

# Course Details

Course Title

Electrical Network  
Analysis

Module

4th

# Student Details

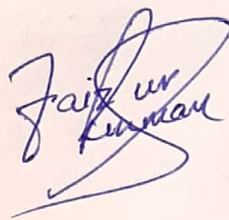
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Q<sub>13</sub> Assume that a 2000-kW -----  
----- But keep it from being  
overloaded?

Sol  
Original load:

$$P_1 = 2000 \text{ kW}, \quad \cos \theta = 0.85 \rightarrow \theta_1 = 31.79^\circ$$

$$S_1 = \frac{P_1}{\cos \theta_1} = 2352.94 \text{ KVA}$$

$$Q_1 = S_1 \sin \theta_1 = 1239.5 \text{ KVAR}$$

Additional load:

$$P_2 = 300 \text{ kW} \quad \cos \theta_2 = 0.8 \rightarrow \theta_2 = 36.87^\circ$$

$$S_2 = \frac{P_2}{\cos \theta_2} = 375 \text{ KVA}$$

$$Q_2 = S_2 \sin \theta_2 = 225 \text{ KVAR}$$

Total load:

$$S = S_1 + S_2 = (P_1 + P_2) + j(Q_1 + Q_2) = P + jQ$$

$$P = 2000 + 300 = 2300 \text{ kW}$$

$$Q = 1239.5 + 225 = 1464.5 \text{ KVAR}$$

The minimum operating PF for a  
2300kW load & not exceeding  
the KVA rating of the generator is

$$\cos\phi = \frac{P}{S_1} = \frac{2300}{2352.94}$$

$$\Rightarrow 0.9775$$

OR

$$\phi = 12.177^\circ$$

The maximum load KVAR for this condition is

~~$$\cos\phi = \frac{P}{S_1} = \frac{2300}{S_1}$$~~

$$\phi = S_1 \sin\phi = 2352.94 \sin(12.177)$$

$$\phi = 496.313 \text{ KVAR}$$

The capacitor must supply the difference between the total load KVAR (i.e.  $\phi$ ) and the Permissible generator KVAR (i.e.  $\phi_n$ )

Thus,

$$\phi = \phi - \phi_n = 968.2 \text{ KVAR}$$

Q2

A balanced abc sequence one-line  
----- Find the phase and the  
currents.

Soln

Line voltage  $V_{AB} = 180 \angle -20^\circ \text{ V}$

$Z_\Delta = 20 \angle 40^\circ \Omega$

~~V<sub>L</sub>~~ Using formula

$V_L = \sqrt{3} V_p \angle 30^\circ \Rightarrow V_p = \frac{V_L}{\sqrt{3} \angle 30^\circ}$

Phase voltage:

$V_{an} = \frac{180 \angle -20^\circ}{\sqrt{3}} \angle -30^\circ$

$\Rightarrow 103.9 \angle -50^\circ \text{ V}$

$Z_Y = \frac{2\Delta}{3} = \frac{20 \angle 40^\circ}{3}$

$\Rightarrow 6.67 \angle 40^\circ \Omega$

Line current

$I_a = \frac{V_{an}}{Z_{\Delta/3}} = \frac{103.9 \angle -50^\circ}{6.67 \angle 40^\circ}$

$I_a = 15.57 \angle -90^\circ \text{ A}$

$I_b = I_a \angle -120^\circ = 15.59 \angle +150^\circ \text{ A}$

$I_c = I_a \angle +120^\circ = 15.59 \angle 30^\circ \text{ A}$

## Phase Current

$$I_{AB} = \frac{15.57 \angle -90^\circ}{\sqrt{3}} \angle 30^\circ$$
$$\Rightarrow 9 \angle -60^\circ \text{ A}$$

$$I_{BC} = I_{AB} \angle -120^\circ = 9 \angle -180^\circ \text{ A}$$

$$I_{CA} = I_{AB} \angle +120^\circ = 9 \angle 60^\circ \text{ A}$$

Q3

Consider a load with value -----

(a) -----

(b) -----

(c) The power factor &amp; the load impedance

Sol:

Given      Data

$$V_{rms} = 110 \angle 85^\circ \text{ V}$$

$$I_{rms} = 0.4 \angle 15^\circ \text{ A}$$

Step 2

The complex power is

$$S = V_{rms} I_{rms}$$

$$S = (110 \angle 85^\circ)(0.4 \angle -15^\circ)$$

$$S = 110 \times 0.4 \angle (85^\circ - 15^\circ)$$

$$\therefore \underline{S = 44 \angle 70^\circ \text{ VA}}$$

The apparent power is

$$S = |S|$$

$$S = 44 \text{ VA}$$

Step 3

Express the complex power in rectangular form

$$S = 44 \angle 70^\circ$$

$$S = 44 [\cos(70^\circ) + j \sin(70^\circ)]$$

$$S = 44 [0.3420 + j0.9397]$$

$$S = 15.05 + j41.35$$

Since  $S = P + jQ$

The real power is

$$\therefore P = 15.05 \text{ W}$$

The reactive power is

$$Q = 41.35 \text{ VAR}$$

Step 4

The power factor is

$$P_f = \cos(70^\circ)$$

$$P_f = 0.342 \text{ (lagging)}$$

The power factor is lagging as the reactive power is positive.

$$Z = \frac{V}{I}$$

$$V = \sqrt{2} V_{\text{rms}}$$

$$I = \sqrt{2} I_{\text{rms}}$$

Step 5

$$Z = \frac{110\sqrt{2} \angle 85^\circ}{0.4\sqrt{2} \angle 15^\circ}$$

$$Z = 275 \angle 70^\circ \Omega$$

$$Z = 275 [\cos(70^\circ) + j\sin(70^\circ)]$$

$$Z = 275 [0.342 + j0.9397]$$

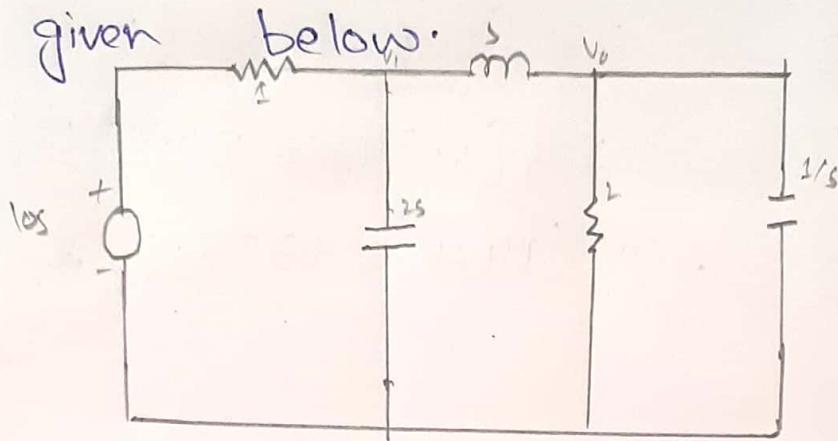
$$Z = (94.05 + j258.4) \Omega$$



Q<sub>14</sub> Apply Laplace transform  
in the circuit figure below.

Sol<sup>n</sup>

s-domain version of the circuit  
is given below.



Node 1

$$\frac{\frac{10}{s} - v_1}{1} = \frac{v_1 - v_o}{s} + \frac{s}{2} v_o \rightarrow 10 = (s+1)v_1 + \left(\frac{s^2}{2} - 1\right)v_o \rightarrow (1)$$

Node 2

$$\frac{v_1 - v_o}{s} = \frac{v_o}{2} + s v_o \rightarrow v_1 = v_o \left(\frac{s}{2} + s^2 + 1\right) \rightarrow (2)$$

Substituting (2) into (1) gives

~~$10 = (s+1)(s^2 + s/2 + 1)v_o + (s^2/2 - 1)v_o$~~

$$10 = (s+1)(s^2 + s/2 + 1)v_o + \left(\frac{s^2}{2} - 1\right)v_o = s(s^2 + 2s + 1.5)v_o$$

$$v_o = \frac{10}{s(s^2 + 2s + 1.5)} = \frac{A}{s} + \frac{Bs + C}{s^2 + 2s + 1.5}$$

$$I_0 = A(s^2 + 2s + 1.5) + Bs + C$$

$$s^2: \quad 0 = A + B$$

$$s: \quad 0 = 2A + C$$

$$\text{Constant: } I_0 = 1.5A \rightarrow A = 20/3 \quad B = -20/3, \quad C = -40/3$$

$$V_0 = \frac{20}{3} \left[ \frac{1}{s} - \frac{s+2}{s^2+2s+1.5} \right]$$

$$\Rightarrow \frac{20}{3} \left[ \frac{1}{s} - \frac{s+1}{(s+1)^2 + 0.7071^2} - 1.414 \frac{0.7071}{(s+1)^2 + 0.7071^2} \right]$$

Taking the inverse Laplace transform

finally yields.

$$V_0(t) = \frac{20}{3} \left[ 1 - e^{-t} \cos(0.7071t) - 1.414 e^{-t} \sin(0.7071t) \right] u(t) \text{ V}$$

Q For the circuit given in Figure below ---

(a) --- much

(b) --- much power is delivered to the speaker at that.

Given Data:

$$V_s = 5V_{rms}$$

$$C = 80nF$$

$$L = 80mH$$

Sol:

Source impedance =  $Z_s = R_s + jX_s$

Load impedance =  $Z_L = R_L + jX_L$

For maximum transfer

$$Z_L = Z_s \quad \text{mean}$$

$$R_L = R_s \quad \& \quad X_C = X_L$$

$$X_C = X_L$$

$$\frac{1}{\omega C} = \omega L$$

Re-arranging

$$\omega = \frac{1}{\sqrt{LC}} = 2\pi f$$

$$f = \frac{1}{2\pi\sqrt{LC}}$$

$$f \Rightarrow \frac{1}{2(3.14) \sqrt{(80 \times 10^{-3})(80 \times 10^{-9})}}$$

$$\Rightarrow \frac{1}{6.28 \sqrt{(80)^2 \times 10^{-12}}}$$

$$\Rightarrow \frac{1}{(6.28)(80)(\sqrt{10^{-12}})}$$

$$\Rightarrow \frac{1}{(6.28)(80)(0.000001)}$$

$$\Rightarrow \frac{1}{0.0005024}$$

$$f = 1990.44 \text{ Hz}$$

Now Part B

As we know that

$$\text{Power deliver} = P = \left( \frac{V_s}{R_{eq}} \right)^2$$

$$P = \left( \frac{V_s}{R_1 + R_2} \right)^2 R_L$$

$$P = \left( \frac{5}{10 + 4} \right)^2 4 = 0.5104 \text{ W}$$

$$\Rightarrow 510 \text{ mW.}$$