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Semester

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6<sup>th</sup>

Date

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No 2

A simply supported rectangular beam 16" wide  
 Draw a sketch of your final diagram.

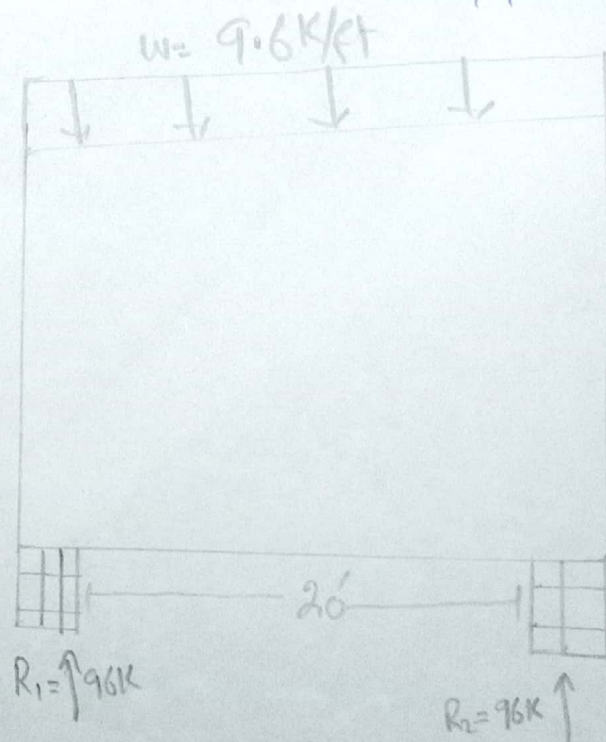
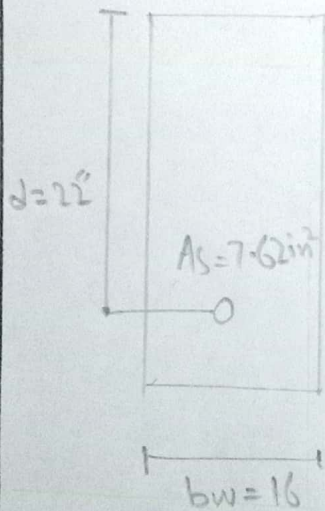
Sol

First of all find the unit load of beam

So  $b \times h_c$

$$= \frac{16}{12} \times 150 \Rightarrow 200 \text{ lb/ft} = 0.2 \text{ K/ft}$$

$$\text{So total factor load} = 9.4 + 0.2 \\ = 9.6 \text{ K/ft}$$



Step #01

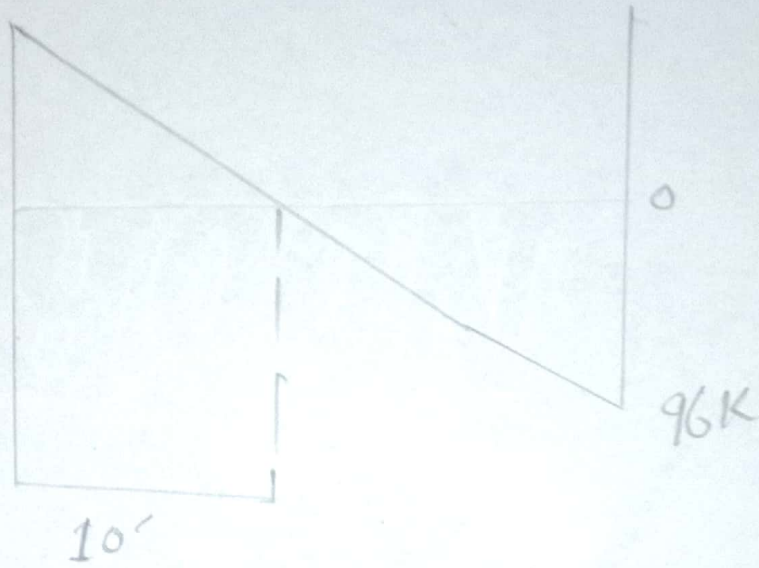
Find the value of  $R_1$  and  $R_2$

$$\text{Total load} = 9.6 \times \frac{20}{2} = 96 \text{ K}$$



Step #2 Draw its shear force diagram.

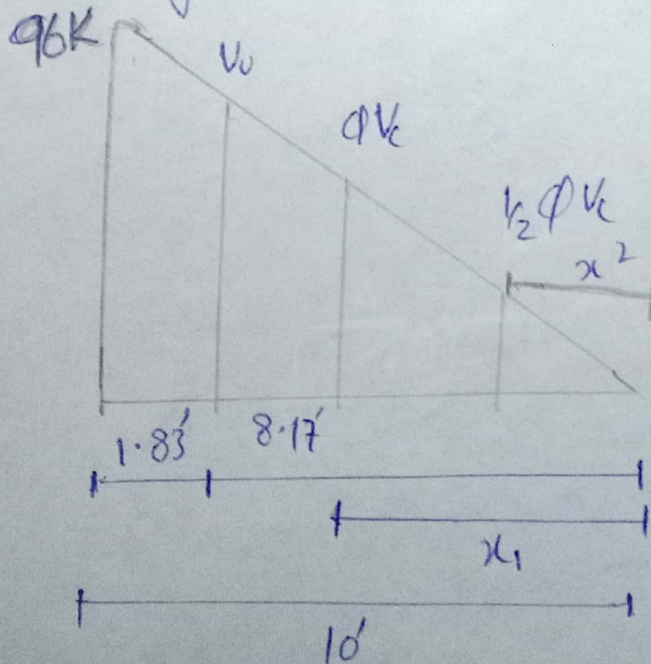
S.F.D  
(KIPS)



Step #3 Find the value of critical stress " $V_u$ " and its location.

As we know that critical section is located at distance " $d$ " from face of support =  $d = 22'' = 1.83'$   
value of critical shear at distance " $d$ " by

Similarity of triangles





From similar  $\Delta$ 's

$$\frac{96}{10} = \frac{V_u}{8.17}$$

$$V_u = 78.43 \text{ k}$$

Step #4 Find the value of " $\phi V_c$ " { " $\frac{1}{2} \phi V_c$ " }  
also its distance from zero shear to right side

$$\phi V_c = \phi \times 2 \times \sqrt{f_c} \times b_w \times d \Rightarrow 0.75 \times 2 \times \sqrt{4000} \times 16 \times 22$$

1000

$$\phi V_c = 33.40 \text{ k}$$

Location of  $\phi V_c$  by similarity of  $\Delta$ 's

$$\frac{96}{10} = \frac{33.40}{x_1}$$

$$x_1 = 3.48'$$

Now  $\frac{1}{2} \phi V_c = \frac{33.40}{2} = 16.70 \text{ k}$

Location of  $\frac{1}{2} \phi V_c \Rightarrow \frac{96}{10} = \frac{16.70}{x_2}$

$$x_2 = 1.74'$$



Step #5 Value of  $\phi V_s$  ( $V_u = \phi V_s + \phi V_c$ )

$$\text{So } \phi V_s = V_u - \phi V_c$$

$$\phi V_s = 78.43 - 33.40$$

$$\boxed{\phi V_s = 45.03 \text{ k}}$$

Step #16 check on section adequacy

$$\phi \times 8 \times \sqrt{f_c'} \times b \times d = \frac{0.75 \times 8 \times \sqrt{4000} \times 16 \times 22}{1000}$$

$$= 133.57 \text{ k}$$

As  $\phi \times 8 \times \sqrt{f_c'} \times b \times d > \phi V_s \rightarrow$  It means section is adequate

Step #07 check on min spacing for stirrups.

$$\phi \times 4 \times \sqrt{f_c'} \times b \times d = \frac{0.75 \times 4 \times \sqrt{4000} \times 16 \times 22}{1000} = 66.79 \text{ k}$$

$$\text{As } \phi \times 4 \times \sqrt{f_c'} \times b \times d > \phi V_s = 45.03 \text{ k}$$

Thus max spacing will be selected from the following

four condition

$$(1) s_{\max} = 24''$$

$$(2) \frac{d}{2} = \frac{22}{2} = 11''$$

$$(3) s_{\max} = \frac{A_v \times f_y}{0.75 \times \sqrt{f_c'} \times b \times w}$$



$$A_v = \frac{\pi}{4} \left(\frac{3}{8}\right)^2 = \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 16} = 17.40''$$

$$A_v = 0.11 \times 2$$

$$A_v = 0.22$$

$$4) f_{max} = \frac{A_v \times f_y}{50 \times b_w}$$

$$= \frac{0.22 \times 60000}{50 \times 16}$$

$$= 16.50$$

From the above four conditions least value of spacing from #3, U shaped will be selected

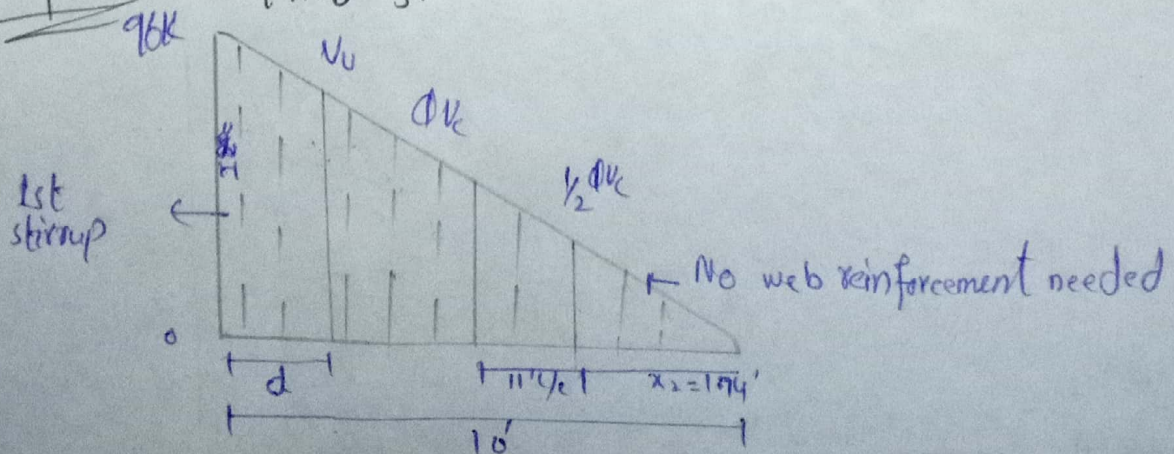
$$So s_{max} = 11'' c/c$$

step #08 Spacing of stirrup from/at critical section

$$S = \frac{\phi \times A_v \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{78.43 - 33.40}$$

$$= 48.4'' \approx 5'' c/c$$

step #9 Find sketch





= As we know that first stirrups from face of support =

$$\Rightarrow \frac{5}{2} = 2.5 \approx 2''$$

Q No 1 A reinforcement concrete slab is \_\_\_\_\_  
 \_\_\_\_\_ Draw sketch of your final design.

Given Data

→ Clear span b/w support = 15'

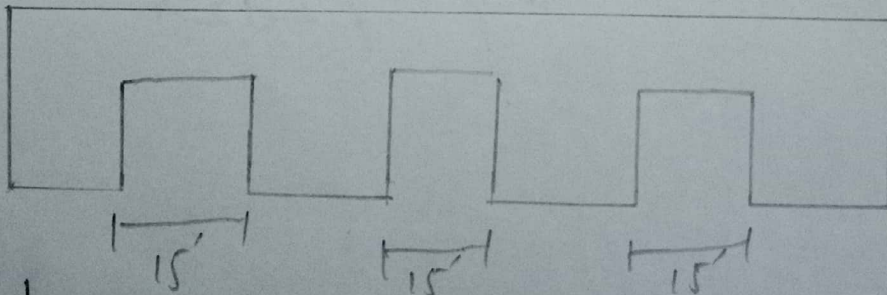
→ Factored live load = 160 lb/ft<sup>2</sup>

→ Service floor finish load = 20 lb/ft<sup>2</sup>

→  $f'_c = 4000$  psi

$f_y = 40$  ksi

Sol



Step # 01 Minimum thickness

By using formula

$$t_{min} = \frac{L}{28} = \frac{15}{28} = 6.4 \approx 6.5''$$



As  $f_y \rightarrow 40 \text{ksi}$

So we will multiply a factor with this thickness

$$\text{Factor} = \left( 0.4 + \frac{f_y}{100} \right)$$

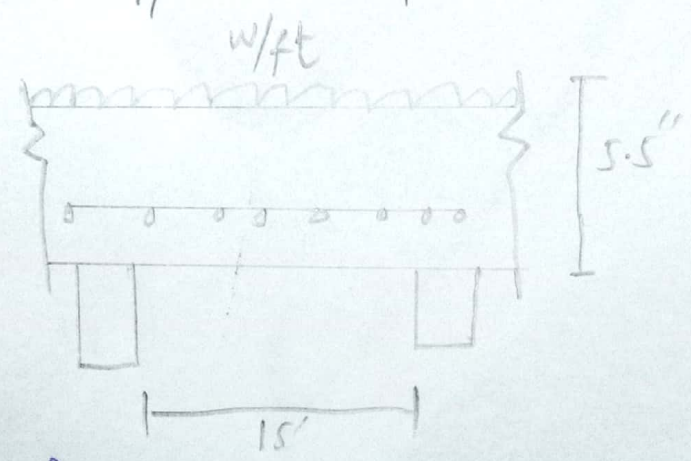
$$= \left( 0.4 + \frac{40}{100} \right) = 0.8$$

Hence the minimum thickness will be

$$6.5 \times 0.8$$

$$t_{\min} = 5.2 \approx 5.5''$$

Step # 2 ← Effective Depth.



By formula

$$d = t - \text{clear cover} - \frac{1}{2} (\text{dia of main bars})$$

$$= 5.5 - 0.75 - \frac{1}{2} \left( \frac{5}{8} \right)$$

$$d = 4.5''$$



Step # 03 Self weight of slab

By formula

$$\frac{t}{12} + \gamma_{\text{concrete}}$$

$$= \frac{5.5}{12} \times 150 = 68.75 \text{ lb/ft}^2$$

Step # 04 Total Factored Load

$$\text{Factored live load} = 160 \text{ lb/ft}^2$$

So the factored dead load will be

$$D.L = 1.2 (20 + 68.75) = 106.5 \text{ lb/ft}^2$$

$$\text{total factored load} = D.L + L.L$$

$$= 106.5 + 160$$

$$= 266.5 \text{ lb/ft}^2$$

$$= 0.2665 \text{ k/ft}^2$$

Step # 05 Ultimate moment

By using formula

$$M_u = \frac{w_u x l^2}{8} = \frac{0.2665 \times (15)^2 \times 12}{8}$$

$$M_u = 89.94 \text{ kips-inches}$$



Step #16

Area of steel for main bars by  
Trial and repeat method.

Trial #01

Let depth of compression block

$$a = 0.2 \times t$$

$$= 0.2 \times 5.5 \Rightarrow 1.1''$$

~~Ast = 0.63 in<sup>2</sup>~~

$$A_{st} = \frac{M_u}{\phi \times f_y \times \left(d - \frac{a}{2}\right)} = \frac{89.94}{0.90 \times 40 \times \left(4.5 - \frac{1.1}{2}\right)}$$

$$A_{st} = 0.63 \text{ in}^2$$

Trial #02

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{0.63 \times 40}{0.85 \times 4 \times 12} \Rightarrow 0.62 \text{ in}^2$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times \left(d - \frac{a}{2}\right)} = \frac{89.94}{0.90 \times 40 \times \left(4.5 - \frac{0.6}{2}\right)}$$

$$A_{st} = 0.59 \text{ in}^2$$

Trial #03

$$a = \frac{0.59 \times 40}{0.85 \times 4 \times 12} = 0.57''$$



$$A_{st} = \frac{89.94}{0.90 \times 40 \times \left(4.5 - \frac{0.57}{2}\right)} = 0.59 \text{ in}^2$$

So we will use  $A_{st} = 0.59 \text{ in}^2$

Step #7 Area of steel for distribution reinforcement.

By formula

$$A_{min} = 0.002 \times b \times t \rightarrow (\text{for Grade 40 steel})$$

$$= 0.002 \times 12 \times 5.5 \Rightarrow 0.132 \text{ in}^2$$

Step #8 Spacing for main bars

By formula

$$\text{Spacing} = \frac{A_b}{A_{st}} \times 12$$

We use #6 bar dia =  $\left(\frac{6}{8}\right)''$

$$\text{Area} = \frac{\pi}{4} \left(\frac{6}{8}\right)^2 = 0.442 \text{ in}^2$$

Step #9 spacing for distribution bars

$$\text{Spacing} = \frac{A_b}{A_{st}}$$

We use #5 bar so

$$\text{dia} = \left(\frac{5}{8}\right)'', \text{Area} = \frac{\pi}{4} \left(\frac{5}{8}\right)^2 = 0.31 \text{ in}^2$$

$$\text{Spacing} = \frac{0.31}{0.132} \times 12 = 28.1'' \approx 28'' \text{ c/c}$$

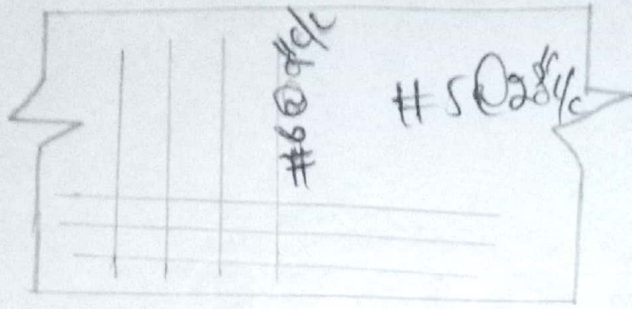
Step #10 Find sketch

$$f'_c = 4 \text{ ksi}, f_y = 40 \text{ ksi}$$

Main steel #6 at 9" c/c

Distribution steel #5 at 28" c/c





Q No 3 Calculate the axial ultimate —  
— design necessary spirals

Step #01 Find gross area of concrete

$$A_g = b \times b \text{ (since it is square tied column)}$$

$$A_g = 12 \times 12 = 144 \text{ in}^2 \text{ (Actual)}$$

Step #02 Find the area of steel

$$\text{Since } A_s = 5\% \text{ of } A_g$$

$$= 0.05 \times 144$$

$$A_s = 7.2 \text{ in}^2$$

Step #03 Ultimate load carrying capacity

$$P_u = \phi \times 0.80 \times \{0.85 \times f'_c \times (A_g - A_s) + A_s \times f_y\}$$

$$= 0.65 \times 0.80 \{0.85 \times 4 \times (144 - 7.2) + 7.2 \times 60\}$$

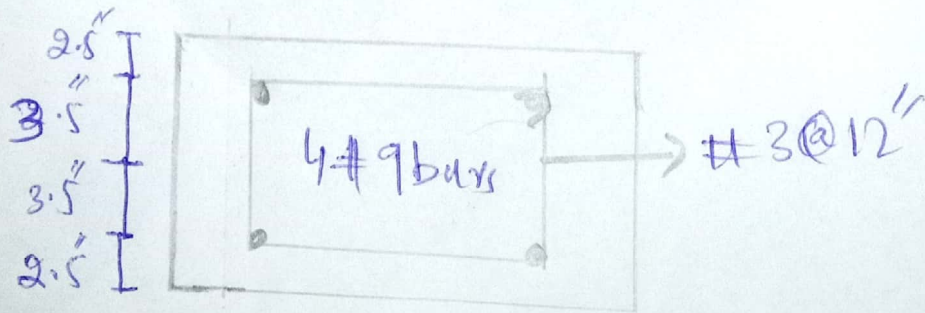
$$P_u = 466.50 \text{ K}$$



### Step#04 sketch and design of Ties (c/c to distance)

From the below value we choose the least value of all thus.

- (1)  $16 \times \text{dia of long bar} = 16 \times 9/8 = 18''$
- (2)  $48 \times \text{dia of Tie bar} = 48 \times 3/8 = 18''$
- (3) least column dimension =  $12''$   
 so c/c distance b/w ties =  $12''$



Since it is a tied square column so there is no spiral stirrup used, the stirrup used is of rectangular shape due to the specification of the structure thus we will use tie stirrups instead.



Q4 Design a square footing ——— sketch of your final design.

Step #01

let  $h = 24''$

Step #02

$$\begin{aligned} \text{Total weight} &= \text{wt of soil} + \text{wt of Re} \\ &= 3 \times 120 + 2 \times 150 \\ &= 660 \text{ psf} = 0.660 \text{ ksf} \end{aligned}$$

Step #03

Effective bearing capacity.

$$q_e = q_u - w$$

$$q_e = 2.50 - 0.660$$

$$q_e = 1.84 \text{ ksf}$$

Step #04

Required Area for foundation

$$A_{req} = \frac{\text{Service load}}{q_e} = \frac{100 + 120}{1.84} = 119.57 \text{ ft}^2$$

Step #05

Since foundation is square

$$A_{req} = b \times b = 119.57 \Rightarrow b \approx 11'$$



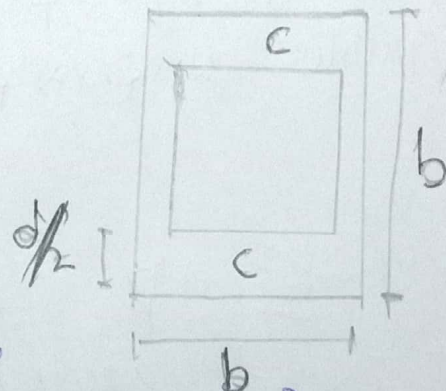
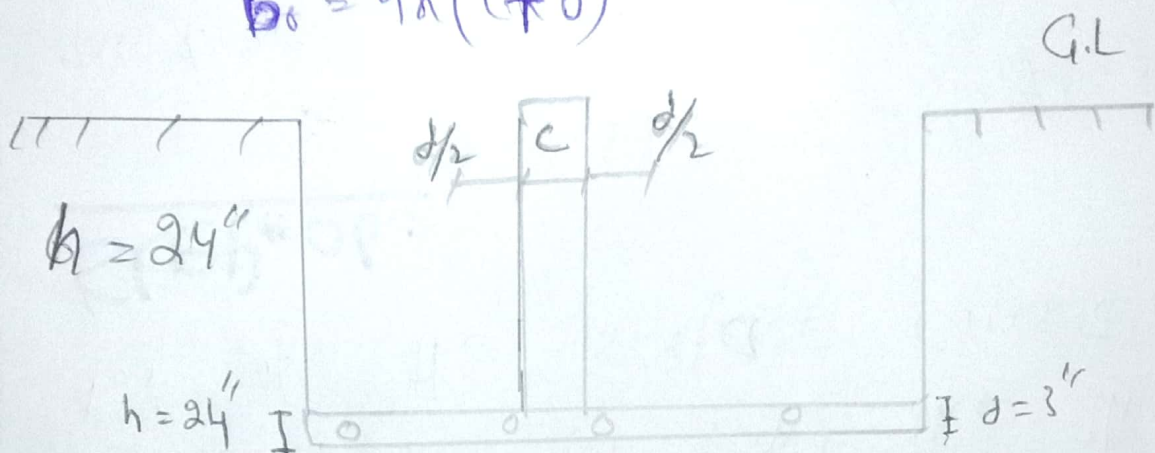
(14) 7834  
Step #6 upward bearing capacity of soil

$$V_{up} = \frac{\text{factored load}}{(B)^2} = \frac{1.2 \times 100 + 1.6 \times 120}{11^2}$$

$$V_{up} = 2.58 \text{ k/ft}^2$$

Step #7 Punching shear

$$b_o = 4 \times (c + d)$$



$$d = h - c.c - \text{dia of bar} - \frac{1}{2} d_b$$

$$= 24 - 3 - 1 - \frac{1}{2}(1) = 19.5''$$

$$b_o = 4 \times (16 + 19.5) = 142''$$

Take #8 bar

$$\text{dia} = \frac{8}{8}'' = 1''$$



Step # 08

$$V_{u2} = q_{up} \times \left[ B^2 - (c+d)^2 \right]$$

$$= 2.58 \times \left[ 11^2 - \frac{(16+19.5)^2}{12} \right]$$

$$V_{u2} = 289.60 \text{ K}$$

Step # 09

$$\phi V_{c/p} = \phi \times 4 \times \sqrt{f'_c \times b \times d}$$

$$= \frac{0.75 \times 4 \times \sqrt{4000 \times 149 \times 19.5}}{1000}$$

$$\phi V_{c/p} = 525.38$$

Step # 10 Beam shear/one way shear check

$$V_{u1} = q_{up} \times B \times \left[ \frac{B}{2} - \frac{c}{2} - d \right]$$

$$V_{u1} = 2.58 \times 11 \times \left[ \frac{11}{2} - \frac{16}{2} - 19.5 \right]$$

$$V_{u1} = 90.95 \text{ K}$$

Step # 11

Self shear capacity

$$C_{pvc} = \phi \times 2 \times \sqrt{f'_c \times b \times d}$$

$$= \frac{0.75 \times 2 \times \sqrt{4000 \times (11 \times 12 - 16)}}{1000}$$



$$= 10.04k > VU_1 \Rightarrow \text{O.K}$$

Step # 12 ultimate moment

$$M_u = \frac{V_u P \times B}{8} \times (B - C)^2 = \frac{2.58 \times 11}{8} \times \left(11 - \frac{16}{12}\right)^2$$

$$M_u = 331.49 \text{ K}' \approx 3977.93 \text{ K}'$$

Step # 13 Area of steel for main bars by trial and Repeat method.

Trial # 01

$$\text{let } a = 0.2 \times h = 0.2 \times 2.4 = 4.8''$$

$$A_s = \frac{M_u}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{4.8}{2}\right)} = 8.56 \text{ in}^2$$

Trial # 02

$$a = \frac{A_s \times f_y}{0.85 \times f_c' \times b} = \frac{8.56 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.53''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.53}{2}\right)} = \boxed{7.197 \text{ in}^2}$$

Trial # 03

$$a = \frac{7.197 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.28''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.28}{2}\right)} \Rightarrow \boxed{7.1 \text{ in}^2}$$



So that area =  $7.1 \text{ m}^2$

Step # 14 check the min reinforcement by the following os method.

$$(a) A_{smin} = 0.0018 \times B \times h = 0.0018 \times (11 \times 12) \times 24 = 5.70 \text{ in}^2$$

$$(b) A_{smin} = \frac{200}{f_y} \times B \times d = \frac{200}{60000} \times (11 \times 12) \times 19.5 = 8.58 \text{ in}^2$$

$$(c) A_{smin} = \frac{3 \times \sqrt{f_c}}{f_y} \times B \times d = \frac{3 \times \sqrt{3000}}{60000} \times (11 \times 12) \times 19.5$$

$$= 7.05 \text{ in}^2$$

From the above value greater value will be selected thus  $A_{smin} = 8.58 \text{ in}^2$

Step # 15 using # 8 bar

$$A_b = 0.785 \text{ in}$$

$$A_b \text{ of bars} = \frac{A_s}{A_b} = \frac{8.58}{0.785} = 10.92 = 11 \text{ bars}$$

in each direction