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Probability and Statistics

Solution:-

(i) (A) least square Regression Equation.

$$\bar{y} = a + b\bar{x}$$

$$a = \bar{y} - b\bar{x}$$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

X	Y	XY	X ²	Y ²
53	20	1060	2809	400
62	32	1984	3844	1024
57	45	2565	3249	2025
71	60	4260	5041	3600
78	80	6240	6084	6400
I.D 86	100	8600	8400 7396	10000
86	120	10320	7396 7396	14400
87	140	12180	7569 7569	19600
96	160	15360	19216 8281	25600
91	180	16380	8281	32400
94	200	18800	8836	40000
94	210	19740	8836	44100
$\sum x = 955$	$\sum y = 1347$	$\sum xy = 117489$	$\sum x^2 = 75587$	$\sum y^2 = 199549$

$$\bar{x} = \frac{\sum x}{n} = \frac{955}{12} = 79.58 \quad (\because n=12)$$

$$\bar{y} = \frac{\sum y}{n} = \frac{1347}{12} = 112.25$$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{12(117489) - (955)(1347)}{12(78557) - (955)^2}$$

$$b = \frac{1409868 - 1286835}{942684 - 912025}$$

$$= \frac{123483}{30659}$$

~~b = 3.79~~

b = 4.02

$$a = \bar{y} - b\bar{x}$$
$$a = 112.25 - 4.02(79.58)$$
$$= 112.25 - 320.518$$

~~a = -208.268~~

a = -208.268

~~$\hat{y} = -208.268 + 4.02x$~~

$\hat{y} = -208.268 + 4.02x$

Regression line Equation

Co-efficient Correlation Y on X :-

$$r = \frac{n \sum xy - \sum x \sum y}{\sqrt{(n \sum x^2 - (\sum x)^2)(n \sum y^2 - (\sum y)^2)}}$$

$$r = \frac{12(117489) - (955)(1347)}{\sqrt{(12(78557) - (955)^2)(12(199549) - (1347)^2)}}$$

$$r = \frac{1409868 - 1286385}{(942684 - 912025)(2394588 - 1814409)}$$

$$r = \frac{123483}{(30659)(580179)}$$

$$r = \frac{123483}{1.778770796 \times 10^{10}}$$

$$r = 6.942041115 \times 10^{-6}$$

Hence the estimated Regression coefficient $b = 6.94 \times 10^{-6}$ which indicate that value of y increase by 6.94×10^{-6} units of increases in x

Q # 2(a)

Solution

n(S) = (13/3) = 286

Let A = Denote all balls of different colours.

n(A) = (4/1)(4/1)(5/1) = 4 x 4 x 5 = 80

P(A) = n(A)/n(S) = 80/286 = 0.28

4-R
4-W
5-G
13-balls

2 x 2 x 2 = 8

even x even x even = even

3 x 2 x 2 = 12

odd x even x even = even

3 x 3 x 2 = 18

odd x odd x even = even

Interpretation:-

There are 28% chances that all the balls are of different colours.

Let B = Denote All balls of same colours

Red white Green

n(B) = (4/3) or (4/2) or (5/3)

= (4/3) + (4/2) + (5/3) = 4 + 4 + 10 = 18

P(B) = n(B)/n(S) = 18/286 = 0.063

Interpretation:-

There are 6.3% chances that all balls are of same colours.

Q # 2(b)

5

Solution:-

$$n(S) = \binom{12}{4} = 495$$

Let $A =$ denote the event that exactly one egg is bad.

$$n(A) = \binom{2}{1} \binom{10}{3} = 2 \times 120 = 240$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{240}{495} = 0.48$$

Interpretation:-

There are 48% chances that exactly one egg is bad.

(ii) Let $B =$ be the event that at least one bad egg is selected.

$$\begin{aligned} n(B) &= \binom{2}{1} \binom{10}{3} + \binom{2}{2} \binom{10}{2} \\ &= 2 \times 120 + 1 \times 45 = 240 + 45 = 285 \end{aligned}$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{285}{495} = 0.58$$

Interpretation:-

There are 58% chances that at least one bad egg is selected.

Q #3

②

The following Scores are made by three batsmen A, B and C in a Series of innings.

A	B	C
12	47	15
15	12	23
6	76	52
73	48	4
7	4	24
86	86	86
199	37	74
36	48	52
84	13	13
29	3	4

$$\begin{aligned}\text{Range of A} &= \mathcal{M} - \mathcal{M}_0 \\ &= 199 - 6 \\ &= 193\end{aligned}$$

$$\begin{aligned}\text{Range of B} &= \mathcal{M} - \mathcal{M}_0 \\ &= 86 - 3 \\ &= 83\end{aligned}$$

$$\begin{aligned}\text{Range of C} &= \mathcal{M} - \mathcal{M}_0 \\ &= 86 - 4 \\ &= 82\end{aligned}$$

Batsmen A		Batsmen B		Batsmen C (7)	
X	X ²	Y	Y ²	Z	Z ²
12	144	47	2209	15	225
15	225	12	144	23	529
6	36	76	5776	52	2704
73	5329	48	2304	4	16
7	49	4	16	24	576
86	7396	86	7396	86	7396
199	39601	37	1369	74	5476
36	1296	48	2304	52	2704
84	7056	13	169	13	169
29	841	3	9	4	16
$\Sigma x = 547$	$\Sigma x^2 = 61973$	$\Sigma y = 374$	$\Sigma y^2 = 21696$	$\Sigma z = 347$	$\Sigma z^2 = 19811$

Batsmen A

$$\bar{X} = \frac{\Sigma x}{n} \quad \therefore n = 10$$

$$= \frac{547}{10} = 54.7$$

$$S_n = \sqrt{\frac{\Sigma x^2}{n} - \left(\frac{\Sigma x}{n}\right)^2}$$

$$= \sqrt{\frac{61973}{10} - \left(\frac{547}{10}\right)^2}$$

$$= 56.614$$

$$C.V = \frac{56.614 \times 100}{\bar{x}} = \frac{56.614}{54.7}$$

$$C.V = 1.03 \times 100 \\ = \underline{103.34}$$

Batsman B

$$\bar{y} = \frac{\sum y}{n} = \frac{374}{10} = 37.4$$

$$S_y = \sqrt{\frac{\sum y^2}{n} - \left(\frac{\sum y}{n}\right)^2} \\ = \sqrt{\frac{21696}{10} - \left(\frac{374}{10}\right)^2} \\ = 27.76$$

$$C.V = \frac{27.76}{37.4} \times 100 \\ = 74.22\%$$

Batsmen C :-

(7)

$$Z = \frac{\Sigma z}{n} = \frac{347}{10} = 34.7$$

$$S_2 = \sqrt{\frac{\Sigma z^2}{n} - \left(\frac{\Sigma z}{n}\right)^2}$$

$$= \sqrt{\frac{19811}{10} - \left(\frac{347}{10}\right)^2}$$

$$= 27.87$$

$$C.V = \frac{S_2}{Z} \times 100$$

$$= \frac{27.87}{34.7} \times 100$$

$$= 79.85$$

Batsman B is more consistent as its value of Co-efficient of variance is smallest.

Compare A with B

B is consistent

Compare B with C

B is more consistent

Compare A with C

C is more consistent