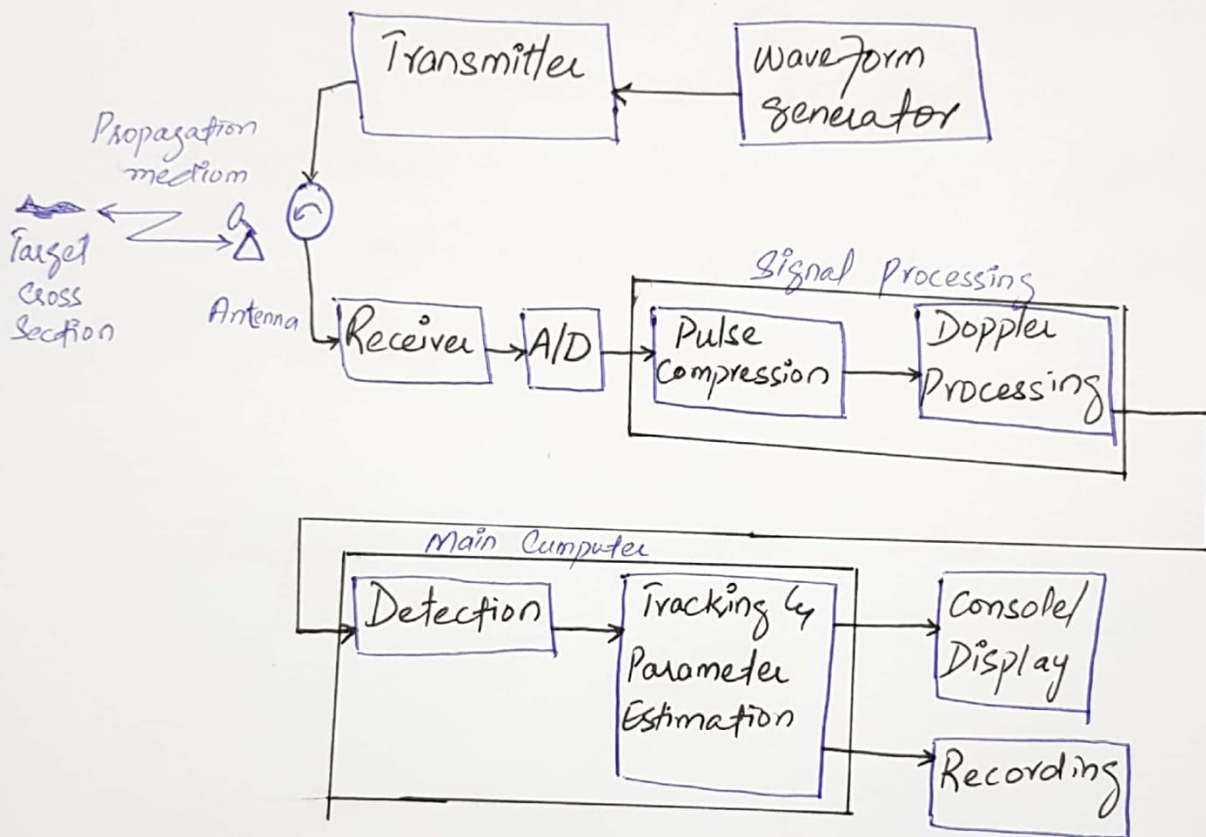
Trilateration

- 1) All sides are measured in trilateration
- 2) Azimuth of the initial line is measured
- (3) Multiple distance determination to an unknown target.
- (4) Reading taken from known location.
- (5) The angle are computed on the basis of measured side lengths applying cosine.



Q2  
(a) Draw and explain Radar Block Diagram?

Radar Block Diagram:



⇒ The basic parts of radar system are illustrated in the simple Block diagram of Fig. The radar signal usually a repetitive train of short pulses, is generated by the transmitter and radiated into the space by the antenna. If the output of the radar receiver is sufficiently large detection of a target is said to occur.



Q2

(b) Find the escape velocity of satellite.

(Ans) Escape velocity of satellite:-

→ consider a satellite of mass  $m$ , stationary on the surface of the Earth.

→ The binding energy of the satellite, on the surface of the Earth, is given by

$$BE = \left( \frac{GMm}{R} \right)$$

Therefore KE of satellite = BE

$$KE = \left( \frac{GMm}{R} \right)$$

$$\text{Therefore, } \frac{1}{2} m v_c^2 = \left( \frac{GMm}{R} \right)$$

$$v_c^2 = \frac{2GM}{R}$$

$$v_c = \sqrt{\frac{2GM}{R}} \rightarrow \textcircled{1}$$

where  $G = 6.67 \times 10^{-11}$   
 $M = 5.97 \times 10^{24}$   
 $R = 6.378 \times 10^6$

Pull all values in eq (1)

$$v_c = \frac{\sqrt{2 (6.67 \times 10^{-11}) (5.97 \times 10^{24})}}{6378000}$$

$$v_c = \frac{\sqrt{2 \times 6.67 \times 5.97 \times 10^{24-11}}}{6378000}$$

$$v_c = \frac{\sqrt{79.72 \times 10^{13}}}{6378000}$$

$$v_c = \sqrt{124992160}$$

$$v_c = 1118 \text{ m/s or } 11.2 \text{ km/s}$$

Q3

(a) Find out the orbital speed and time period of satellite?

Ans Orbital Speed:- It is the minimum speed required to put satellite in given orbit around earth.

$$v = \sqrt{\frac{GM}{r}} = \sqrt{\frac{gR^2}{r}}$$

Where  $g = 9.8 \text{ m/s}^2$

$RE$  = radius of earth.

The value for orbital velocity was found to be  $7.92 \text{ km/s}$

$$v = R \sqrt{\frac{g}{R+h}}$$

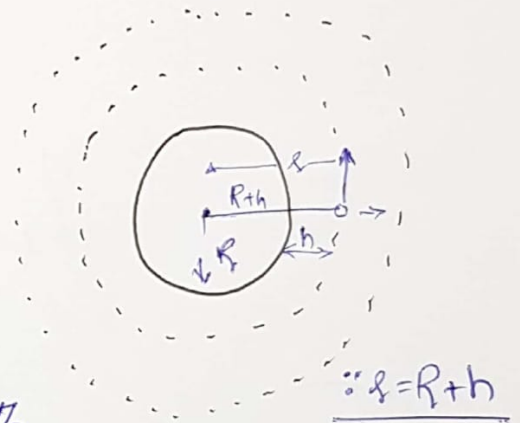
Satellite is close to earth.

$$R+h \approx R$$

$$v = R \sqrt{\frac{g}{R}}$$

$$v = \sqrt{g \times R} = \sqrt{gR}$$

$$v = 7.92 \times 10^3 \text{ m/s}$$



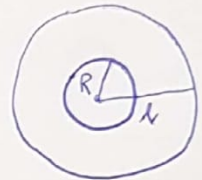


## \* Time Period of Satellite

Time taken by satellite for one complete revolution around earth.

$$T = \frac{\text{Distance travelled in one revolution}}{\text{orbital speed.}}$$

$$T = \frac{2\pi r}{v} = \frac{2\pi r}{R\sqrt{g/r}}$$



$$T = \frac{2\pi r}{R} \sqrt{\frac{r}{g}} = \frac{2\pi}{R} \sqrt{r^3/g}$$

$$T = \frac{2\pi}{R\sqrt{g}} \sqrt{r^3}$$

$$T = \frac{2\pi}{R\sqrt{g}} = \sqrt{(R+h)^3}$$

$$v = \frac{R\sqrt{g}}{\sqrt{r}}$$

It is independent of mass of satellite  
~~mass of satellite~~

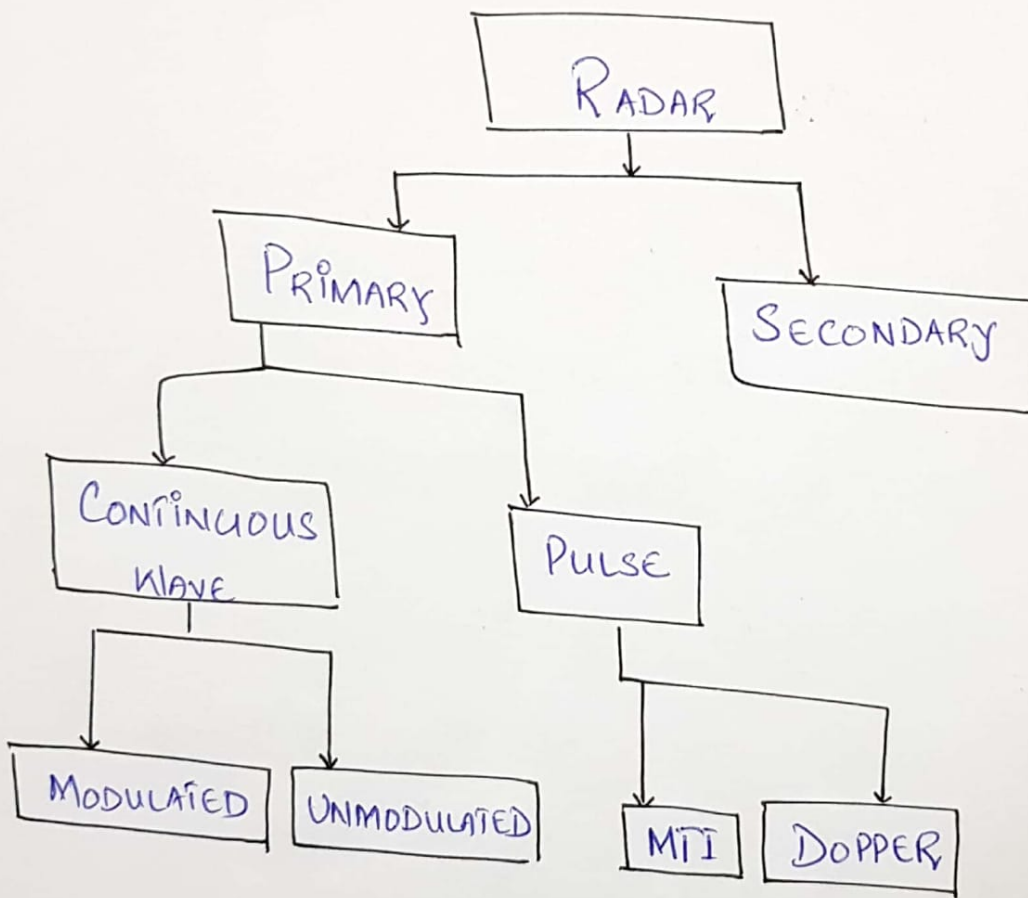
$$v \propto \frac{1}{\sqrt{r}}$$

Orbital velocity decrease with increase in orbital radius.

(Q3)

Explain different types of Radar systems?

(Ans) Types of Radar



(a) Primary Radar:-

Primary Radar relies solely on the energy that it has generated and radiated. being reflected back from the target. i.e. echo.

(b) Secondary Radar:-

It has some co-operation from the target- the target generates its own 'em' radiation.

Therefore Primary Radar has following types.

1) Pulse Radar:-

It sends high power and frequency pulses towards the target object. The range will depend on pulse repetition frequency.

(2) Continuous Wave Radar:-

It does not measure the range of the target but rather the rate of change of range by measuring the doppler shift of the return signals.