

Name : M. Shawal Khan

Id 7813

Section A

Semester 6th

Assignment Hydraulic Engineering

Submitted to : Sir Fawad

Q1. What is venturi flume? Explain with detail.

Venturi Flume:-

A venturi flume is a critical flow open flume with a constricted flow which causes a drop in hydraulic grade line, creating a critical depth.

It is used in flow measurement of very large flow rates, usually gives in millions of cubic units.

A venturi meter would normally measure in millimeters. Whereas a venturi flume measures in meters.

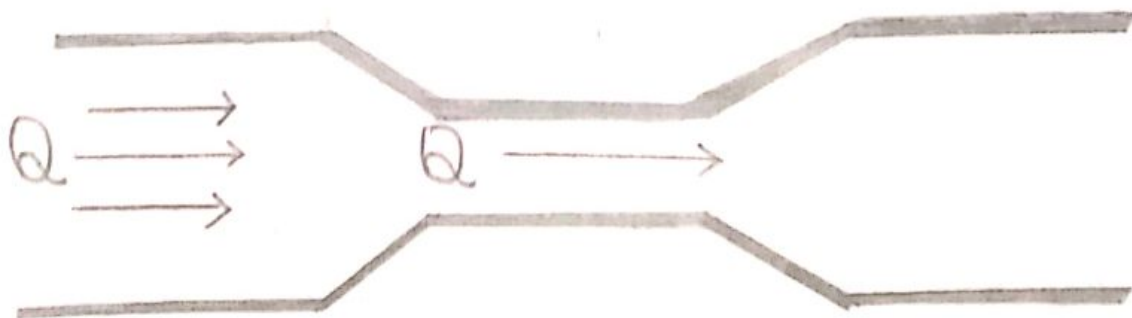
Measurement of discharge with venturi flume requires two measurements, one upstream and one at a throat.

If flow passes in a sub-critical state through flume.

If flume are designed so as to pass flow from sub-critical to super-critical state while passing through flume a single measurement at throat is sufficient for computation of discharge.

To ensure occurrence of critical depth at throat flumes are usually designed in such a way to form a hydraulic jump on downstream side of structure.

These flumes are called "standing wave flumes". It causes drop in hydraulic gradeline.



Flow through a venturi Flume

Q2

A 3m wide channel carries a total discharge of $12 \text{ m}^3/\text{sec}$

Calculate

- Critical Depth
- Minimum Specific energy.
- Alternative depths when $E = 4 \text{ m}$.

Given Data:-

Width of channel (b) = 3m

Discharge $Q = 12 \text{ m}^3/\text{sec}$.

Required:-

- Critical depth
- Minimum Specific Energy.
- Alternative depth when $E = 4 \text{ m}$.

Sol:-

Critical Depth

$$\text{As } q = Q/b$$

$$\frac{12}{3} = q$$

$$q = 4 \text{ m}^2/\text{sec}$$

Using formula.

$$y_c = \left(\frac{q^2}{g} \right)^{1/3}$$

$$= \left(\frac{4^2}{9.81} \right)^{1/3} = 1.177 \text{ m}.$$

The Minimum Specific energy (For rectangular channel).

$$Q = AV \rightarrow \text{eq 1}$$

and

$$Q = qb \rightarrow 2$$

Equating eq 1 & 2

$$Q = Q$$

$$AV = qb$$

$$\text{by } v = qb$$

$$vy = q$$

$$v = q/y_c$$

$$v = \frac{4}{1.177} = 3.398 \text{ m/sec}$$

$$E_{\min} = y + \frac{v^2}{2g}$$

$$= 1.177 + \frac{(3.398)^2}{2(9.81)}$$

$$E_{\min} = 1.76 \text{ m.}$$

The alternate depth when $E = 4 \text{ m.}$

As $E > E_c$, there are two possible depths for a given specific energy.

$$E = h + \frac{v^2}{2g} \quad \text{where} \quad v = \frac{Q}{A} = \frac{q}{h} \quad (\text{for rectangular channel})$$

$$E = h + \frac{q^2}{2gh^2}$$

Substituting values in meter-second units

$$4 = h + 0.8155 / h^2$$

Assignment 1

Pg 4

For the sub-critical (slow, deep) solution, the first term associated with potential energy dominates, so rearrange as

$$h = 4 - \frac{0.8155}{h^2}$$

Iteration from $h=4$ gives $h=3.948\text{m}$.

From the sub-critical (fast, shallow) solution, the second term associated with kinetic energy dominates so rearrange as.

$$h = \sqrt{\frac{0.8155}{4-h}}$$

Iteration from $h=0$ gives $h=0.4814\text{m}$

Answer:- Alternate depth are 3.95 and 0.481m

Problem 1

Water flows at depth of 10cm with velocity of 6m/s in rectangular channel. Is flow critical or subcritical? What is its alternate depth?

Given Data:-

$$\text{Depth} = 10\text{cm}$$

$$\text{Velocity} = 6\text{m/s}$$

Required:-

Type of flow

Alternate depth.

Sol:-

First we have to check Froude Number.

$$\begin{aligned} Fr &= \frac{V}{\sqrt{gy}} = \frac{6\text{m/s}}{\sqrt{9.81\text{m/s}^2 \times 0.1}} \\ &= 6.06 > 1 \end{aligned}$$

So flow is supercritical.

Alternate Depth:-

$$\begin{aligned} E &= y + \frac{V^2}{2g} \quad \text{As we know} \\ &= 0.1 + \frac{6^2}{2 \times 9.81} = 1.935\text{m} \end{aligned}$$

The alternate depth for $E = 1.935\text{m}$ yields

$$y_{\text{alt}} = 1.93\text{m}$$

Giving $y_2 = 3.17$ and $\Delta y = y_2 - y_1 = 0.17\text{m}$ so water surface rises 0.02m .

The maximum upstep possible before affecting upstream water surface level is for,

$$y_2 = y_c$$

$$y_c = \sqrt[3]{\frac{q^2}{g}}$$

$$y_c = \sqrt[3]{\frac{6^2}{9.18}}$$

$$y_c = 1.54\text{m}$$

Problem:-

A water passing from slice gate in Dam.

..... 3.9m.

Determine:-

a. Discharge

b. Froude number Upstream & Downstream.

Given Data:-

Depth at upstream side $y_1 = 3.6m$.

Depth at downstream side (y_2) $0.9m$

Width of slice gate $b = 3.9m$.

Required:-

Discharge

Froude number Upstream & downstream.

Sol:-

As we know

$$E_1 = E_2$$

$$y_1 + \frac{V_1^2}{2g} = y_2 + \frac{V_2^2}{2g} \rightarrow \text{eq 1.}$$

Also

$$Q = A_1 V_1 = A_2 V_2$$

$$b_1 y_1 V_1 = b_2 y_2 V_2$$

$$y_1 V_1 = y_2 V_2$$

$$V_2 = \frac{y_1}{y_2} \times V_1$$

$$V_2 = \frac{3.6}{0.9} \times V_1$$

$$V_2 = 4V_1 \rightarrow \text{eq 2}$$

Put in eq 1

$$y_1 + \frac{V_1^2}{2g} = y_2 + \frac{V_2^2}{2g}$$

$$3.6 + \frac{V_1^2}{2g} = 0.9 + \frac{(4V_1)^2}{2g}$$

$$3.6 + \frac{V_1^2}{2g} = 0.9 + \frac{16V_1^2}{2g}$$

$$\frac{V_1^2}{2g} - \frac{16V_1^2}{2g} = 0.9 - 3.6$$

$$\frac{V_1^2 - 16V_1^2}{2g} = -2.7$$

$$\frac{-15V_1^2}{2g} = -2.7$$

$$\sqrt{V_1^2} = \sqrt{\frac{2.7 \times 2(9.81)}{15}}$$

$$V_1 = 1.879 \text{ m/sec}$$

Put value of "V₁" in eq 2

$$V_2 = 4V_1$$

$$V_2 = 4(1.879) = 7.516 \text{ m/sec.}$$

As

$$Q = A_1 V_1 = by_1 V_1$$

$$= 3.9 \times 3.6 \times 1.879 = 26.38 \text{ m}^3/\text{sec.}$$

$$Q_2 = A_2 V_2 = by_2 V_2$$

$$= 3.9 \times 0.9 \times 7.516 = 26.38 \text{ m}^3/\text{sec}$$

$$Q = Q_1 = Q_2 = 26.38 \text{ m}^3/\text{sec.}$$

1) Froude Number at upstream side:-

$$Fr_1 = \frac{V_1}{\sqrt{g y_1}} = \frac{1.879}{\sqrt{9.81 \times 3.6}} = 0.31 \text{ (Sub-critical flow)}$$

2) Froude number at downstream side:-

$$Fr_2 = \frac{V_2}{\sqrt{g y_2}} = \frac{7.516}{\sqrt{9.81 \times 0.9}} = 2.52 \text{ (Super Critical flow)}$$
