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Section: B

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Subject: Hydraulic engineering

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Q# 01

Part (A)

Given data:-

$$\text{Discharge } Q = 7886 \text{ Lit/sec}$$

$$\frac{7886}{1000} = 7.886 \text{ m}^3/\text{sec}$$

$$\text{Width} = b = 8 \text{ m}$$

$$\text{Mean velocity} = v = 7886 - 220$$

$$= \frac{7666}{3.28} = 2337.19 \text{ m}^3/\text{sec}$$

Height of hydraulic jump:-

As we know that

$$q = Q/b$$

$$q = 7.886/8$$

$$q = 0.9857 \text{ m}^2/\text{sec}$$

=&gt; Critical depth:-

$$y_c = \left( \frac{q^2}{g} \right)^{1/3} = \left( \frac{(0.9857)^2}{9.81} \right)^{1/3}$$

$$y_c = 0.46267 \text{ m}$$

=&gt; Critical velocity:-

As we know that

$$q = Vy \Rightarrow V = q/y$$

$$V_c = q/y_c$$

$$V_c = \frac{0.9857}{0.46267}$$

$$V_c = 2.13046 \text{ m/sec}$$

Depth of water on upstream side of Hydraulic jump.

As we know that

$$Q = AV \Rightarrow Q = (b \times y) V$$

$$\Rightarrow y = \frac{Q}{V \cdot b} \Rightarrow y_1 = \frac{Q}{V_1 \cdot b}$$

$$y_1 = \frac{7.886}{2.13046 \times 8} = 0.4598$$

To find water depth on downstream side by using that formula.

$$y_2 = \frac{-y_1}{2} + \sqrt{\frac{y_1^2}{4} + \frac{2y_1 V_1^2}{g}}$$

$$y_2 = \frac{-0.4598}{2} + \sqrt{\frac{(0.4598)^2}{4} + \frac{2(0.4598)(2.13046)^2}{9.81}}$$

$$y_2 = 0.92151 \text{ m}$$

Difference in depth:-

$$\Delta y = y_2 - y_1$$

$$\Delta y = 0.92151 - 0.4598$$

$$\Delta y = 0.46171 \text{ m}$$

By discharge formula:-

$$Q_1 = Q_2$$

$$A_1 V_1 = A_2 V_2$$

$$K_{y_1} \cdot V = K_{y_2} \cdot V_2 \quad ; b = b_1 = b_2$$

$$V_2 = \frac{y_1 V_1}{y_2} = \frac{0.4598 \times 2327.19}{0.92151}$$

$$V_2 = 1166.1728 \text{ m/sec}$$

Since,

$$\Delta E = E_1 - E_2$$

$$E_1 - E_2 = \left( y_1 + \frac{V_1^2}{2g} \right) - \left( y_2 + \frac{V_2^2}{2g} \right)$$

$$= \left( 0.4598 + \frac{(2327.19)^2}{2 \times 9.81} \right) - \left( 0.92151 + \frac{(1166.1728)^2}{2 \times 9.81} \right)$$

$$\Delta E = 209097.3006$$

Power Dissipation in Hydraulic Jump:-

As we know that

$$\Delta P = \rho g Q [E_1 - E_2]$$

$$\Delta P = (1000)(9.81)(9.886)(209097.3006)$$

$$\Delta P = 2.027860331 \times 10^{10} \text{ Watts} \text{ Ans}$$

Q#01

Part (B)

Given data:-

Channel width =  $b = 4\text{m}$ Discharge  $Q = 7886 \text{ ft}^3/\text{sec}$ 

$$Q = \frac{7886}{1000} = 7.886 \text{ m}^3/\text{sec}$$

Depth of upstream side =  $2.9\text{m}$ Depth of downstream side =  $1.1\text{m}$ 

Solution:-

→ Downstream Velocity:-

As from specific energy equation specific energy remain same on both stream.

$$E_1 = E_2$$

$$y_1 + \frac{V_1^2}{2g} = y_2 + \frac{V_2^2}{2g} \rightarrow \text{A}$$

Also we know that

$$Q = AV$$

$$A_1 V_1 = A_2 V_2$$

$$b y_1 \cdot V_1 = b y_2 \cdot V_2$$

$$y_1 V_1 = y_2 V_2$$

$$V_2 = \frac{y_1 \cdot V_1}{y_2} = \frac{2.9}{1.1} V_1$$

$$V_2 = 2.63 V_1$$

Q# 2

Part (A)

Given data:-

$$\text{channel depth} = 1.8 \text{ m}$$

$$\text{Discharge } Q = 7886 \text{ ft}^3/\text{sec}$$

$$\text{Discharge} = 221.32 \text{ m}^3/\text{sec}$$

$$\text{Width of channel} = 66 \text{ ft}$$

$$= \frac{66}{3.28} = 20.12 \text{ m}$$

Required:-

$$\text{Weir height} = P = ?$$

Solution:-

As we know that

$$Q = AV$$

$$V = Q/A$$

$$V_1 = Q/b \times y = \frac{221.32}{20.12 \times 1.8}$$

$$V_1 = 6.11 \text{ m/sec}$$

Critical depth:-

As we know that

$$y_c = \left( \frac{q^2}{g} \right)^{1/3}$$

$$q = Q/b$$

$$q = \frac{221.32}{20.12}$$

$$y_c = \left( \frac{(11)^2}{9.81} \right)^{1/3}$$

$$20.12$$

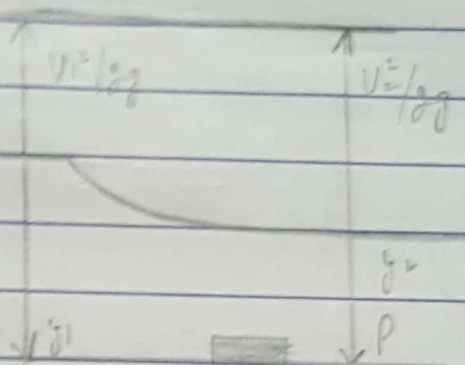
$$q = 11 \text{ m}^2/\text{sec}$$

$$y_c = 2.37 \text{ m}$$

$$\text{Also, } V = \sqrt{gy}$$

$$V_c = \sqrt{gy_c} = \sqrt{9.81 \times 2.31}$$

$$V_c = 4.76 \text{ m/sec}$$



According to the given figure

$$\frac{V_1^2}{2g} + y_1 = \frac{V_2^2}{2g} + y_c + P$$

$$\frac{6.11}{2 \times 9.81} + 1.8 = \frac{4.76}{2 \times 9.81} + 2.31 + P$$

$$1.902 + 1.8 = 1.1848 + 2.31 + P$$

$$\boxed{P = 0.237 \text{ m}}$$

So the weir should have height of 0.237m measured from the channel bed.

Put the value in equ (A)

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$2.9 + \frac{v_1^2}{2g} + 1.1 + \frac{(2.63 v_1)^2}{2g}$$

$$\frac{v_1^2}{2 \times 9.81} - \frac{6.91 v_1^2}{2 \times 9.81} = 1.1 - 2.9$$

$$\frac{v_1^2 - 6.91 v_1^2}{19.62} = -1.8$$

$$19.62$$

$$+ 5.91 v_1^2 = + (1.8)(19.62)$$

$$\sqrt{v_1^2} = \sqrt{\frac{(1.8)(19.62)}{5.91}}$$

$$\boxed{v_1 = 2.44 \text{ m/sec}}$$

Put the value of  $v_1$  in equ (A)

$$v_2 = 2.63 (v_1)$$

$$v_2 = 2.63 (2.44)$$

$$\boxed{v_2 = 6.41 \text{ m/sec}}$$



⇒ Type of flow on upstream side:-

By Froude number

$$Fr_1 = \frac{v}{\sqrt{gD}} = \frac{2.44}{\sqrt{9.81 \times 2.91}}$$

$$Fr_1 = 0.45$$

$Fr < 1 \rightarrow$  Sub critical flow

⇒ Type of flow on downstream side:-

$$Fr_2 = \frac{v_2}{\sqrt{gD_2}} = \frac{6.41}{\sqrt{9.81 \times 1.1}}$$

$$Fr_2 = 1.95$$

$Fr > 1 \rightarrow$  Super critical flow

Q#2

part (B)

Given data:

$$Breath = b = 2.8 \text{ m}$$

$$Depth = d = 1.5 \text{ m}$$

$$H_1 = 5 \text{ m}$$

$$H_2 = 5 + 1.5 = 6.5 \text{ m}$$

~~$$H = 5 + 1.5$$~~

$$H = 5 + 0.6 = 5.6$$

$$C_d = 0.781$$

Solution:-

→ Discharge through submerged portion.

By using formula

$$Q_1 = C_d \times b \times (H_2 - H) \times \sqrt{2gH}$$

$$Q_1 = 0.781 \times 2.8 \times (6.5 - 5.6) \times \sqrt{2(9.81)(5.6)}$$

$$Q_1 = 20.62$$

→ Discharge through free portion:-

As we know that

$$Q_2 = \frac{2}{3} C_d \times b \sqrt{2g} \times [H_2^{3/2} - H_1^{3/2}]$$

$$= \frac{2}{3} (0.781) \times 2.8 \sqrt{2 \times 9.81} \times [5.6^{3/2} - 5^{3/2}]$$

$$Q_2 = 13.37 \text{ m}^3/\text{sec}$$

Now total discharge will be

$$Q = Q_1 + Q_2$$

$$Q = 20.62 + 13.37$$

$$Q = 33.99 \text{ m}^3/\text{se}$$

Q#03

Part (A) Given data:-

$$d_1 = R - 200 \quad d_2 = R + 3000$$

$$d_1 = 7886 - 200 \quad d_2 = 7886 + 3000$$

$$d_1 = 7686 \text{ mm} \quad d_2 = 10886 \text{ mm}$$

Discharge,  $Q = 0.95 \text{ m}^3/\text{sec}$

Pressure in large pipe  $P_2 = R + 800$

$$= 7886 + 800$$

$$= 8686 \text{ N/m}^2$$

Solution:-

Headloss due to sudden Enlargement.

$$d_1 = 7686 \text{ mm} = 7.686 \text{ m}$$

$$A_1 = \frac{\pi}{4} d_1^2 = \frac{\pi}{4} (7.686)^2$$

$$A_2 = \frac{\pi}{4} d_2^2$$

$$A_1 = 46.37355 \text{ m}^2$$

$$A_2 = \frac{\pi}{4} (10886)^2$$

As we know that  $A_2 = 93096421.8$

$$Q = AV \Rightarrow V = Q/A$$

$$V_1 = Q/A_1 = 0.95 / 46.37355$$

$$V_1 = 0.020$$

$$\begin{aligned}
 \text{As } V_2 &= Q/A_2 \\
 &= 0.95 / 93026491.8 \\
 \boxed{V_2} &= \boxed{1.021215944 \times 10^{-6}}
 \end{aligned}$$

As sudden enlargement:-

$$h_e = \left(1 - \frac{A_1}{A_2}\right)^2 \times \frac{(V_1 - V_2)^2}{2g}$$

$$h_e = \left(1 - \frac{46.37355}{93026491.8}\right)^2 \times \frac{(0.020 - 1.021215944 \times 10^{-6})^2}{2 \times 9.81}$$

$$\boxed{h_e = 1.019315434 \times 10^{-3}}$$

Power loss due to sudden  
Enlargement:-

As we know that

$$P = \rho g Q h_e \quad (1.019315434 \times 10^{-3})$$

$$P = (1000)(9.81)(0.95) \times 1.019315434 \times 10^{-3}$$

$$\boxed{P = 9.4995}$$

Pressure in smaller pipe:-

Using Bernoulli equation:

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + h_e$$

$$\begin{aligned}
 \frac{P_1}{1000 \times 9.81} + \frac{(0.020)^2}{2 \times 9.81} &= \frac{P_2}{1000 \times 9.81} + \frac{(1.021215944 \times 10^{-6})^2}{2 \times 9.81} \\
 &+ 1.019315434 \times 10^{-3}
 \end{aligned}$$

$$\frac{P_1}{9810} + 0.0000203 = \frac{8686}{9810} + 5.115329218 \times 10^{-12}$$

$$+ 1.019315434 \times 10^{-3}$$

$$\frac{P_1}{9810} + 0.0000203 = 0.8864$$

$$\frac{P_1}{9810} = 0.8864 - 0.0000203$$

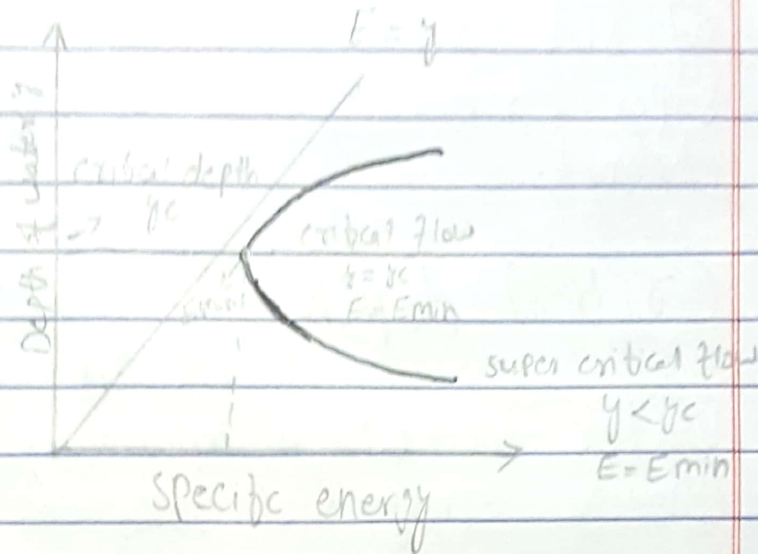
$$\frac{P_1}{9810} = 0.8863$$

$$P_2 = 8695.384 \text{ AN}$$

Q#03

Part (B)

Ans



### Black Curve:

→ from the given figures The black curve is the 3-degree polynomial curve which show the flow is critical, sub-critical and super critical flow.  
 ⇒ The Middle point show the depth of water is equal to minimum energy so the flow is critical flow.

$$y = y_c \text{ and } E < E_{\min}$$

### Specific energy:-

Specific energy is the parameter that can be used to clarify the meaning

of Sub-critical, Critical and Super-critical flow is an open channel.

Critical depth:-

Depth of Water at which minimum specific energy is obtained.

Equation of specific energy:-

$$(E-y)y^2 = q^2 / 2g \rightarrow \text{D}$$

$E$  = Specific energy

$y$  = depth of water

$q$  = discharge per unit

width its unit is  $m^2/\text{sec}$

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