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Section :- B

Subject :- Structural Analysis - II

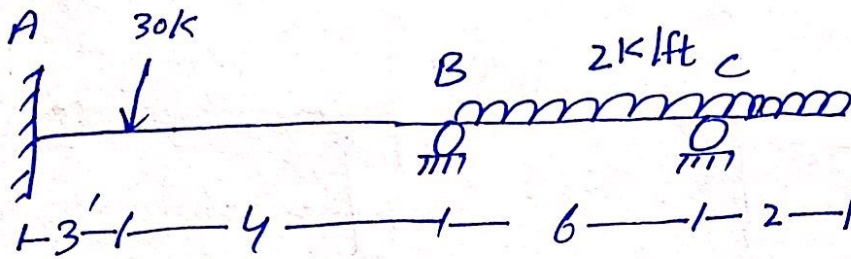
Sir :- Engr. Adeed Khan

Date :- 25/09/2020

# Problem # 01

7839

①

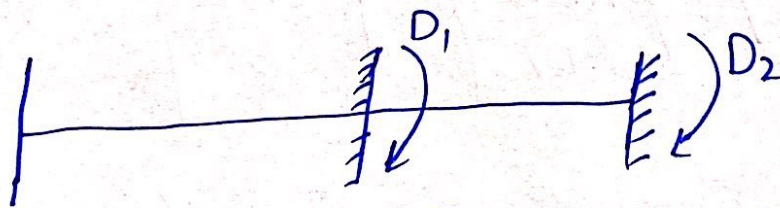
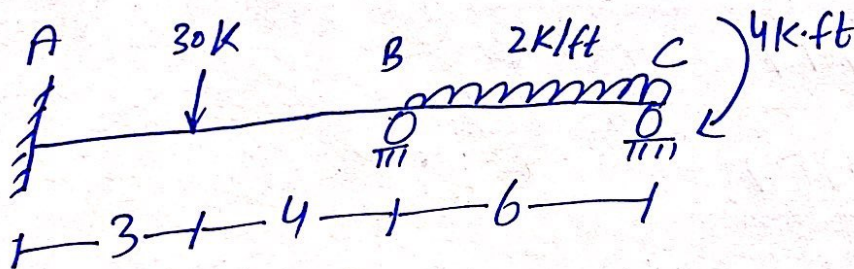


Step # 01: -

$K \cdot I = 2^6$  (Neglecting Axial Effects)

Step # 02: -

Select the unknown joint displacement.

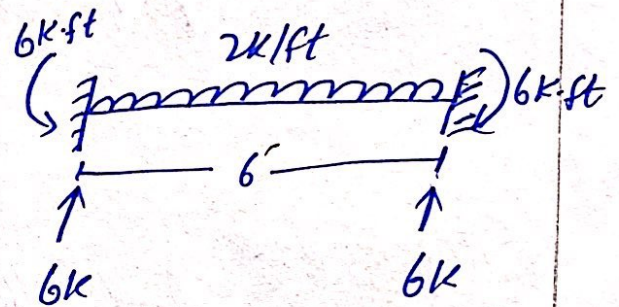
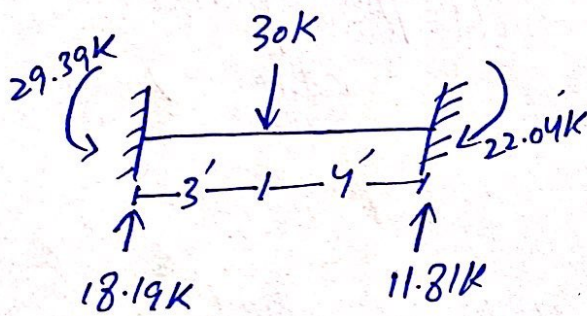
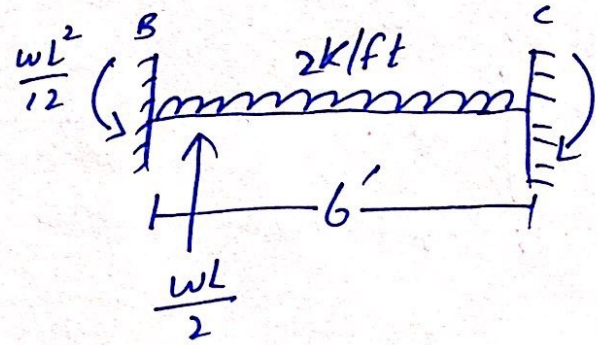
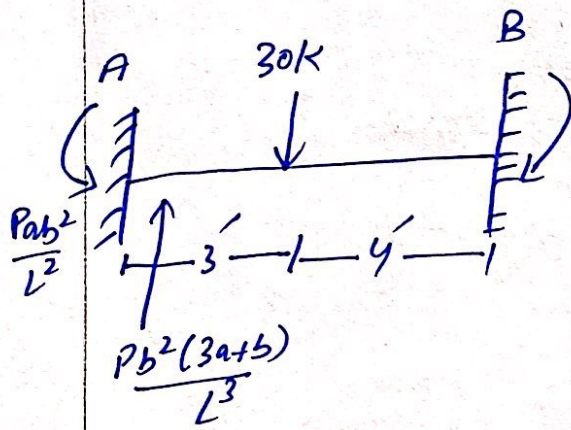


$$[D] = \begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, [AD] = \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

Step # 03:- Compute [ADL] matrix

7839

(2)



$$ADL_1 = 22.04'K - 6'K$$

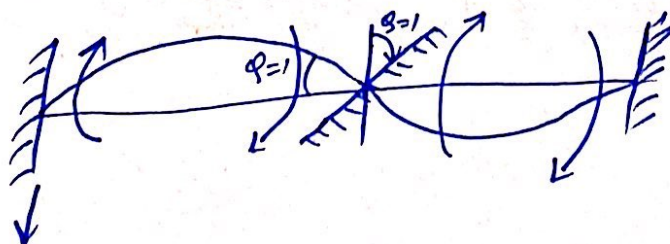
$$ADL_1 = 16.04'K$$

$$ADL_2 = 6'K$$

$$\text{So } [ADL] = \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix} = \begin{bmatrix} 16.04 \\ 6 \end{bmatrix}$$

Step # 04:- Compute [S] matrix

(i)

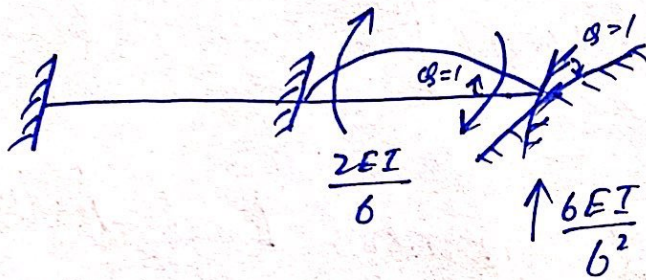


When  $D_1 = 1$ ,  $D_2 = 0$

$$S_{11} = \frac{4EI}{7} + \frac{4EI}{6} = 1.238 EI$$

$$S_{21} = \frac{2EI}{6} = 0.333 EI$$

ii) when  $D_1 = 0$ ,  $D_2 = 1$



$$S_{12} = \frac{2EI}{6} = 0.333 EI$$

$$S_{22} = \frac{4EI}{6} = 0.667 EI$$

Stiffness Matrix  $[S] = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$

$$[S] = \begin{bmatrix} 1.238 & 0.333 \\ 0.333 & 0.667 \end{bmatrix} EI$$

Step # 05:- Compute the value of  $D_1$  and  $D_2$

$$[AD] = [ADL] + [S][D]$$

$$[D] = [s]^{-1} [AD - ADL]$$

7839

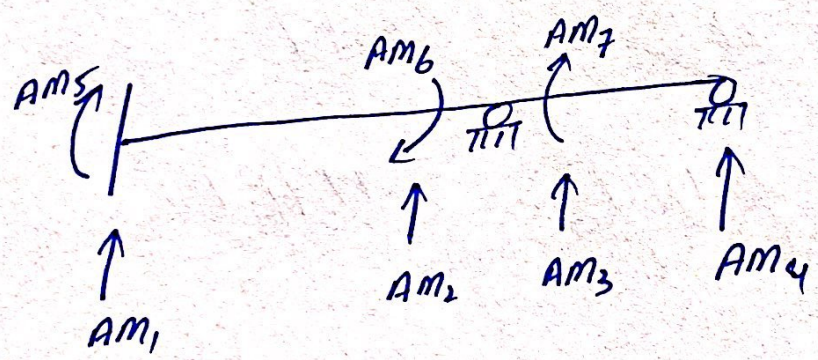
(4)

$$[D] = \left( \begin{bmatrix} 1.238 & 0.333 \\ 0.333 & 0.667 \end{bmatrix} EI \right)^{-1} \begin{bmatrix} 0 & -(16.04) \\ 4 & -(6) \end{bmatrix}$$

$$= \frac{1}{EI} \begin{bmatrix} 0.933 & -0.466 \\ -0.466 & 1.732 \end{bmatrix} \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

$$[D] = \frac{1}{EI} \begin{bmatrix} -14.03 \\ 4.01 \end{bmatrix}$$

Step#ob:- Compute member End Actions



$$[AM] = [AML] + [AMD][D]$$

$$[AML]; [AML] = \begin{bmatrix} AML_1 \\ AML_2 \\ AML_3 \\ AML_4 \\ AML_5 \\ AML_6 \\ AML_7 \end{bmatrix} = \begin{bmatrix} 18.19K \\ 11.81K \\ 6K \\ 6K \\ -29.39K \\ 22.04K \\ -6K \end{bmatrix}$$

[AMD];

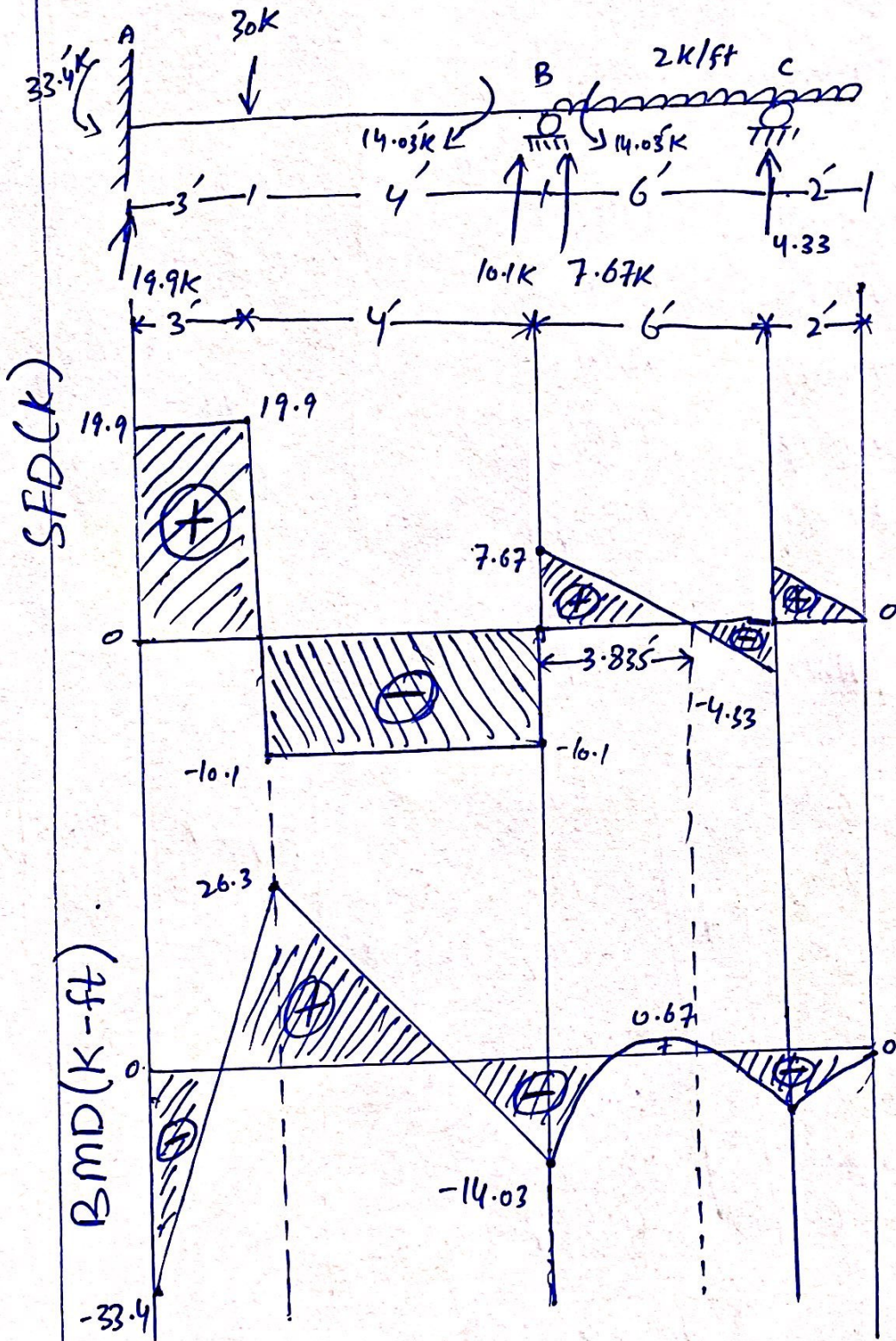
7839 (5)

$$[AMD] = \begin{bmatrix} AMD_{11} & AMD_{12} \\ AMD_{21} & AMD_{22} \\ AMD_{31} & AMD_{32} \\ AMD_{41} & AMD_{42} \\ AMD_{51} & AMD_{52} \\ AMD_{61} & AMD_{62} \\ AMD_{71} & AMD_{72} \end{bmatrix} = EI \begin{bmatrix} -0.122 & 0 \\ 0.122 & 0 \\ -0.167 & -0.167 \\ 0.167 & 0.167 \\ 0.286 & 0 \\ 0.571 & 0 \\ 0.667 & 0.333 \end{bmatrix}$$

Now,  $[Am] = [AML] + [AMD][D]$

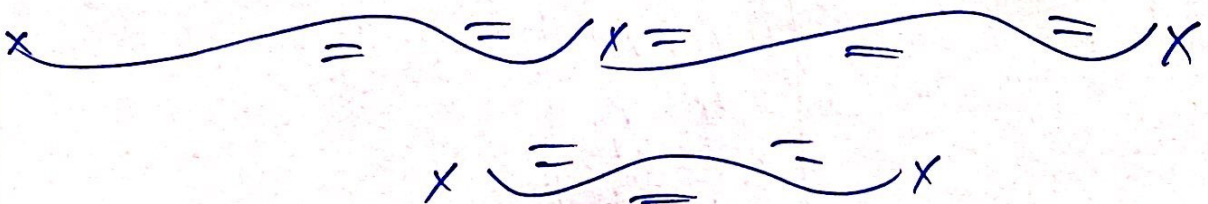
$$[Am] = \begin{bmatrix} 18.19 \\ 11.19 \\ 6 \\ 6 \\ -29.39 \\ 22.04 \\ -6 \end{bmatrix} + \begin{bmatrix} -0.122 & 0 \\ 0.122 & 0 \\ -0.167 & -0.167 \\ 0.167 & 0.167 \\ 0.286 & 0 \\ 0.571 & 0 \\ 0.667 & 0.333 \end{bmatrix} \cdot \frac{1}{EI} \begin{bmatrix} -14.03 \\ 4.01 \end{bmatrix}$$

$$[Am] = \begin{bmatrix} 19.9K \\ 10.1K \\ 7.67K \\ 4.33K \\ -33.4K \\ 14.03K \\ -14.03K \end{bmatrix}$$



SFD(k)

BMD(k-ft)

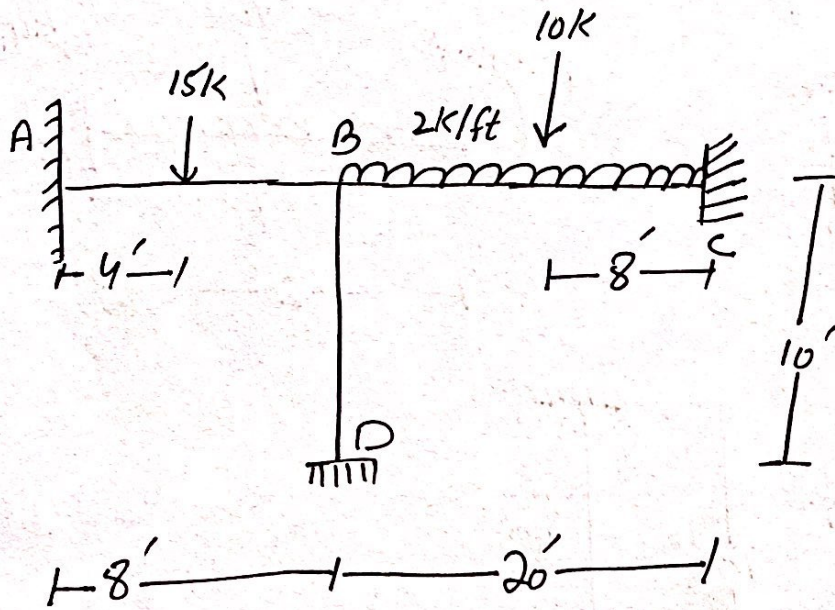


# Problem # 02

7839

(6)

(7)



Solution:-

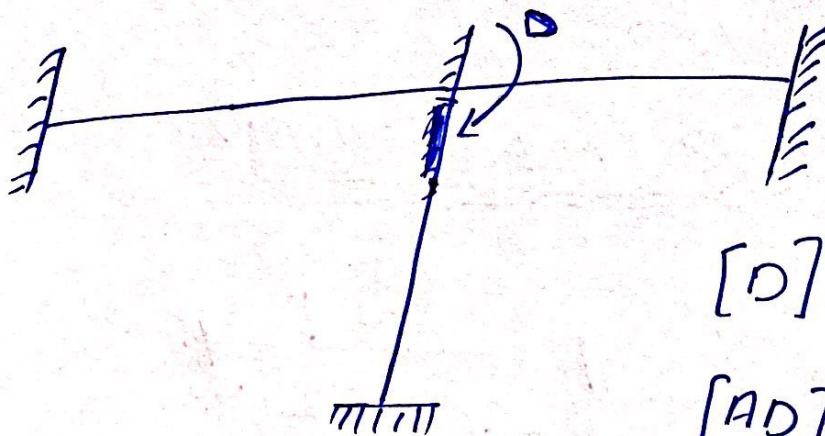
Step # 01:-

Determine Kinematic Indeterminacy

$$K.I = 1$$

Step # 2:-

Determine unknown Joint Displacement



$$[D] = [?]$$

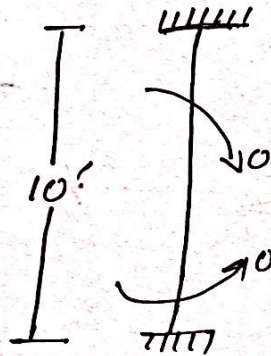
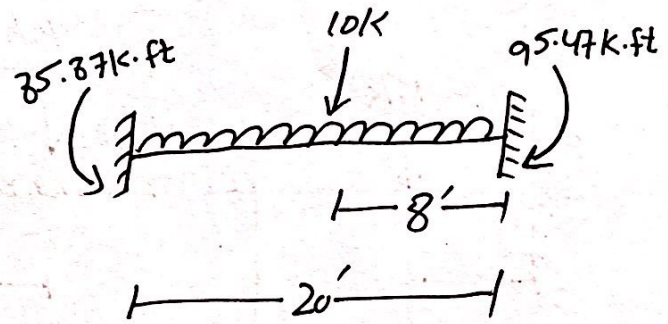
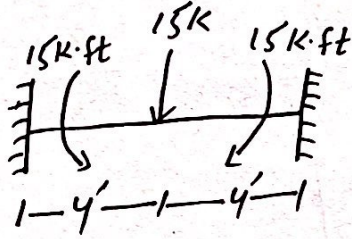
$$[AD] = [0]$$



Step # 03:-

7839

Compute [ADL] Matrix



⇒ Point load at Center:-

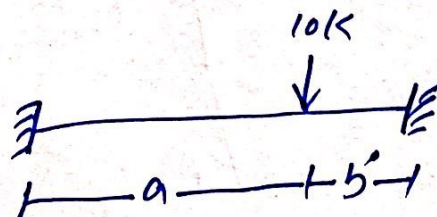
$$\frac{PL}{8} = \frac{(15)(8)}{8} = 15 \text{ kip.ft}$$

⇒ Uniformly Distributed Load:-

$$\frac{wL^2}{12} = \frac{(2)(20)^2}{12} = 66.67 \text{ K.ft}$$

⇒ Point Load (Not at Mid):-

Suppose:-



For Left End:-

7839



(9)

$$\frac{Pab^2}{L^2} = \frac{(10)(12)(8)^2}{(20)^2} = 19.2 \text{ k}\cdot\text{ft}$$

For Right End:-

$$\frac{Pa^2b}{L^2} = \frac{(10)(12)^2(8)}{(20)^2} = 28.8 \text{ k}\cdot\text{ft}$$

So Total moment at Left End:-

$$19.2 + 66.67 = 85.87 \text{ k}\cdot\text{ft}$$

Similarly at right End:-

$$28.8 + 66.67 = 95.47 \text{ k}\cdot\text{ft}$$

$$\text{So } [ADL] = -85.87 + 15 = -70.87 \text{ k}\cdot\text{ft}$$

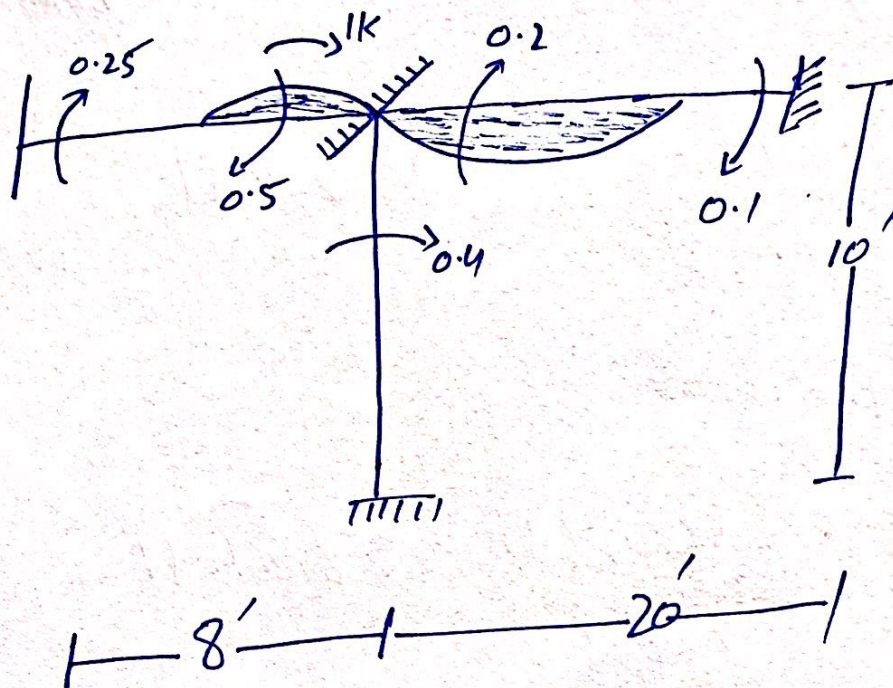
Step #04:-

Determine  $[S]$  matrix

$$[S] = [s_{ij}]$$

Now

$$D = 1K$$



$$\Rightarrow \frac{4EI}{8} = 0.5$$

$$\frac{2EI}{8} = 0.25$$

$$\Rightarrow \frac{4EI}{20} = 0.2$$

$$\frac{2EI}{20} = 0.1$$

$$\Rightarrow \frac{4EI}{10} = 0.4$$

$$\frac{2EI}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2)EI$$

$$[S] = 1.1EI$$

Step #05 :-

7839

(11)

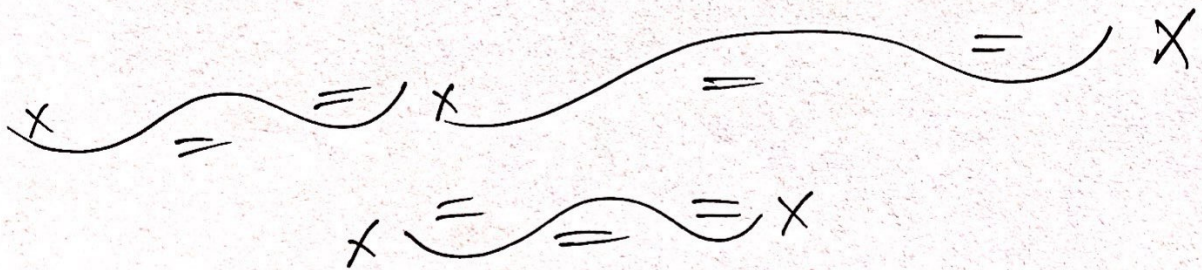
Compute  $[D]$  matrix

$$[D] = [S]^{-1} \times [AD] - [ADL]$$

$$[D] = \frac{1}{1.1} \times [0] - [-70.87]$$

$$= \frac{70.87}{1.1}$$

$$[D] = [64.42] \text{ 'EI}$$

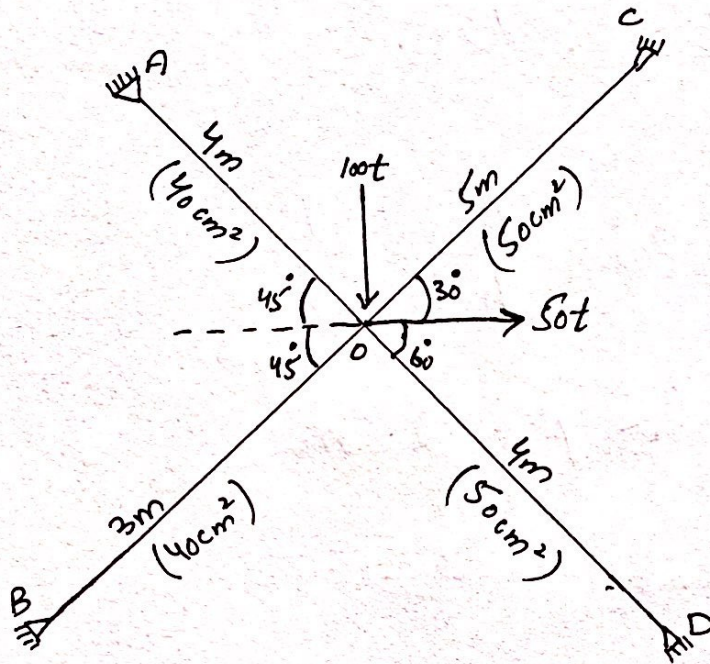


# Problem # 03

7839

(11)

(12)



$$E = 2000t/cm^3$$

Solution:-

For A:-

$$\sin 45^\circ = \frac{P}{h} = \frac{P}{4}$$

$$\Rightarrow P = 2.828m$$

$$\cos 45^\circ = \frac{b}{4}$$

$$\Rightarrow b = 2.828m$$

For B:-

$$\sin 45^\circ = \frac{P}{3}$$

$$\Rightarrow P = 2.12m$$

$$\cos 45^\circ = \frac{b}{h}$$

7839 (12)

$$\Rightarrow b = 2.12 \text{ m}$$

For C:-

$$\sin 30^\circ = \frac{P}{h} = \frac{P}{5}$$

$$\Rightarrow P = 2.5 \text{ m}$$

$$\cos 30^\circ = \frac{b}{5}$$

$$\Rightarrow b = 4.33 \text{ m}$$

Now:-

$$EA(A) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(B) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(C) = 2000 \times 50 = 100,000 \text{ t}$$

$$EA(D) = 2000 \times 50 = 100,000 \text{ t}$$

Step # 01:-

K.I

$$K.I = 2I - \gamma$$

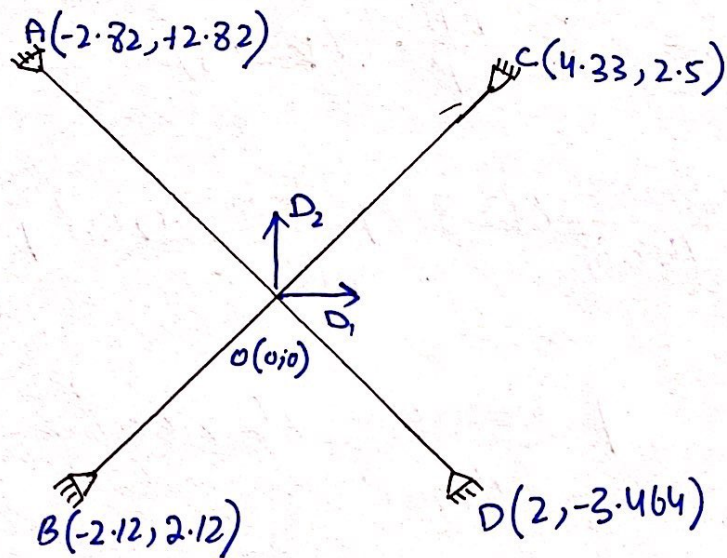
$$K.I = 2(5) - 8$$

$$K.I = 2^\circ$$

Step # 02 :-

7839

Select unknown Joint displacement



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

Step # 03 :-  $[AMD]_{4 \times 2}$  and  $[S]_{2 \times 2}$

i)  $D_1 = 1, D_2 = 0$

$$AMD = \frac{EA}{l^2} (x_k - x_j)$$

$$AMD_{11} = \frac{80,000}{(400)^2} \times (0 + 282) = 141$$

$$AMD_{21} = \frac{80,000}{(300)^2} \times (0 + 212) = 188.44$$

$$AMD_{31} = \frac{100,000}{(500)^2} \times (0 - 433) = -173.2$$

$$AMD_{41} = \frac{100,000}{(400)^2} \times (0-200) = -125$$

7839

(14)

(15)

$$\text{Now } S_{11} = \sum_{i=1}^m \frac{EA}{L^3} (x_k - x_j)^2$$

$$= \frac{80,000}{(400)^3} \times (282)^2 + \frac{80,000}{(300)^3} \times (212)^2 + \frac{100,000}{(500)^3} \times (-433)^2$$

$$+ \frac{100,000}{(400)^3} \times (-200)^2$$

$$S_{11} = 99.405 + 133.167 + 149.991 + 62.5$$

$$S_{11} = 445.063$$

$$S_{12} = S_{21} = \sum_{i=1}^m \frac{EA}{L^3} \times (x_k - x_j)(y_k - y_j)$$

$$= \frac{80,000}{(400)^3} \times (282)(-282) + \frac{80,000}{(300)^3} \times (212)(212)$$

$$+ \frac{100,000}{(500)^3} \times (-433)(0-250) + \frac{100,000}{(400)^3} \times (-200)(0+346)$$

$$S_{12} = S_{21} = 12.237$$



Step # 04:-

7834

(8)

$$[D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.063 & 12.237 \\ 12.237 & 469.628 \end{bmatrix}^{-1} \times \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

Step # 05:-

[AM]

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.44 & 188.44 \\ -173.2 & -100 \\ -125 & 216.25 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

$$= \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + 188.44 \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ -125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 16.68 & + 30.46 \\ 22.29 & - 40.70 \\ -20.49 & + 21.6 \\ -14.79 & - 46.71 \end{bmatrix}$$

(16)

$$ii) D_1 = 0, D_1 = 1K'$$

7839

(16)

$$AMD = \frac{EA}{L^2} (y_k - y_j)$$

(17)

$$AMD_{12} = \frac{80,000}{(400)^2} (-282) = -141$$

$$AMD_{22} = \frac{80,000}{(300)^2} (212) = 188.44$$

$$AMD_{32} = \frac{100,000}{(500)^2} (-250) = -100$$

$$AMD_{42} = \frac{100,000}{(400)^2} (346) = 216.25$$

$$\text{Now } S_{22} = \sum_{i=1}^m \frac{EA}{L^3} (y_k - y_j)^2$$

$$= \frac{80,000}{(400)^3} (-282)^2 + \frac{80,000}{(300)^3} (212)^2 + \frac{100,000}{(500)^3} (-250)^2$$

$$+ \frac{100,000}{(400)^3} (346)^2$$

$$S_{22} = 469.628$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 47.136t \\ -18.413t \\ 1.11t \\ -61.498t \end{bmatrix}.$$

