

MID Online

Exame

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Section "A"

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Subject PRCD-I

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Q NO 01 A Rectangular Beam That Must Carry a Service Live Load of 2.47 kips/ft and a calculated dead load of 1.05 kips/ft (with out self weight) on an 18-ft simple span is limited to 10 inches width and 20 inches total depth for architectural reason if  $f_y = 6000 \text{ psi}$  and  $f'_c = 4000 \text{ psi}$  what steel area must be provided? Draw sketch of your final design.

Given Data :-

Beam live load (L.L) = 2.47 kips/ft

Beam Dead load (D.L) = 1.05 kips/ft

span of Beam = 18-ft

width of the Beam = 10"

depth of the Beam = 20"

$f_y = 6000 \text{ psi} = 60 \text{ ksi}$

$f'_c = 4000 \text{ psi} = 4 \text{ ksi}$

Solution :-

Step # 01

Calculate effective depth (d)

$$h - 3 = 20 - 3 = 17''$$

Step # 02

Calculate effective cover (d')

$$\text{Assume } d' = 2.5''$$

Step # 03

Reinforcement Ratio

$$\rho_{max} = 0.85 \times \beta \times \frac{f_c'}{f_y} \times \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$\rho_{max} = 0.85 \times 0.85 \times \frac{4}{60} \times \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$\rho_{max} = 0.0180625$$

Step # 04

Calculate Area of steel :-

As we know that

$$\rho_{max} = \frac{A_{st}}{b \times d}$$

$$A_{st} = \rho_{max} \times b \times d$$

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$$\Rightarrow A_{st} = \rho_{max} \times (b \times d)$$

$$A_{st} = 0.0180625 \times 10 \times 17$$

$$A_{st} = 3.070625 \text{ in}^2$$

Step #05

By Formula of Design Moment

$$M_{u2} = \phi \times A_{st} \times f_y \times (d - \frac{a}{2})$$

First we find the value of a

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b}$$

$$a = \frac{3.07 \times 60}{0.85 \times 4 \times 10} = 5.42''$$

$$M_{u2} = 0.90 \times 3.07 \times 60 \times (17 - \frac{5.42}{2})$$

$$M_{u2} = 2368.99 \text{ kips-inch}$$

Moment Due to given Load:-

$$\text{Beam self weight} = b \times t \times \gamma_c$$

$$= \frac{10}{12} \times \frac{20}{12} \times 150$$

$$= 208.33 \text{ lb/ft}^3$$

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Total Factored Load:-

$$\begin{aligned}W_T &= 1.2 D.L + 1.6 L.L \\ &= 1.2 (1050 + 208.33) + 1.6 (2470) \\ &= 5461.99 \text{ lb/ft} \\ &= 5.46 \text{ kips/ft}\end{aligned}$$

Step #06

Ultimate Factored Moment:-

$$\begin{aligned}M_u &= \frac{W \times L^2}{8} \times 12 \\ &= \frac{5.46 \times 18^2}{8} \times 12\end{aligned}$$

$$M_u = 2653.56$$

As we have

$$M_u > M_{ug}$$

$$2653.56 > 2368.99$$

⇒ Design of a section is  
Doubly Reinforcement

Step #07

To Find  $M_{u1}$ :-

$$M_{u1} = M_u - M_{ug}$$

$$M_{u1} = 2653.56 - 2368.99$$

$$M_{u1} = 284.57 \text{ kip-inch}$$

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Step # 08

As we know that

$$M_{u1} = \phi \times A_s' \times f_y \times (d - d')$$

$$A_s' = \frac{M_{u1}}{\phi \times f_y \times (d - d')}$$

$$A_s' = \frac{284.57}{0.90 \times 60 \times (17 - 2.5)}$$

$$A_s' = 0.36 \text{ in}^2$$

This is the steel area in  
compression zone

Total Steel Area =

$$A_{st} = A_{st} + A_s' = 3.07 + 0.36$$

$$A_s = 3.43 \text{ in}^2$$

Step # 09

Selection of Bars:-

(A) For Tensile steel:-

let try #8 bars having

$$A_{sb} = 0.785 \text{ in}^2$$

$$\Rightarrow \text{Number of Bars} = \frac{A_s}{A_b} = \frac{3.43}{0.785}$$

$$= 4.369 \approx 5 \text{ bars}$$

So ~~5 bars~~ #8 bars

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(B) For compression steel:-

Let try #6 bars having  
Area =  $0.44 \text{ in}^2$

$$\text{Number of Bar} = \frac{A'_s}{A_b} = \frac{0.36}{0.44}$$

$$= 0.81 \approx 1 \text{ bars}$$

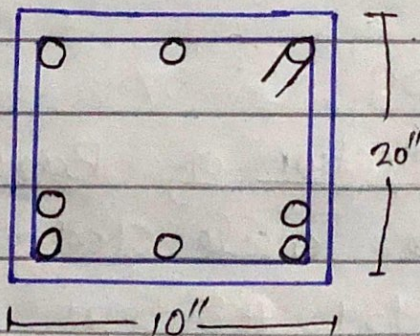
So 1 #6 Bar in compression  
Zone.

Step#09

Check on Minimum width  
of Beam:-

$$b_{\min} = 2(1.5) + 2\left(\frac{3}{8}\right) + 5\left(\frac{8}{8}\right) + 4\left(\frac{8}{8}\right)$$
$$= 19.75 > 10"$$

$\Rightarrow$  Not good in one layer



$$\Rightarrow \text{Effective depth } (d) = 20 - 1.5 - \frac{3}{8} - \frac{8}{8} - \frac{1}{2}\left(\frac{8}{8}\right)$$
$$d = 16.62"$$

$$\Rightarrow \text{Effective cover } (d') = 1.5 + \frac{3}{8} + \frac{1}{2}\left(\frac{8}{8}\right)$$
$$d' = 2.25"$$

Step #10

Design Moments

$$M_d = \phi \times [A_s' \times f_{y_s} (d - d') + (A_{st} - A_s') \times f_y \times (d - \frac{a}{2})]$$

As we know that

$$a = \frac{(A_{st} - A_s') \times f_y}{0.85 \times f_c' \times b}$$

$$a = \frac{(5 \times 0.785 - 1 \times 0.44) \times 60}{0.85 \times 4 \times 10} = 6.15$$

$$M_d = 0.90 \left[ (1 \times 0.44) \times 60 \times (16.62 - 2.25) + (5 \times 0.785 - 1 \times 0.44) \times 60 \times \left( 16.62 - \frac{6.15}{2} \right) \right]$$

$$M_d = 2890.46$$

$$\text{As } M_d = 2890.46 \text{ } 72653.56 \text{ K}''$$

So the Design is OK



QNO02  
(a) Briefly describe bond stress and development length.

### Bond stress:-

The stress which is acting on the outer interface of steel to the surrounding concrete is called bond stress.

=> The resulting stress of bond is called bond stress.

=> This stress helps in keeping bond between reinforcement and concrete together.

=> Bond stress resists any force that tries to pull out the rods from the concrete.

=> When you try to pull out the reinforcement bar from hardened concrete, then bond stress resists the bar to come out.

### Development length:-

The necessary length between the point of max stress in a bar and the end of a bar is called.

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Development length OR

⇒ The length of bar required to transfer the force in the bar to surrounding concrete through bond is called development length.

### Reason For Providing Development length

→ To develop a safe bond between the bar surface and concrete so that no failure due to slippage of bar occurs during the ultimate loading condition.

→ Also the extra length of the bar provided as development length is responsible for transferring the stresses development in any section of the adjoining section.

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Q No 2

(b)

In which condition doubly reinforced beam can be used  
 We can use the doubly reinforced beam on that condition when the restriction occurs in the size of beam.

⇒ For example if someone said that the depth of beam should not be greater than 12" and the external load on beam is very much which can not resist a beam of singly reinforcement in that condition we used Doubly Reinforced Beam.

Q No 2

(c)

Differentiate between T-Beam analysis and Rectangular Beam Analysis.

T-Beam	Rectangular Beam
→ In case of T-Beam slab and beam are connected with one another.	→ In case of Rectangular Beam slab has been placed on the

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and act as a  
one member

beam so there  
is no connection

→ In T Beam  
the →

blw slab and  
beam

⇒ T Beam are mostly  
Used and heavy duty  
and large space such  
is bridge.

→ Rectangular Beam  
are mostly use in  
commercial building

→ T Beam are more  
economical than R-Beam

→ Rectangular Beam  
are less economical  
than T-Beam

Q No 2 write short Note on the effect  
(d) of strength reduction factor on  
flexural strength.

In the design of flexural strength  
the strength reduction factor decrease  
from tension control section  
to compression. Controlled section  
to increase safety with decreasing  
ductility. This show to determine  
the reduction factor for flexural  
strength of reinforcement concrete.

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- Q No 2 Briefly describe design Methods  
 (e) Which one of them can be best used for design of different structure members and why?

### Designing Methods =

Two Methods are worldily used for the designing of concrete and different structure members.

- 1) ASD Method
- 2) Usp Method

1) => ASD Method :-

ASD method is also know as working stress design method. it is based on the principle that stresses developed in the structural member should not exceed a certain limit fraction of elastic limit.

=> In this method all load are taken as service load and no factor is

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is applied to increase these service load.

2) => USD Method

-> Ultimate strength design method is also called as load factor method.

-> for the structure subjected to large external load the ultimate strength is determined by the inelastic analysis.

=> USD method is best for designing different structural method because of the following reason.

1) As the ultimate strength of the material is considered we will get much slender section for column and beam compare to other method.

2) USD method result is more economical design for a building with fewer special need for customized area and requirement.

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Q NO 03

A concrete floor system consist of parallel T beam spaced 10 ft. on centers and spanning 32 ft between support. The 6 inch thick slab is cast monolithically with beam web having width  $b_w = 14$  inch and total depth measured from the top of the slab of  $h = 28$  inch. The effective depth will taken 3 inch less than the total depth. In addition to its own weight, each beam must carry a superimposed D.L of 50 psf and service live load of 225 psf. Material strength are  $f_y = 60000$  psi and  $f'_c = 4000$  psi. Determine the required tensile steel area and selected the reinforcement needed for a typical member, Draw sketch of final design.

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Given data:-

Clear distance = 10'

Length = 33'

Thickness of slab ( $h_f$ ) = 6"

Beam web width ( $b_w$ ) = 14"

Total depth ( $h$ ) = 28"

Effective depth =  $28" - 3" = 25"$

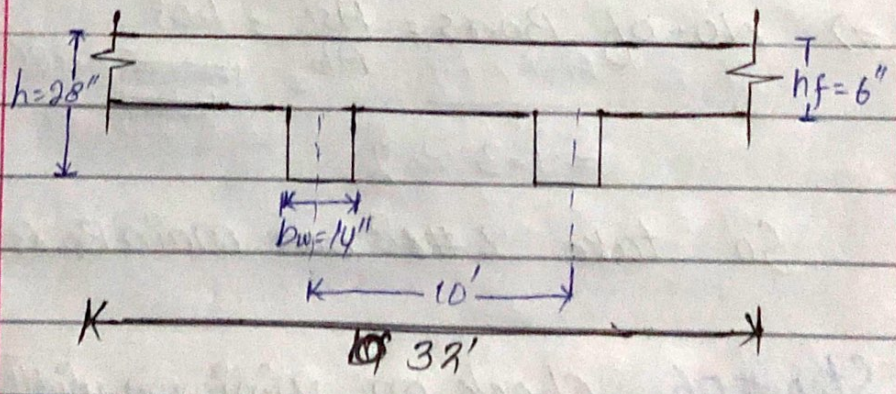
Dead load ~~of beam~~ = 50 lb/ft<sup>2</sup>

Live Load (L.L) = 225 lb/ft<sup>2</sup>

$f_y = 60000 \text{ psi} = 60 \text{ ksi}$

$f'_c = 4000 \text{ psi} = 4 \text{ ksi}$

Solution:-



Step #01 Ultimate Factored Moment

$$M_u = \frac{W_u \times l^2}{8} =$$

$W_u = \text{Total Factored Load.}$



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Find self weight per feet:-

$$\begin{aligned}
 W_t &= b \times t \times \gamma_c \\
 &= \frac{14}{12} \times \frac{28}{12} \times 150 \\
 &= 408.33 \text{ lb/ft}
 \end{aligned}$$

Find Total Factored Load

$$\begin{aligned}
 W_u &= 1.2 \text{ D.L} + 1.6 \text{ D.L} \\
 W_u &= 1.2(50 + 408.33) + 1.6(225) \\
 W_u &= 909.96 \text{ lb/ft} \\
 W_u &= 0.909 \text{ kips/ft}
 \end{aligned}$$

Now Moments:-

$$\begin{aligned}
 M_u &= \frac{W_u \times l^2}{8} \\
 &= \frac{0.909 \times (32)^2 \times 12}{8}
 \end{aligned}$$

$$M_u = 1396.22 \text{ kips-inch}$$

Step#02 Calculate effective width "be"

- 1)  $16 \times h_f + b_w = 16 \times 6 + 14 = 110''$
- 2) c/c distance =  $10 \times 12 = 120''$
- 3)  $s_pom/4 = \frac{32}{4} \times 12 = 96''$
- 4) So  $be = 96''$

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Step # 03 Check whether Rectangular or I-beam:-

Trial # 01:-

$$\text{Let } a = hf = 6$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{1396.23}{0.90 \times 60 \times (25 - \frac{6}{2})}$$

$$A_{st} = 1.175 \text{ in}^2$$

Trial # 02:-

$$a = \frac{A_s \times f_y}{0.85 \times f_c' \times b_e}$$

$$a = \frac{1.175 \times 60}{0.85 \times 4 \times 96}$$

$$a = 0.21" < 6"$$

⇒ So Rectangular Beam Design

$$A_s = \frac{1396.23}{0.90 \times 60 \times (25 - \frac{0.21}{2})}$$

$$\Rightarrow \boxed{A_{st} = 1.03 \text{ in}^2}$$

Trial # 03:-

$$a = \frac{A_s \times f_y}{0.85 \times f_c' \times b_e}$$

$$a = \frac{1.03 \times 60}{0.85 \times 4 \times 96} = 0.18"$$

$$A_{st} = \frac{1396.23}{0.90 \times 60 \left( 25 - \frac{0.18}{2} \right)}$$

$$\Rightarrow A_{st} = 1.03 \text{ in}^2$$

Step #04 Check  $\rho_{max}$  and  $\rho_{min}$ :

$$\rho_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_t} \right)$$

$$\rho_{max} = 0.85 \times 0.85 \times \frac{4}{60} \times \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$\Rightarrow \rho_{max} = 0.018$$

$$\Rightarrow \rho_{min} = \frac{200}{f_y} = \frac{200}{60000} = 0.003$$

$$\Rightarrow \rho = \frac{A_{st}}{b \times d} = \frac{1.03}{14 \times 25} =$$

$$\Rightarrow \rho = 0.00294$$

$$\rho_{max} < \rho <$$

$$\rho_{min} < \rho < \rho_{max}$$

$$0.003 < 0.00294 < 0.018$$

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As we know that

 $\rho$  is less than  $\rho_{min}$ 

So

$$\rho = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = \rho \times b \times d$$

$$A_{st} = 0.003 \times 14 \times 25 = 1.05 \text{ in}^2$$

Step #05 Selection and No. of Bars

Let try #8 main bars

having area of one # 10 bar  
=  $1.27 \text{ in}^2$ 

$$\Rightarrow \text{NO. of Bars} = \frac{A_{st}}{A_b} = \frac{1.05}{\cancel{0.785} \times 1.27} = 1.3 \approx 2$$

So take 2 #8 main bars

Step #06 Check on minimum width

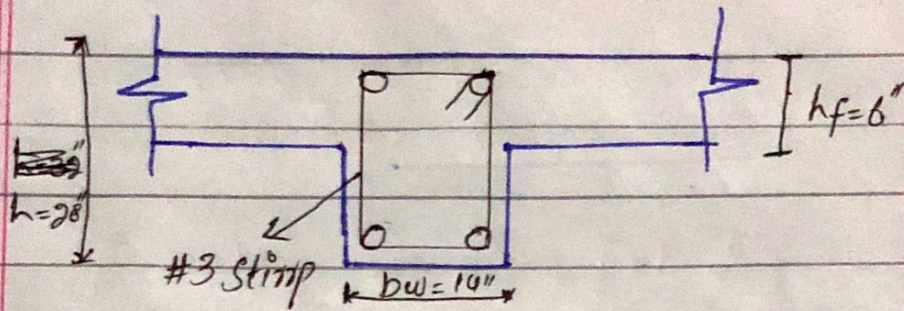
$$b_{min} = 2 \times 1.5 + 2 \times \left(\frac{3}{8}\right) + 2 \left(\frac{1}{8}\right) + \left(\frac{1}{8}\right)$$

$$b_{min} = 6.75" < 14"$$

$\Rightarrow$  so good in one layer.

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### Step #07 Design Moment

$$M_d = \phi \times f_y \times A_{st} \times \left(d - \frac{a}{2}\right)$$

But first find "A<sub>st</sub>" & "a"

A<sub>st</sub> = Area of one bar x NO of bars

$$A_{st} = \cancel{1.27} 0.785 \times 2 = 1.57 \text{ in}^2$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f_c \times b_e} = \frac{1.57 \times 60}{0.85 \times 4 \times 96}$$

$$a = 0.2 \text{ inches}$$

$$M_d = 0.90 \times 60 \times 1.57 \times \left(25 - \frac{0.2}{2}\right)$$

$$M_d = 2111.02 \text{ Kips-in}$$

~~M<sub>d</sub>~~

$$M_d = 2111.02 \text{ K}'' > M_u = 1396.23 \text{ K}''$$

the design is OK ✓