

Final Term Exam

Name M. Mansoor

ID 7810

Section 6 "A"

Subject Hydraulic Engineering

Submitted To Engr Fawad

Q.01 A prototype gate valve which will control the flow in pipe -----

Solution:

We should have to find the relevant variable and its dimension

$$* \Delta p \Rightarrow ML^{-1}T^{-2}$$

$$* h \Rightarrow L$$

$$* V \Rightarrow LT^{-1}$$

$$* \rho \Rightarrow ML^{-3}$$

$$* \mu \Rightarrow ML^{-1}T^{-1}$$

$$* d \Rightarrow L$$

So The total number of variable = 6 = η

number of independent variable

$$= m = 3 [MLT]$$

Number of non dimensional group

$$= \eta - m = 6 - 3$$

$$= 3$$

Select $m=3$ scaling variable

- geometric (d)
- kinematic / ~~time~~ dependent (v)
- dynamic / mass dependent (P)

Now we have to form dimensionless group by non dimensionalising the remaining variable which are ΔP , h and μ

Thus write the $\bar{\pi}$ term as

$$\bar{\pi}_1 = \Delta P d^a v^b \rho^c$$

$$\begin{aligned} M^0 L^0 T^0 &= (M L^{-1} T^{-2}) (L)^a (L T^{-1})^b (M L^{-3})^c \\ &= M^{1+c} \cdot L^{-1+a+b-3c} \cdot T^{-2-b} \end{aligned}$$

$$\Rightarrow M \Rightarrow 0 = 1+c \Rightarrow c = -1$$

$$\Rightarrow L \Rightarrow 0 = -1+a+b-3c$$

$$a = 1+3c-b = 0$$

$$a = 1 + 3c - b$$

$$a = 1 + 3(-1) - (-2)$$

$$a = 1 - 3 + 2$$

$$a = 0$$

$$\Rightarrow T \Rightarrow 0 = +2 - b \Rightarrow b = -2$$

$$\begin{aligned}\bar{\Lambda}_1 &= \Delta p d^0 v^{-2} \rho^{-1} \\ &= \Delta p v^{-2} \rho^{-1}\end{aligned}$$

$$\boxed{\bar{\Lambda}_1 = \frac{\Delta p}{\rho v^2}}$$

$$\Rightarrow \bar{\Lambda}_2 = \frac{h}{d} \rightarrow$$

$$\Rightarrow \bar{\Lambda}_3 = u d^a v^b \rho^c$$

$$\begin{aligned}\Rightarrow M^0 L^0 T^0 &= (M L^{-1} T^{-1}) (L)^a (L T^{-1})^b (M L^{-3})^c \\ &= \cancel{M} \cancel{L} \cancel{T} \\ &= M^{1+c} \cdot L^{-1+a+b-3c} \cdot T^{-1-b}\end{aligned}$$

$$\Rightarrow M \Rightarrow 0 = 1 + c \Rightarrow c = -1$$

$$\Rightarrow L \Rightarrow 0 = -1 + a + b - 3c \Rightarrow a = 1 - b + 3c$$

$$a = 1 - (-1) + 3(-1)$$

$$a = 1 + 1 - 3$$

$$a = 2 - 3$$

$$a = -1$$

$$\Rightarrow T \Rightarrow 0 = -1 - b \Rightarrow b = -1$$

$$\Rightarrow \pi_3 = \mu d^{-1} v^{-1} p^{-1}$$

$$\boxed{\bar{\pi}_3 = \frac{\mu}{pvd}}$$

$$\Rightarrow \bar{\pi}'_3 = (\bar{\pi}_3)^{-1} = \frac{pvd}{\mu}$$

Hence dimensional analysis yield

$$\bar{\pi}_1 = f(\bar{\pi}_2, \bar{\pi}'_3)$$

$$\Rightarrow \frac{\Delta P}{\rho V^2} = f\left(\frac{h}{d}, \frac{\rho V d}{\mu}\right)$$

a) As for the dynamic similarities all non dimensional group must be same in model as well as prototype so

$$\bar{\pi}_1 = \left[\frac{\Delta P}{\rho V^2} \right]_p = \left[\frac{\Delta P}{\rho V^2} \right]_m$$

$$\bar{\pi}_2 = \left[\frac{h}{d} \right]_p = \left[\frac{h}{d} \right]_m$$

$$\bar{\pi}_3 = \left[\frac{\rho V d}{\mu} \right]_p = \left[\frac{\rho V d}{\mu} \right]_m$$

From \bar{n}_3 we have the following velocities ratio

$$\frac{v_p}{v_m} = \frac{(u/p)_p}{(u/p)_m} \cdot \frac{d_m}{d_p}$$

$$= \frac{0.02/800}{1.0 \times 10^{-6}} \times \frac{1}{5}$$

$$\frac{v_p}{v_m} = 0.5$$

Hence $v_m = \frac{v_p}{0.5} = \frac{3.0}{0.5}$

$$v_m = 6 \text{ m/s}$$

b) The ratio of Quantities of flow is

$$\frac{Q_p}{Q_m} = \frac{(\text{velocity} \times \text{Area})_p}{(\text{velocity} \times \text{area})_m}$$

$$= \frac{v_p}{v_m} \cdot \left[\frac{d_p}{d_m} \right]^2$$

$$= 0.5 \times 5^2$$

$$\Rightarrow \frac{Q_p}{Q_m} = 12.5$$

c) Now the pressure drop in the prototype

$$\text{As } \bar{\lambda}_1 = \left[\frac{\Delta P}{\rho V^2} \right]_p = \left[\frac{\Delta P}{\rho V^2} \right]_m$$

$$\Rightarrow \frac{(\Delta P)_p}{(\Delta P)_m} = \frac{\rho_p}{\rho_m} \cdot \left(\frac{V_p}{V_m} \right)^2$$

$$= \frac{800}{1000} \times (0.5)^2$$

$$\frac{(\Delta P)_p}{(\Delta P)_m} = 0.2$$

$$\Rightarrow (\Delta P)_p = 0.2 \times \Delta P_m$$

$$= 0.2 \times 60$$

$$\boxed{\Delta P_p = 12 \text{ kPa}}$$

Q.02

Given Data:

Max depth of water in Reservoir = 78m
 Specific Gravity of Dam Material = $G = 2.35$

Allowable Compression stress for the
 Dam Masonary $\sigma_{all} = 781 \frac{T}{m^2}$

Height of wave = 1.35m

$$u = 0.7$$

No uplift pressure, $C_u = 0$

Solution:

$$\begin{aligned} 1) H_{\text{limiting}} &= \frac{G \sigma_{all}}{\gamma_w (G - C_u + 1)} \\ &= \frac{781 \times 1000}{1000 (2.35 - 0 + 1)} \end{aligned}$$

$$H_{\text{limiting}} = 233.134 > H_w = 78$$

So it is low gravity Dam

2) Top width "a"

$$\text{Free board} = 1.5 \text{ hwave}$$

$$= 1.5 \times 1.35$$

$$\text{F.B} = 2.02 \text{ m}$$

$$\text{Height of Dam} = H_D = H_w + \text{F.B}$$

$$= 78 + 2.02$$

$$= 80.02 \text{ m}$$

$$a = 14\% \text{ of } H_D$$

$$a = 0.14 \times 80.02$$

$$a = 11.20$$

3) Base width = b' (with out offset)

1) for no sliding criteria

$$b' = \frac{H_w}{u_g} = \frac{78}{0.7 \times 2.35}$$

$$b' = 47.5 \text{ m}$$

(10)

ii) For no tension crit.

$$b' = \frac{Hw}{\sqrt{G}} = \frac{78}{\sqrt{2.35}}$$

$$b' = 51 \text{ m}$$

use $b' = 51 \text{ m}$

4) Depth of vertical position on U/S side

$$h' = 2a \sqrt{C_1 - C_2}$$

$$h' = 2 \times 11.20 \sqrt{2.35} - 0$$

$$h' = 34.338 \text{ m}$$

5) up stem ~~side~~ offset

$$\Rightarrow \frac{a}{16} = \frac{11.20}{16}$$

$$= 0.7 \text{ m}$$

6) Depth below the water level to the end of inclined position is $4/5 = 3.149 \sqrt{g}$

$$= 3.149 \sqrt{g}$$

$$= 3.14 \times 11.20 \sqrt{2.35}$$

$$= 53.91$$

$$\approx 54 \text{ m}$$

7) Total width:

$$b = b' + \frac{a}{16} = 51 + \frac{11.20}{16}$$

$$= 51 + 0.7$$

$$= 51.7 \text{ m}$$

$$8) \tan \alpha = \frac{b'}{H} = \frac{51}{78}$$

$$\tan \alpha = \left(\frac{17}{26} \right)$$

$$\alpha = \tan^{-1} \left(\frac{17}{26} \right)$$

$$\alpha = 33.17^\circ$$

9) Depth of vertical position on D/S
(from WL on U/S side)

$$\tan \alpha = \frac{q}{d'} = \frac{11.20}{d'}$$

$$\Rightarrow \tan \alpha = \frac{11.20}{d'}$$

$$\frac{17}{26} d' = 11.20$$

$$d' = \frac{11.20 \times 26}{17}$$

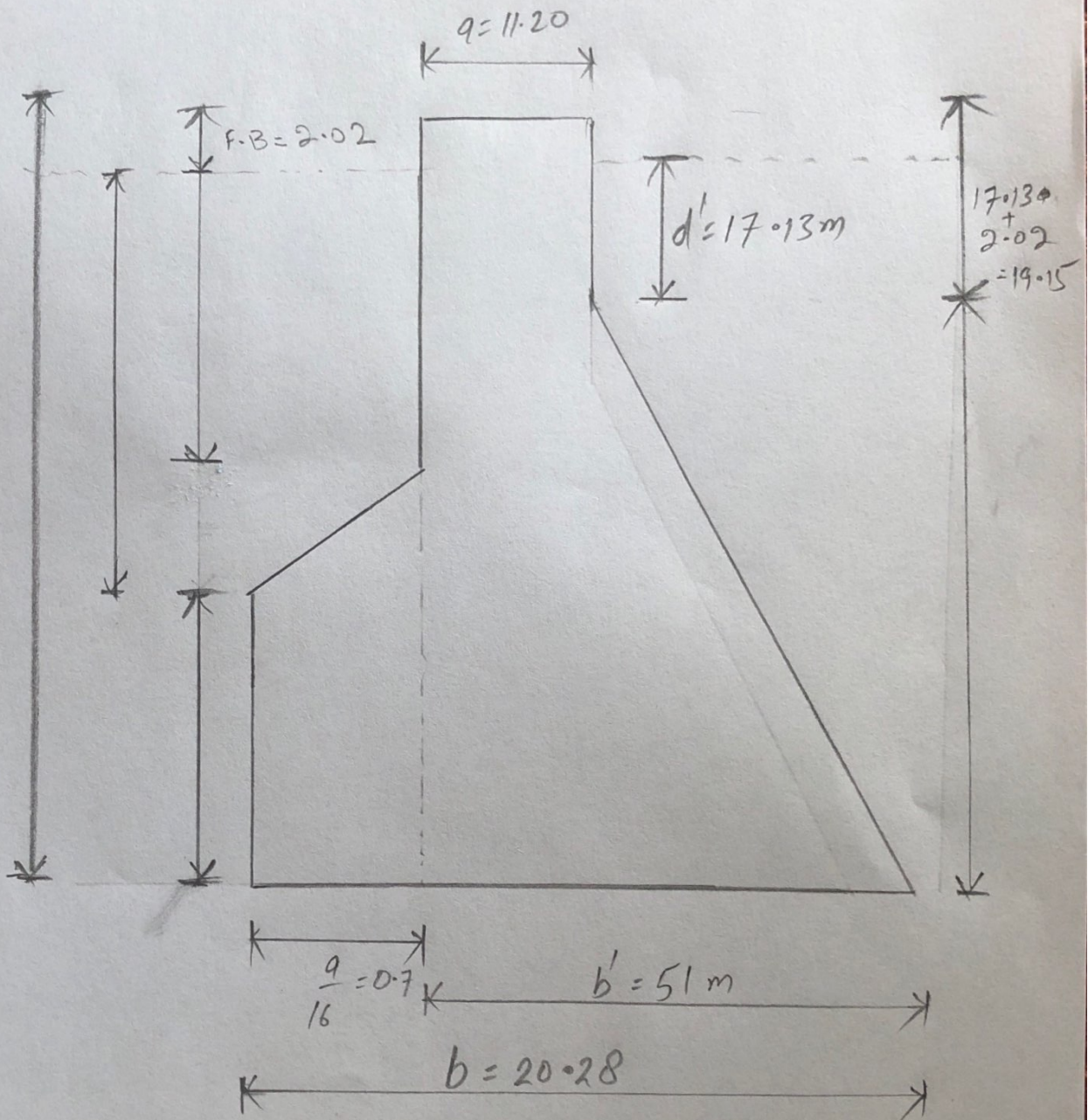
$$d' = 17.13 \text{ m}$$

Depth on vertical position:-

$$d = d' + F.B$$

$$d = 17.13 + 2.02$$

$$\Rightarrow d = 19.15$$



Q:04 What will be the effect of sediment particles, diameter, particle density, particle concentration, particle shape, viscosity of water, turbulence of water flowing in reservoir on fall velocity? Explain in detail.

Ans

Particle diameter:

The diameter of particle is directly proportional to the fall velocity. Greater the size of particle, so it will be faster as compared to the particle of small size. Thus there will be more gravitational force on particle of greater size, so it will fall quickly due to its weight.

Particle Density:

Density of particle is directly proportional to the rate of fall velocity since

Particle with high density tends to settle down early compare with particle of low density.

Particle Concentration:

Concentration of particle size will considerably effect its fall velocity as the section having greater concentration will be settle down at the place thus causing more fall velocity comparing with section of low concentration

Particle shape:

Non-spherical analogue particle fall up to 75% slower than equivalent sphere model show 100 μm non spher spherical particle travel 44% further than spherical

Viscosity of water:-

fluid velocity through porous media is approximated as inversely

Rto

proportional to the kinematic viscosity
A decrease in viscosity therefore
increase the fall velocity

Turbulence of water:

Turbulence of water effect the
fall velocity of water in reservoirs
because the non-linearity and non
uniform path of effect the flow
of water and cause the variation
in the flow.