

Name : Husna Pervez

ID : 6965

Program : Bs DT

Date : 22 - 6 - 2020.

(1)

Q:- a) Calculate the correlation coefficient between  $x$  and  $y$ .

Price ( $x$ )	3	4	5	6	7	8	9	10	11	13
Demand ( $y$ )	25	24	20	20	19	17	16	13	10	8

Ans

$x$	$y$
3	25
4	24
5	20
6	20
7	19
8	17
9	16
10	13
11	10
13	8

$$\bar{y} = \frac{172}{10} = 17.2$$

$$\bar{x} = \frac{76}{10} = 7.6$$

$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sqrt{\sum (x - \bar{x})^2 \sum (y - \bar{y})^2}}$$

$$r = \frac{\sum (76 - 7.6)(172 - 17.2)}{\sqrt{\sum (68.4)^2 \sum (154.8)^2}}$$

(2)

$$\gamma = \frac{10588.32}{112112520}$$

$$\gamma = \frac{10588.32}{10588.32} \quad \boxed{1.00000}$$

→ b) Given the following Set of values.

x	20	11	15	10	17	18	21	25	28
y	5	15	14	17	8	9	12	16	18

Ans.	x	y	xy
3	20	5	100
4	11	15	165 ✓
		14	20
5	15	17	170
6	10	8	136
7	17	9	162
		12	252
8	18	16	400
9	21	18	504
10	25	14	2099
11	28		
12	165		



(3)

$$b_{xy} = \frac{\sum xy - \frac{\sum x \sum y}{n}}{\sum x^2 - \frac{(\sum x)^2}{n}}$$

$$b_{xy} = \frac{2099 - 165 \times 114}{165^2 - 114^2}$$

$$b_{xy} = \frac{2099 - 18810}{27225 - 12996}$$

$$b_{xy} = \frac{2099 - 18810}{27225 - 12996}$$

$$b_{xy} = \frac{-1671}{14229}$$

$$b_{xy} = -0.1174$$

$$b_{xy} = 0.1158644$$

$$144229$$

Q.14 Determine the equation of the least squares regression line of  $y$  on  $x$  and  $x$  on  $y$ .

$x$	$y$	$x^2$	$y^2$	$xy$
20	5	400	25	100
11	15	121	225	165
15	14	225	196	210
10	17	100	289	170
17	8	289	64	136
18	9	324	81	162
22	12	484	144	264
25	16	625	256	400
27	18	729	324	486
165	124	27225	1604	2099

(4)

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{9(2099) - (165)(124)}{9(3309) - (165)^2}$$

$$b = \frac{18891 - 20460}{29781 - 27225}$$

$$b = \frac{-1569}{2556}$$

$$b = -0.6$$

$$a = \frac{\sum y}{n} = b \sum x$$

$$a = \frac{124 - (-0.6)(165)}{9}$$

$$= \frac{124 - (-99)}{9}$$

$$a = 247$$

→ Hence the required regression line is given by

$$\hat{y} = a + bx$$
$$\hat{y} = 247 - 0.6x$$

(5)

Regression line  $x$  on  $y$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum y^2 - (\sum y)^2}$$

$$b = \frac{9(2099) - (165)(124)}{9(1604) - (124)^2}$$

$$b = \frac{18891 - 20460}{14436 - 15376}$$

$$b = \frac{1569}{-940}$$

$$b = 1.7$$

$$a = \frac{\sum x - b \sum y}{n} = \frac{165 - (1.7)(124)}{9}$$

$$a = \frac{165 - 210.8}{9}$$

$$a = \frac{45.8}{9}$$

$$a = -5.1$$

Hence the required regression line is given by

$$\hat{x} = a_1 + b_1 y$$

$$\hat{x} = -5.1 + 1.7y$$



(6)

Find the product value of  
 $y$  for  $x = 20, 11, 15, 25, 28$

$x$  for  $y = 5, 15, 9, 12, 16, 18$

$$\hat{y} = 24.7 - 0.6x$$

$$\hat{x} = -5.1 + 1.7y$$

$x$	$y$	$\hat{y} = 24.7 - 0.6x$	$\hat{x} = -5.1 + 1.7y$
20	5	12.7	3.4
11	15	18.1	20.4
15	9	15.1	10.2
25	12	9.7	15.3
28	16	7.9	22.1
	18		25.5

→ This is the required product value.

Q2)

Q:- A fair coin is tossed 5 times. Find the probabilities of obtaining various number of heads.

Ans. Each coin has two probable results. Probability of getting head.  $p = \frac{1}{2}$

(7)

Toss = 5 Time

$$P(2 \text{ head and 1 tail}) = \binom{5}{2} \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right) = \frac{5}{8}$$

$$P(1 \text{ head and 2 tails}) = \frac{5}{8} \left(\frac{1}{2}\right) \left(\frac{1}{2}\right)^2 = \frac{5}{8}$$

$$\text{Probability of (head)} = \frac{5}{8} + \frac{5}{8} = \frac{10}{8} = 1.25$$

part (b)

Two possible outcome: win and not win

⇒ Prob. A winning  $P = \frac{2}{3}$

• 10 games

•  $n = 10$   $P = \frac{2}{3}$

• Successive games won and

• Last independy win

$$i) P(x=4) = \frac{10}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right) = \frac{1128}{6561} = 0.1996$$

$$ii) P(x > 4) = 1 - P(x < 4) = 1 - \sum_{x=0}^4 \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= 1 - \left[ \left(\frac{1}{3}\right)^{10} + \binom{10}{1} \left(\frac{2}{3}\right) \left(\frac{1}{3}\right)^9 + \binom{10}{2} \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^8 + \binom{10}{3} \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^7 \right]$$

$$= 1 - \frac{1}{6561} (10 + 16 + 28 + 448)$$

$$= 1 - \frac{527}{6561} = \frac{5984}{6561} = 0.9121$$

$$P(x > 6) = \sum_{x=7}^{10} \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= \frac{10}{6} \left(\frac{2}{3}\right)^6 \left(\frac{2}{3}\right) \left(\frac{1}{3}\right)^4 + \binom{10}{7} \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^3 + \binom{10}{8} \left(\frac{2}{3}\right)^8 \left(\frac{1}{3}\right)^2$$

$$= \frac{100}{6561} (30 + 16 + 2) = \frac{100 \times 48}{6561} = \frac{4800}{6561} = 0.7316$$



(8)

$$\begin{aligned}
 P(3 \leq 1 \leq 6) &= \sum_{k=3}^6 \binom{16}{k} \left(\frac{2}{3}\right)^k \left(\frac{1}{3}\right)^{16-k} \\
 &= \frac{16}{3} \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^{13} + \binom{16}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^{12} + \binom{16}{5} \left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right)^{11} + \binom{16}{6} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^{10} \\
 &= \frac{\binom{16}{3}}{3} (50 + 160 + 340 + 244) \\
 &= \frac{10 \times 644}{6561} = \frac{6440}{6561} \approx 0.98155
 \end{aligned}$$

Q. The following give the number of children born to 50 women.

2	6	1	5	4	3	3	8	10	1
4	3	3	0	5	2	1	4	10	3
5	3	3	6	3	3	2	2	7	4
1	4	2	4	4	4	6	8	10	7
7	5	6	5	3	2	3	9	2	2

1) Construct the ungrouped frequency distribution of these data.

No	Woman	Frequency	Cumulative Frequency
0	1	1	1
1		4	5
2		8	13
3		11	24
4		8	32
5		5	37
6		4	41
7		4	44
8		2	46
9		1	47
10		2	50

Q No (3) PART (A)

(9)

Q.3 Given information of children  
PART born to 50 women  
(B)

2	6	1	5	4	3	3	8	10	1
4	3	3	0	5	7	1	4	10	3
5	3	3	6	3	3	3	2	2	7
1	4	2	4	4	6	8	10	10	2
7	5	6	5	3	2	3	9	2	1

Grouped Frequency distribution  
for given data.

$$N = 50 \quad X_0 = 1, \quad X_m = 10$$

$$\text{Range} = \frac{X_m - X_0}{1} \\ 10 - 1 = \boxed{9}$$

$$K = 1 + 3.3 \log(50)$$

$$= 1 + 3.3 (1.695)$$

$$= 1 + 5.6066$$

$$K = 6.6066 = \boxed{6}$$

$$h = \text{class interval} = \frac{\text{Range}}{K}$$

$$h = \frac{9}{6} = 1.285 = \boxed{2}^K$$

(10)

We find out The information from data.

$N: 50$  ,  $R: 9$  ,  $K: 6$  ,  $h: 2$

Classes	Frequency	Class boundary	Midpoint
0-1	5	-0.5-1.5	1
2-3	19	1.5-3.5	2.5
4-5	13	3.5-5.5	4.5
6-7	7	5.5-7.5	6.5
8-9	3	7.5-9.5	8.5
10-11	3	10.5-11.5	11

Total:

R. Frequency	R. Frequency	C.F	R.C.F
$5/50$	$5/50 \times 100 = 10$	5	$5/50 = 0.1$
$19/50$	$19/50 \times 100 = 38$	24	$24/50 = 0.48$
$13/50$	$13/50 \times 100 = 26$	37	$37/50 = 0.74$
$7/50$	$7/50 \times 100 = 14$	44	$44/50 = 0.88$
$3/50$	$3/50 \times 100 = 6$	47	$47/50 = 0.94$
$3/50$	$3/50 \times 100 = 6$	50	$50/50 = 1$