

ID: 7313

Pg 1

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Paper: Hydraulics Engineering.

Qno: 1. A prototype - - - - -
- - - - - viscosity μ .

Soln.

The pressure drop ΔP is expected to depend upon the gate opening h , the overall depth d , the velocity V , density ρ & viscosity μ .

The relevant variable.

$\Delta P, h, d, V, \rho, \mu$.

Dimension.

$$\Delta P = ML^{-1}T^{-2}$$

$$h = L$$

$$d = L$$

$$V = LT^{-1}$$

$$\rho = ML^{-3}$$

$$\mu = ML^{-1}T^{-1}$$

Number of variable = $n = 6$.

Number of independent dimension $M = 3$ (M, L, T).

Number of non-dimensional group $n - M = 3$.

Chose $M = 3$ scaling variable; geometric (d);

kinematic / time - dependent (V), dynamic / mass dependent (ρ).

From dimension less group by non-dimensionalizing the remaining variable = $\Delta P = f(h, \mu)$

$$\pi_1 = \rho d^a v^b f^c$$

$$M^0 L^0 T^0 = [ML^{-1}T^{-2}]^a [LT^{-1}]^b [ML^{-3}]^c$$

$$= M^{1+c} L^{-1+a+b-3c} T^{-2-b}$$

$$M = 0 = 1+c \Rightarrow c = -1$$

$$T = 0 = -2-b \Rightarrow b = -2$$

$$L = 0 = -1+a+b-3c \Rightarrow a = 1+3c-b = 0$$

$$\Rightarrow \pi_1 = \rho V^{-2} P^{-1} = \frac{VP}{fV^2}$$

Now $\pi_2 = \frac{f}{d}$ (by inspection, since f is the

length. $\pi_2 =$

$$\pi_2 = v d^a v^b f^c$$

$$M^0 L^0 T^0 = (ML^{-1}T^{-1})^a [L]^b [LT^{-1}]^c [ML^{-3}]^c$$

$$= M^{1+c} L^{-1+a+b-3c} T^{-1-b}$$

$$M = 0 = 1+c \Rightarrow c = -1$$

$$T = 0 = -1-b \Rightarrow b = -1$$

$$L = 0 = -1+a+b-3c \Rightarrow 0 = 1+3c-b = -1$$

$$\Rightarrow \pi_2 = \mu d^{-1} v^{-1} P^{-1} = \frac{\mu}{\rho v d}$$

Recognition of the Reynold number suggest that we replace π_2 by $\pi_2^{-1} =$

$$[\pi_2]^{-1} = \frac{\rho v d}{\mu}$$

Hence dimensional Analysis yield:

$$\text{i.e. } \pi_1 = f(\pi_2, \pi_3)$$

$$\frac{\Delta P}{\rho V^2} = f\left[\frac{h}{d}, \frac{\rho V d}{\mu}\right]$$

Part a:

Dynamic similarity requires that all non-dimensional groups to be the same in model and prototype.

i.e.

$$\pi_1 \left[\frac{\Delta P}{\rho V^2}\right]_p = \left[\frac{\Delta P}{\rho V^2}\right]_m$$

$$\pi_2 \left[\frac{h}{d}\right]_n = \left[\frac{h}{d}\right]_m \quad \text{Similar shape i.e. geometric similarity.}$$

$$\pi_3^{-1} \left[\frac{\rho V d}{\mu}\right]_p = \left[\frac{\rho V d}{\mu}\right]_m$$

From the last, we have a velocity ratio

$$\frac{V_p}{V_m} = \frac{(\mu/\rho)_p}{(\mu/\rho)_m} \quad \frac{d_m}{d_p} = \frac{0.002/800 \times 1}{1.0 \times 10^{-6} \times 5} = 0.5$$

$$\text{Thus ; } V_m = \frac{V_p}{0.5} = \frac{3.0}{0.5} = 6 \text{ m/s.}$$

Part: b:-

The ratio of the quantities of flow is

$$\frac{Q_p}{Q_m} = \frac{(\text{Velocity} \times \text{area})_p}{(\text{Velocity} \times \text{area})_m} = \frac{V_p}{V_m} \left[\frac{d_p}{d_m} \right]^2 = 0.5 \times 5^{-2} = 12.5.$$

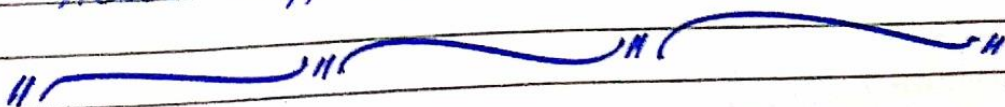
Part: c:-

simply for the Pressure drop.

$$\pi_1 = \left[\frac{\Delta P}{f V^2} \right]_p = \left[\frac{\Delta P}{f V^2} \right]_m \Rightarrow \frac{(\Delta P)_p}{(\Delta P)_m} = \frac{f_p}{f_m} \left[\frac{V_p}{V_m} \right]^2$$

$$= \frac{800}{1000} \times 0.5^2 = 0.2.$$

$$\text{Hence } \Delta P_p = 0.2 \times \Delta P_m = 0.2 \times 60 = 12.0 \text{ kPa.}$$



Qno: 2 : Design a Practical
 one another.

Sol:

$$T = 731, \quad G = 2.4, \quad C_u = 0.$$

$$1: \text{Humidity} = \frac{C_u W}{W(G - C_u + 1)} = \frac{120 \times 731 \times 1000}{1000(2.4 - 0 + 1)}$$

$$25800 \text{ M.}$$

$$\text{Let } H_w = 25000.$$

$$\text{Thus } 25800 > H_w \text{ } 25000.$$

So it is low gravity.

2: Top width "a"

$$\text{free board} = 1.5 H_w = 1.5 \times 25000$$

$$F.B = 37500.$$

$$\text{Height of Dam} = H_D = H_w + F.B.$$

$$H_D = 25000 + 37500$$

$$H_D = 62500.$$

$$a = 14\% \text{ of } H_D.$$

$$= 0.14 \times 62500$$

$$a = 8750.$$

5: Base width 'b' (with out off set).

i) for no sliding criteria.

$$b' = \frac{Hw}{\mu G} = \frac{25000}{0.7 \times 2.4} = 14880.95.$$

$$b' \approx 14880 \text{ m.}$$

ii) for non tension criteria

$$b' = \frac{Hw}{\sqrt{G}} = \frac{25000}{\sqrt{2.4}} = 16137.43$$

$$b' \approx 16137 \text{ m.}$$

4:- Depth of vertical Portion on v/s side.

$$h' = 2a\sqrt{G - C_u}$$

$$h' = 2 \times 8750 \sqrt{2.4 - 0}$$

$$h' = 27110.88$$

$$h' \approx 27110 \text{ m.}$$

6:- Up stream off set :-

$$\frac{a}{16} = \frac{8750}{16} = 546.87 \text{ m}$$

6:- Depth below the water level to the end of inclined portion in U/s: $3.14 a \sqrt{a}$

$$= 3.14 (8750) \sqrt{2.4}$$

$$= 42564.08 \text{ m}$$

7:- Total width of the base of the dam

$$b = b' + \frac{a}{16}$$

$$b = 16137 + \frac{8750}{16}$$

$$b = 16683.87$$

$$8:- \text{Tan } \theta = \frac{b'}{H} = \frac{16137}{25000}$$

$$\theta = \tan^{-1} \left(\frac{16137}{25000} \right)$$

$$\theta = 32.84^\circ$$

9:- Depth of vertical Portion on D/s

$$\text{Tan } \theta = \frac{a}{d'} = \frac{8750}{d'}$$

$$\left(\frac{16137}{25000} \right) d' = 8750$$

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$$d' = \frac{8750 \times 25000}{16137} = 13555.80 \text{ m.}$$

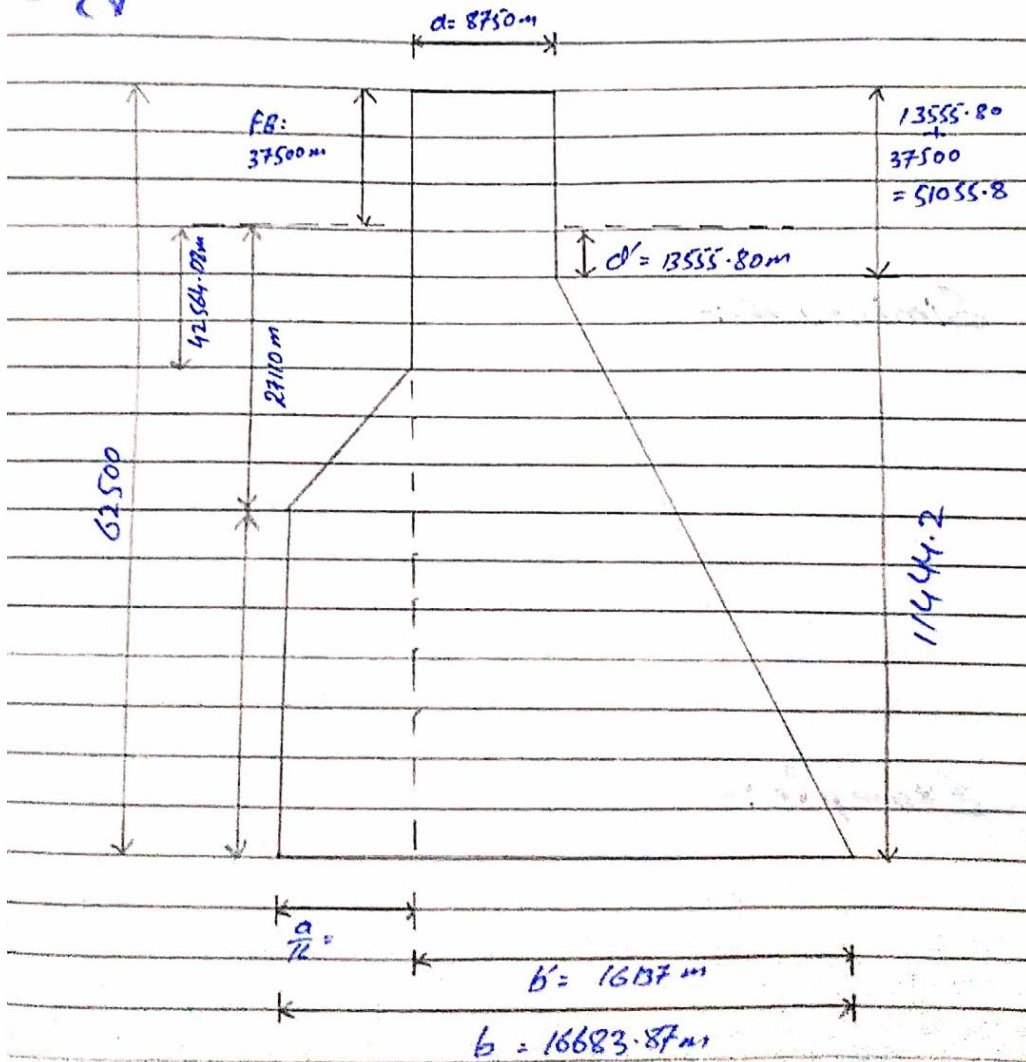
$$d = 13555.80 \text{ m.}$$

depth of vertical portion.

$$d = d' + FB$$

$$13555.80 + 37500 = 51055.8 \text{ m.}$$

Diagram:-



Q3:- Using any model
 analysis.

Dimensional Analysis:-

In engineering and science dimensional analysis of the relationship between different physical quantities by identifying their base quantities such as length, mass, time and electric charge and units.

The dimensional analysis or more specially the factor-label method also known as the unit factor method.

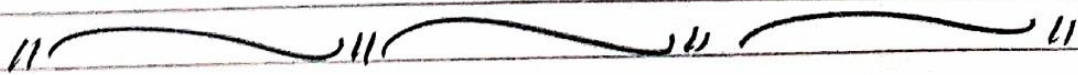
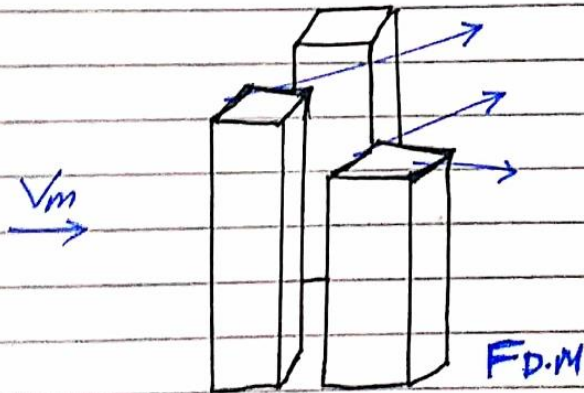
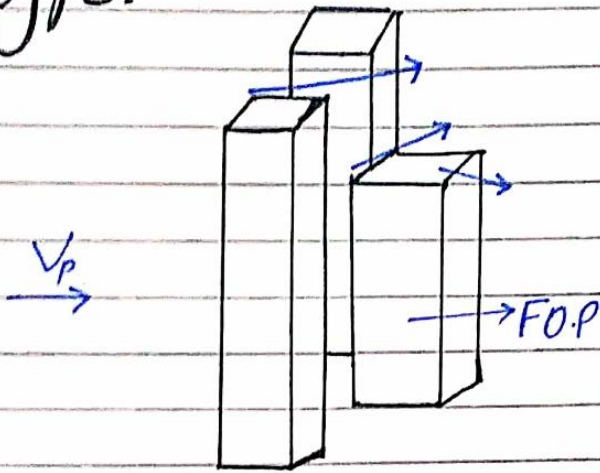
Similitude:-

Similitude is a concept applicable to the testing of engineering models. A model is said to have similitude with the real application if the two share geometric similarity, kinematic similarity and dynamic similarity. Similitude and similitude are interchangeable in this context.

Example:-

The velocity at any point in the model flow must be proportional (by a constant scale factor) to the velocity at the corresponding point in the ~~the~~ prototype flow.
 Similarly of motion.

Prototype:



Q4:- What will be the -----
----- in detail.

Ans:- Particle diameter:-

The diameter of the particle is directly proportional to the fall velocity because greater the size of particle so it will tend to move faster as compared to the particle of small size thus there will be more gravitational force on particle of greater size so it will fall quickly due to its weight.

Particle Density:-

Density of the particle is directly proportion to the rate of fall velocity since particle with high density tends to settle down early compared with the particle of density.

Particle concentration:-

Concentration of particle size will considerably effect its fall velocity as the section having greater concentration will be settled down at the place thus causing the more fall velocity comparing with section of low concentration.

Particle shape:-

Particle having regular shape tends to be effected more than irregular shape since regular shape particles have even surfaces which offers very little or no ~~offer~~ friction while particles with irregular shape offers more friction as the particle with smaller surface area are more likely to be effected due to their less resistance.

Viscosity of water:-

From the experimental study we can see that parameter, such as temperature and pressure changes the magnitude of viscosity so the section of water more temperature and pressure will fall objectively more due to increase in the kinetic energy. So fall velocity will be more.

Turbulence of water:-

Turbulence of water depends upon the different factor such as velocity. It will effect the velocity because of its zigzag motion thus the velocity varies at every point which is why it effect the fall velocity moreover increase the kinetic energy tends to effect the fall velocity compared with steady fluid.

