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x	x^2	y	y^2	xy
3	9	25	625	75
4	16	24	576	96
5	25	20	400	100
6	36	20	400	120
7	49	19	361	133
8	64	17	289	136
9	81	16	256	144
10	100	13	169	130
11	121	10	100	110
13	169	8	64	104

Q NO 1

(b)

x	y	xy	x^2
20	5	100	121
11	15	165	225
15	14	210	100
10	17	170	289
17	8	136	324
18	9	162	441
21	12	252	625
25	16	400	784
28	18	504	
$\Sigma x = 165$	$\Sigma y = 114$	$\Sigma xy = 2099$	$\Sigma x^2 = 330$

(a)

$$y = a + bx$$

$$y = a + bx$$

$$\Sigma y = na + b \Sigma x$$

P

$$\sqrt{P-T=0}$$

P-3

$$\sum xy = a \sum x + b \sum x^2$$

Now

$$\bar{x} = \frac{\sum x}{n} = \frac{165}{9} = \boxed{18.33}$$

$$\bar{y} = \frac{\sum y}{n} = \frac{114}{9} = \boxed{12.66}$$

Now to find b

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$= \frac{9(2099) - (165)(114)}{9 \sum x^2 - (165)^2}$$

$$a = \bar{y} - b\bar{x} \quad r=4$$

$$a = 12.66 - 0.00645(18.33)$$

$$a = 12.66 - 0.11$$

$$a = 12.55$$

$$\hat{y} = 12.55 + 0.0064x$$

x on y

$$\hat{x} = a + by$$

$$\hat{x} = 12.55 + 0.0064y$$

$$\hat{x} = 12.55 + 0.0064y$$

Q No 2

(a) A fair coin is tossed 5 times. Find the probabilities of obtaining various number of heads.

Answer

~~A fair coin is tossed 5 times~~

→ Let us regard the tossing of a coin as an experiment then we observe that

- Each toss of coin has possible outcome head and tail
- The probability of head (success) is $p = \frac{1}{2}$ and remain same for successive tosses
- the successive tosses of the coin are independent

Therefore the coin is tossed five times
no of head (success) has a binomial probability distribution with

$p + q = 1$

P-6.

$p = \frac{1}{2}$ and $n = 5$ the possible value of X are 0, 1, 2, 3, 4,

$$\begin{aligned} P(\text{no head}) = P(X=0) &= \binom{5}{0} \left(\frac{1}{2}\right)^0 \left(\frac{1}{2}\right)^5 \\ &= 1 \times \left(\frac{1}{2}\right)^5 \\ &= \left(\frac{1}{32}\right) \end{aligned}$$

$$\begin{aligned} P(1 \text{ head}) = P(X=1) &= \binom{5}{1} \left(\frac{1}{2}\right)^1 \left(\frac{1}{2}\right)^{5-1} \\ &= 5 \times \left(\frac{1}{2}\right)^5 = \boxed{\frac{5}{32}} \end{aligned}$$

$$\begin{aligned} P(3 \text{ head}) = P(X=3) &= \binom{5}{3} \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^{5-3} \\ &= 10 \times \left(\frac{1}{2}\right)^5 = \boxed{\frac{10}{32}} \end{aligned}$$

$$\begin{aligned} P(4 \text{ head}) = P(X=4) &= \binom{5}{4} \left(\frac{1}{2}\right)^4 \left(\frac{1}{2}\right)^{5-4} \\ &= 5 \times \left(\frac{1}{2}\right)^5 = \boxed{\frac{5}{32}} \end{aligned}$$

$$P(5 \text{ head}) = P(X=5) = \binom{5}{5} \left(\frac{1}{2}\right)^5 \left(\frac{1}{2}\right)^0 =$$

$$1 \times \left(\frac{1}{2}\right)^5 = \left(\frac{1}{32}\right)$$

Here Probability in table form

X	0	1	2	3	4	5
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Q2

part b

Solution

therefore the Binomial probability
dist with $n=10$

$$p = \frac{2}{3}$$

$$q = 1 - p$$

$$q = 1 - \frac{2}{3}$$

$$q = \frac{1}{3}$$

Let x denote the number of
won by A then

$$\textcircled{1} P(x \geq 4) = 1 - P(x < 4)$$

$$= 1 - \sum_{x=0}^3 \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= 1 - \left[\left(\frac{1}{3}\right)^{10} + 10 \left(\frac{2}{3}\right) \left(\frac{1}{3}\right)^9 + 45 \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^8 \right.$$

$$\left. + 120 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^7 \right]$$

$$1 - \frac{1}{59049} (1 + 20 + 180 + 960)$$

$$1 - 0.0197$$

$$P(x \geq 4) = 0.9803$$

$$ii) P(x \geq 4) = \binom{10}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^2$$

$$= 210 \cdot \left(\frac{16}{81}\right) \cdot \left(\frac{1}{9}\right)$$

$$\frac{3360}{59049}$$

$$P(x \geq 4) = 0.056$$

iii) $P(x=11) = f(0) =$ because x can take only values

0, 1, 2, 3, ..., 10.

iv) 6 or more games

$$P(x \geq 6) = \sum_{x=6}^{10} \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

P-9

$$2 \binom{10}{6} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^4 + \binom{10}{7} \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^3 +$$

$$\binom{10}{8} \left(\frac{2}{3}\right)^8 \left(\frac{1}{3}\right)^2 + \binom{10}{9} \left(\frac{2}{3}\right)^9 \left(\frac{1}{3}\right)^1$$

$$+ \binom{10}{10} \left(\frac{2}{3}\right)^{10} \left(\frac{1}{3}\right)^0$$

$$= 0.228 + 0.261 + 0.196 + 0.087$$

$$+ 0.018$$

$$P(X \geq 6) = 0.79$$

X ——— X

Q No 3

P-10

9	6	1	5	4	3	3	3	10	1
4	3	3	0	5	2	1	4	10	3
5	3	3	6	3	3	2	2	7	4
1	4	2	4	4	4	6	8	10	7
7	5	6	5	3	2	3	9	2	2

(a) Construct the ungrouped frequency distribution of the data

(b) Construct the grouped frequency distribution of these data.

Solution: given data

(1) X_0 (minimum value) = 0
 X_m (maximum value) = 10

(2) range = ~~$X_m - X_0$~~
= 10 - 0

= 10

Children Born
 x_i

8

0

1

1

4

2

8

3

11

5

5

6

4

7

3

8

2

9

1

10

3

$$N = 12$$

Now (b) The Grouped frequency data.

Children born group	f
0-1	5
2-3	19
4-5	13
6-7	7
8-9	3
10-11	3
	50