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Sec :- "A"

Subject :- Intro to Structure Dynamic
& Earthquake Engg:

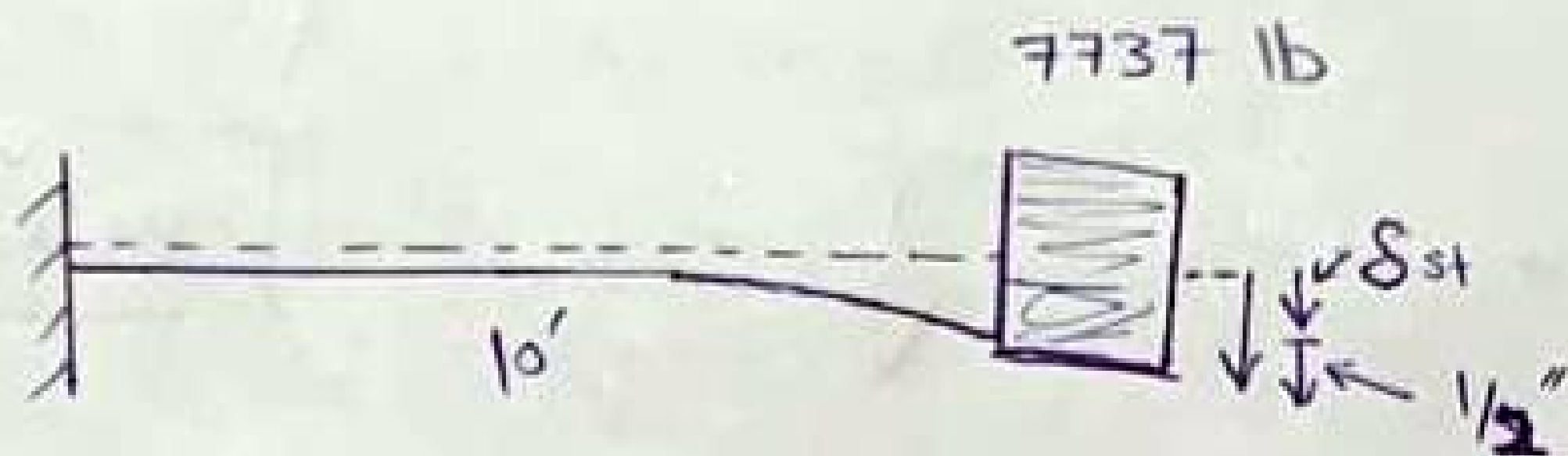
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Isra National University
Peshawer

Q No 1 :-

Page No (1)

Given Data :-



$$L = 10'$$

$$E = 29000 \text{ Ksi}$$

$$I = 150 \text{ in}^4 \text{ Sst}$$

Deflection due to ~~7737~~ 7737 lb

Solution :-

$$Ku + C\dot{u} + m\ddot{u} = P(t)$$

In our case system is undamped ($c=0$) undergoing free vibration. $P(t) = 0$

Hence General EDM become $Ku + m\ddot{u} = 0 \rightarrow \textcircled{1}$

$$K = 3EI/L^3$$

$$= \frac{3 \times (29000 \frac{\text{K}}{\text{in}^2}) (150) \text{ in}^4}{(10 \times 12 \text{ in})^3}$$

$$= 7.55 \text{ K/in}$$

In order to eliminate the chances of mistakes of during calculation, it is appropriate to use fundamental units like lb, ft, sec or kg, m, sec

$$K = 7.55 \text{ K/in} = (7.55) \times (1000) (12)$$

$$K = 90625 \text{ lb/ft}$$

$$m = \frac{W}{g} = \frac{7737}{32.2} = \boxed{240.28 \text{ Slug}} \quad P(2)$$

$$\omega_n = \sqrt{k/m} = \sqrt{\frac{90625}{240.28}}$$

$$\omega_n = 19.42 \text{ rad/sec}$$

$$T_n = \frac{2\pi}{\omega_n} = \frac{2\pi}{19.425} = \boxed{0.323 \text{ Sec}}$$

Put m & k in eqn (1)

where k is in lb/ft & m is

$$\boxed{\text{lb sec/ft}}$$

⇒ General Solution to EOM for undamped free vibration,

$$u(t) = u(0) \cos(\omega_n t) + \frac{\dot{u}(0)}{\omega_n} \sin(\omega_n t)$$

$$u(t) = \frac{1}{24} \cos(19.425t) + 0 =$$

$$= \frac{1}{24} \times \cos 19.42t$$

Equivalent static force at any time is

$$F_s(t) = k \cdot u(t) = \frac{90625 \times \cos(19.425t)}{24}$$

$$= \boxed{3776 \cos(19.25t)}$$

P(3)

Amplitude of dynamic displacement
 u_0 for undamped free vibration is

$$u_0 = \sqrt{\left(u(0)\right)^2 + \left(\frac{\dot{u}(0)}{\omega_n}\right)^2}$$

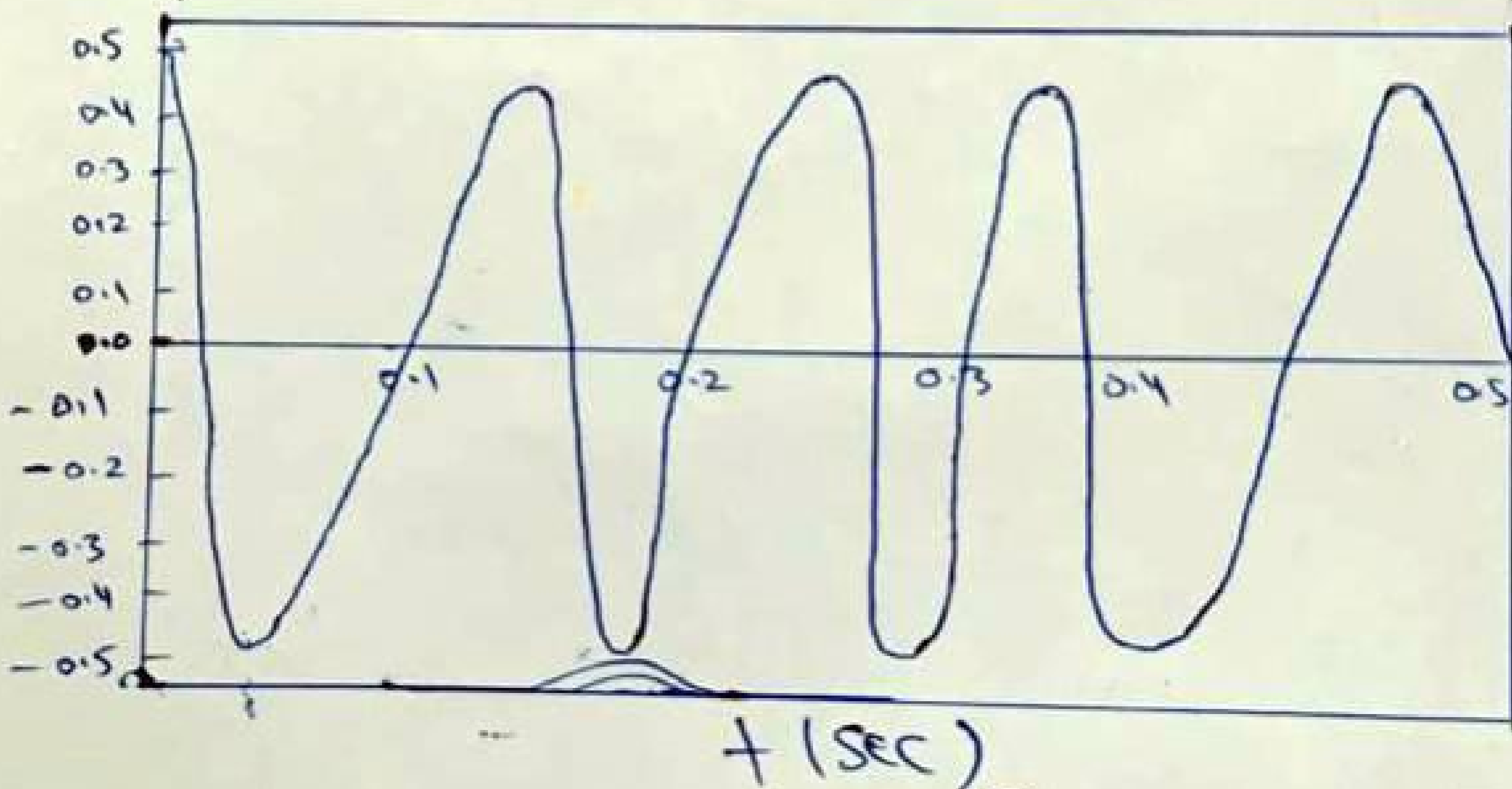
$$= \sqrt{\left(\frac{1}{24}\right)^2 + 0}$$

$$= \frac{1}{24} \text{ ft}$$

Amplitude of Equivalent
 Static force f_{so} .

$$k u_0 = 90625 \times \frac{1}{24}$$

$$k u_0 = 3776$$



Variation of displacement

Given Data Q No 2

P(4)

S (Damping ratio) of reinforced concrete
with Cracking Considered ~~3-5%~~
= 3-5% = 3%

Required Data :-

Develop and solve the Eqn showing
Variation in equivalent static force
with time.

→ Draw graph to show the variation
of displacement with time the
variation of equivalent static
force with time.

Solution :-

EOM for damped force vibration

$$Ku + Cu + m\ddot{u} = 0 \rightarrow \textcircled{1}$$

from data,

$$K = 90625 \text{ lb/ft}$$

$$\omega_n = 19.36 \text{ or } 20 \text{ rad/sec}$$

$$m = 240.28$$

We know that

$$C = S \times 2m \omega_n$$

$$= (0.03) \times 2(240.28)(19.42)$$

$$\boxed{C = 279.97} \text{ or } 280 \text{ lb-sec/ft}$$

Put the value of Eq (1)

P(5)

$$90625u + 280.76\dot{u} + 240.28$$

Solution to the EOM from damped
free vibration is.

$$u(t) = e^{-\zeta \omega_n t} \left[u(0) \cos(\omega_D t) + \frac{1}{\omega_D} \left[\dot{u}(0) + u(0) \zeta' \omega_n \right] \sin \omega_D t \right]$$

$$\omega_D = 19.36 \text{ rad/sec}$$

$$u(t) = e^{-0.03(19.36)t} \left[\frac{1}{24} \times \cos(19.36t) + \frac{1}{19.36} \times \left[0 + \frac{1}{24} \times 0.03 \right] \times 19.36 \times \sin(19.36t) \right]$$

$$u(t) = e^{-0.5808t} \left[0.041 \times \cos(19.36t) + 0.0516 \times \sin(19.36t) \right]$$

$$f_s(t) = k \cdot u(t) \Rightarrow 90625 \times u(t)$$

$$f_s(t) = e^{-0.5808t} \left[(90625 \times 0.041) \cos(19.36t) + 90625 \times 0.0516 \times \sin(19.36t) \right]$$

$$f_s(t) = e^{-0.5808t} \left[3715.62 \cos(19.36t) + 90625 \cdot 0.0516 \sin 19.36t \right]$$

Q No 3

P(6)

Given Data :-

$$\text{Force} = 60 \text{ kips}$$

$$U_s = 7737 / 1000 = 7.737 \text{ m}$$

After $T = 7$ (Cycles)

Completed = 3.57 Sec

$$U_{s+1} = 2.286 \text{ cm} = 0.9 \text{ in}$$

Ignore the Vertical Vibration

Required :-

- Damping ratios
- Natural Period of undamped vibration
- Stiffness of Structure
- Weight of tank
- Damping coefficient
- etc

Solution

(a) $\zeta =$ Damping ratio = ?

$$\text{Ans: } T = \frac{1}{2\pi\zeta} \ln \left| \frac{41}{45+11} \right|$$

By Putting Value

$$7 = \frac{1}{2(3.14)\zeta} \ln \left| \frac{7.737}{0.9} \right|$$

$$\zeta (7 \times 2 \times 3.14) = 2.151$$

$$\zeta (43.96) = 2.151$$

$$\zeta = 2.151 / 43.96$$

$$= 0.0489$$

$$\zeta = 4.89\%$$

$$(b) T_n = ?$$

P(8)

As 7 Cycle completed in 3.57 Sec

thus time required to complete

$$\text{one Cycle} = 7 / 3.57 = 1.96 \text{ Sec}$$

$$T_D = 1.96 \text{ Sec}$$

$$T_n = T_D (\sqrt{1 - \zeta^2})$$

$$= 1.96 (\sqrt{1 - (0.0489)^2})$$

$$T_n = 1.957 \text{ Sec}$$

Natural
Period of
undamped
vibration

(c) Stiffness of Structure

" $K = ?$ "

$$\text{As } K = \frac{F \cdot \cos \theta}{2}$$

$$K = \frac{60 \cos 60^\circ}{2}$$

$$= 15 \text{ K/in}$$

$$K = 18000 \text{ lb/ft}$$

(d) weight of tank
"w = ?"

P(9)

$$w_n = \sqrt{k/m} = \sqrt{(k/w/g)} = \sqrt{\frac{k \cdot g}{w}}$$

$$w^2 = k \cdot g / w \Rightarrow w = k \cdot g / w_n^2$$

By putting value of $w_n = 2\pi/T_n$

$$w = k \cdot g / (4\pi^2/T_n^2) = k \cdot g \left(\frac{T_n^2}{4\pi^2} \right)$$

$$w = 12000 \frac{\text{lb}}{\text{ft}} \cdot 32.2 \frac{\text{ft}}{\text{sec}} \left(\frac{(1.957)^2}{4(3.14)^2} \right)$$

$$w = 56284.75 \text{ lb} = \boxed{56.284 \text{ klb}}$$

(e) Damping Coefficient "C = ?"

It is known that

$$\zeta = \frac{C}{2m w_n}$$

$$C = \zeta (2m w_n) = \zeta \left(2m \left(\frac{2\pi}{T_n} \right) \right)$$

By putting value

$$C = \frac{0.0489 \left(2 \left(\frac{56284}{32.2} \right) \left((2)(3.14) \right) \right)}{1.957}$$

$$C = 548.57 \text{ lb-sec/ft}$$

(f) "No of Cycles to reduce displacement altitude from
" 7.737 in to 0.5 in "

P(10)

$T = ?$

$$T = \frac{1}{2\pi\zeta} \ln \left| \frac{u_1}{u_{s+1}} \right|$$

$$= \frac{1}{2(3.14)(0.0489)} \ln \left| \frac{7.737}{0.5} \right|$$

$$= (3.256) (2.151)$$

$$= 7.004 \text{ OR}$$

$$T = 7 \text{ Cycles}$$