

Haroon Rashid

Reg# 16549

Semester :6th

Subject: DLD Assignment

Submitted to: Sir MUHAMMAD AMIN

Q1

Answer:

$$Qa: 45.25_{10} = ()_2$$

$$\frac{45.25}{2} = 22.625 = 0.625 = 0$$

$$\frac{22}{2} = 11 = 0$$

$$\frac{11}{2} = 5.5 = 0.5 \times 2 = 1$$

$$\frac{5}{2} = 2.5 = 0.5 \times 2 = 1$$

$$\frac{2}{2} = 1$$

$$(00111)_2$$

(b)

$$10000000 \cdot 1010_2 = ()_{10}$$

$$= 10000000 \cdot 1010$$
$$= 2^7 \cdot 2^6 + 2^7 \cdot 2^4 + 2^7 \cdot 2^3 + 2^7 \cdot 2^1 + 2^0 + 2^{-1} + 2^{-2} + 2^{-3} + 2^4$$

$$= 10000000 \cdot 1010$$
$$2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 \cdot 2^{-1} + 2^{-2} + 2^{-3} + 2^{-4}$$

Value of zero will not be considered

$$= 2^7 \cdot 2^{-1} + 2^{-3}$$

$$= 128 \cdot 0.5 + 0.125$$

=

(c)

$$4D7F_{16} = ()_{10}$$

$$4D7F_{16} = \begin{array}{|c|c|c|c|} \hline 4 & D & 7 & F \\ \hline 0100 & 1101 & 0111 & 1111 \\ \hline \end{array}$$

$$= 0100110101111111$$

(d)

$$128_{10} = ()_{16}$$

$$\frac{128}{16} = 8$$

$$\frac{8}{16} = 0.5 = 0.5 \times 16 = 8$$

8 Ans.

$$\begin{aligned} \textcircled{e} \quad 3A6F_{16} &= (\quad)_2 \\ 3A6F &= \overbrace{0011}^3 \overbrace{1010}^A \overbrace{0110}^6 \overbrace{1111}^F \\ &= 0011101001101111 \end{aligned}$$

$$\textcircled{f} \quad \overline{11000} 1100001111100101_2 = (\quad)_{16}$$

$$110001111100101$$

At first there is 1 digit less so we add one digit

$$\begin{array}{cccc} \overbrace{0110} & \overbrace{0011} & \overbrace{1110} & \overbrace{0101} \\ 6 & 3 & E & 5 \end{array}$$

$$63E5$$

$$\textcircled{g} \quad 6173_8 = (?)_{10}$$

$$6173_8 = (6 \times 8^3) + (1 \times 8^2) + (7 \times 8^1) + (3 \times 8^0)$$

$$= (6 \times 512) + (1 \times 64) + (7 \times 8) + (3 \times 1)$$

$$= 3072 + 64 + 56 + 3$$

$$= 3195_{10}$$

$$(h) 169_{10} = (?)_8$$

$$\frac{169}{8} = 21.125 \rightarrow 0.125 \times 8 = 1$$

$$\frac{21}{8} = 2.625 \rightarrow 0.625 \times 8 = 5$$

$$\frac{2}{8} = 0.25 \rightarrow 0.25 \times 8 = 2$$

$$\text{Ans: } (152)_8$$

$$(i) 2A7D_{16} = (?)_8$$

$$2A7D_{16}$$

$$= 2A7D$$

$$\begin{array}{cccc} \swarrow & \downarrow & \downarrow & \searrow \\ 2 & 10 & 7 & 13 \end{array}$$

$$0010 \quad 1010 \quad 0111 \quad 1101$$

$$001010100111101$$

if we add two zero for last one but we can take all zero so we neglect last zero

$$\begin{array}{cccccc} 010 & 101 & 001 & 111 & 101 & \\ \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \\ = 421 & 421 & 421 & 421 & 421 & \\ 2 & 5 & 1 & 7 & 5 & \end{array}$$

$$= (25175)_8$$

$$(j) \quad 11111111_2 = ?_{10}$$

(a) The bits & their powers-of-two weights for the positive number are as follows

Solution

2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
1	1	1	1	1	1	1	1

$$128 + 64 + 32 + 16 + 8 + 4 + 2 + 1 =$$

2's Complement is 255

Q 198 = ()_{BCD}

$$198 = \begin{matrix} 1 & 9 & 8 \\ 0001 & 1001 & 1000 \end{matrix}$$

Ans = 000110011000 BCD

M 100001110000_{BCD} = (?)₁₀

$$\begin{matrix} \underbrace{10000}_{8} & \underbrace{1110000}_{7} & \underbrace{0000}_{0} \end{matrix}$$

Ans: (870)₁₀

N 1001010₂ = (?)_{Gray}

$$\begin{matrix} 1 \rightarrow + & 0 \rightarrow + & 0 \rightarrow + & 1 \rightarrow + & 0 \rightarrow + & 1 \rightarrow + & 0 \rightarrow + \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 1 & 1 & 0 & 1 & 1 & 1 & 1 \end{matrix}$$

1101111 Gray

O ~~10101111~~ 10101111_{Gray} = (?)₂

$$\begin{matrix} 1 & & 0 & & 1 & & 0 & & 1 & & 1 & & 1 & & 1 \\ \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow & \downarrow \\ 1 & \times & 1 & \times & 0 & \times & 0 & \times & 1 & \times & 0 & \times & 1 & \times & 0 \end{matrix}$$

(11001010)₂

(P) 0100 0001 = (?) ASCII

		01000001	
Symbol =	Dec	Binary	Hex
1	33	01000001	21

(Q) 111000 = (?) 111000 Even Parity

Solution → Make the parity bit either 1 or 0 as necessary to make the total number of 1s even. The parity bit will be the left most bit.

111000

Even 1's

1111000 Even Parity

Q2. Calculate each of the following

(a) $01111111_2 - 00000111_2$
 $(01111111 + (-00000111))$

$$\begin{array}{r} 01111111 \\ + 00000111 \\ \hline 01111000 \end{array} \quad \text{2's complement } (-00000111)$$

01111000 Ans:-

(b) $01101010 \times 11110001_2$

$$\begin{array}{r} 01101010 \\ + 11110001 \\ \hline 01101010 \\ + 00000000 \\ \hline 001101010 \\ + 00000000 \\ \hline 0001101010 \\ + 00000000 \\ \hline 00001101010 \\ + 01101010 \\ \hline 011100001010 \\ + 01101010 \\ \hline 1010001001010 \\ + 10101010 \\ \hline 11010011001010 \\ + 01101010 \end{array}$$

2's complement

$$\begin{array}{r} 111100111001010 \\ 000011000110101 \end{array}$$

Now we attached Signed bit

$$\boxed{1000011000110101}$$

↓ Ans:-

$$\boxed{01111001100101}$$

(c) $10001000 \div 00100010_2$

Step 1: The sign of both numbers are positive, so the quotient will be positive. The quotient is initially zero: 00000000

Step 2: Subtract the Divisor from the dividend using 2's complement addition (final carries are discarded)

$$\begin{array}{r} 10001000 \text{ Dividend} \\ + 00100010 \text{ 2's complement of divisor} \\ \hline 10101010 \text{ Positive 1st partial remainder} \end{array}$$

Add 1 to quotient: $00000000 + 00000001 = 00000001$

Step 3: Subtract the divisor from the 1st partial remainder using 2's complement addition

$$\begin{array}{r} \cancel{01001011} \quad 10101010 \text{ 1st Partial remainder} \\ + \cancel{110011} \quad + 00100010 \text{ 2's complement of divisor} \\ \hline 10001000 \text{ Positive 2nd partial remainder} \end{array}$$

Add 1 to quotient: $00000001 + 00000001 = 00000010$

Step 4: Subtract the divisor from the 2nd partial remainder using 2's complement addition

$$\begin{array}{r} \cancel{0010010} \quad 10001000 \text{ 2nd Partial remainder} \\ + \cancel{110011} \quad + 00100010 \text{ 2's complement of divisor} \\ \hline 00000000 \text{ zero remainder} \end{array}$$

Add 1 to quotient: $00000010 + 00000001$

$= 00000011$ (final quotient)

The process is complete.

Q2 (e) $00010110_{BCD} + 00010101_{BCD} = (?)_{10}$

$$\begin{array}{r}
 00010110 \\
 + 00010101 \\
 \hline
 00101011
 \end{array}$$

$$\begin{array}{r}
 16 \\
 + 15 \\
 \hline
 31
 \end{array}$$

Right group
So this invalid BCD (>9)

00101011 left group is valid

+ 0110 Add 6 to invalid code. Add

$$\begin{array}{r}
 00101011 \\
 + 0110 \\
 \hline
 00110001 \\
 \hline
 3 \quad 1
 \end{array}$$

Carry, 0001, to next group.

Valid BCD number

QUESTION:3:

Q3- Apply CRC to the data bits 11010011_2 using the generator code 1010_2 to

Produce the transmitted CRC code.
 $G = 1010$

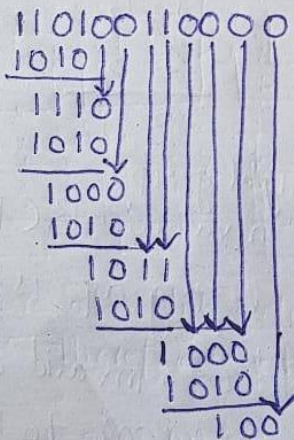
Solution-

Since the generator code has 4 bits, add four 0s to the data byte. The appended data (D') is

$$D' = 110100110000$$

Divide the appended data by the generator code using the modulo-2 operation until all bits have been used

$$\frac{D'}{G} = \frac{110100110000}{1010}$$



The transmitted CRC is 110100110100

Q4: Assume that the procedure in problem Q3 incurs an error in the most significant bit during transmission. Apply CRC to detect the error.

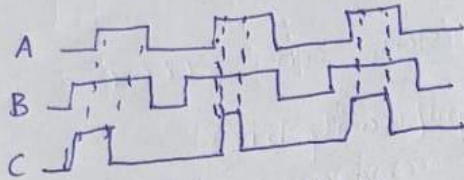
Solution - During Transmission, an error occurs in the most significant bit

Solution - Applying the CRC process to the received data to detect the error

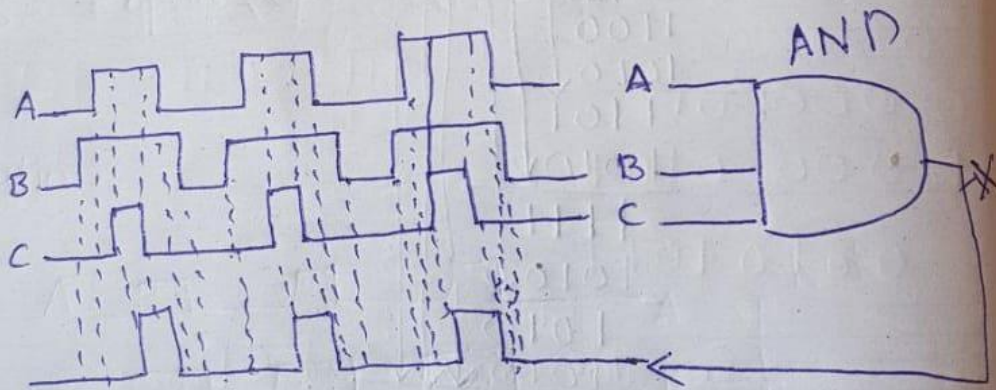
$$\begin{array}{r}
 100100110100 \\
 \underline{1010} \downarrow \\
 1100 \\
 \underline{1010} \downarrow \\
 1101 \\
 \underline{1010} \downarrow \\
 1111 \\
 \underline{1010} \downarrow \\
 1010 \\
 \underline{1010} \downarrow \downarrow \downarrow \\
 0100
 \end{array}$$

Remainder = 0100. Since it is not zero, an error is indicated.

Q5. The input wave forms in Figure 1 is applied to a 3 input AND gate. Show the output wave form in proper relation to the inputs with a timing diagram



Solution.. The Diagram show ~~suppose~~ that the all three inputs are high only

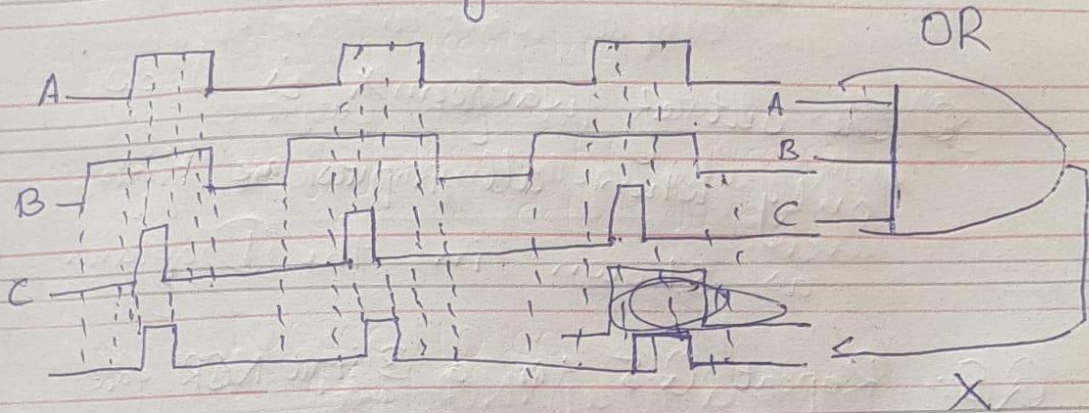


A, B & C are all High during of three intervals, therefore, X is High.

The output waveform X is High only when both A & B wave forms are High as shown in the above Diagram

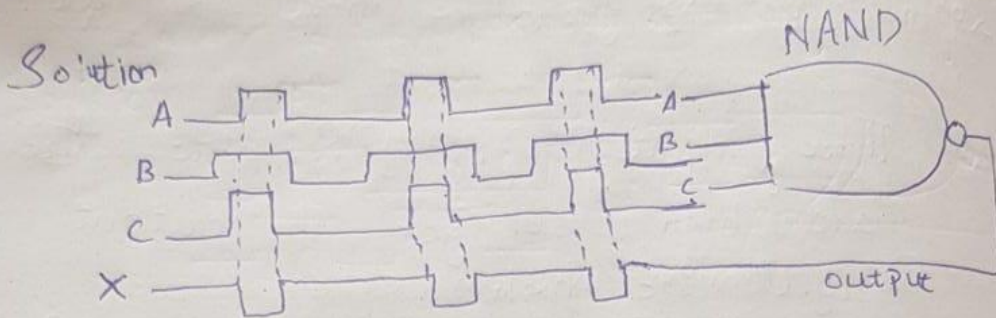
Q6. Repeat Q5 for a 3 input OR gate

Solution: Three inputs for OR gate ~~the~~ are high so for the output will be high



The output waveform of a 3 input OR gate is high when either one are all high.

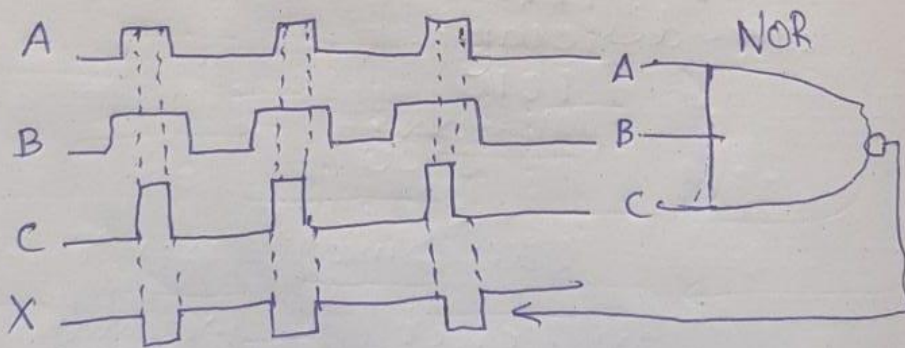
Q7: Repeat Q.5 for 3 input NAND gate



The output waveform X is Low only when all inputs are High as shown in the Diagram

Q8: Repeat Q.5 for a 3 input NOR gate

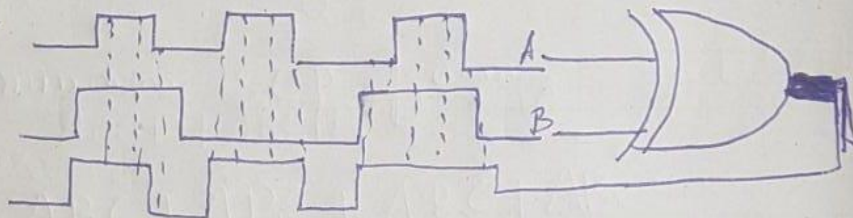
Solution



The output X is Low when any input is High as shown by the output waveform X in the timing diagram

Q9:- The input waveforms in Figure 2 is applied to a XOR gate. Show the output waveform in proper relation to the inputs with a timing diagram.

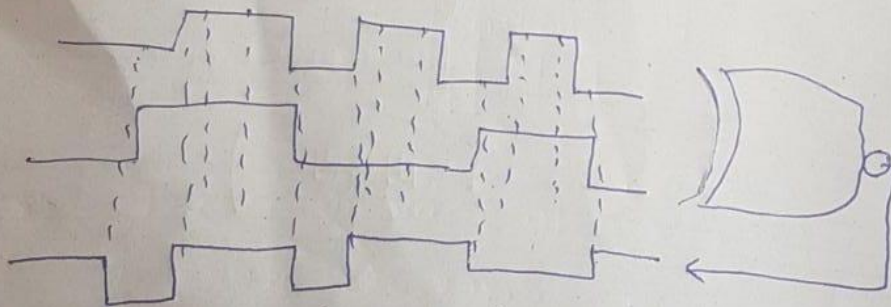
Solution:-



The output waveforms are shown
Notice that the XOR output is High only when both inputs are at opposite levels.

Q10:- Repeat Q.9 for XNOR gate.

Solution



The XNOR output is High only when both inputs are the same level

Q2. Convert the following expressions into Standard SOP forms $(C+D)(A'+D)$

$$= ABCD + ABC(D+D') + (A'+A)BCD + ABC(D+D')$$

$$= ABCD + ABCD + ABCD' + (A'B'CD + ABCD)$$

$$\leftarrow ABCD + ABCD'$$

$$= \underset{m_{15}}{1111} + \underset{m_{15}}{1111} + \underset{m_{14}}{1110} + \underset{m_7}{1101} + \underset{m_{15}}{1111} + \underset{m_{15}}{1111} + \underset{m_{15}}{1111}$$

Solve with 8421

$$ABCD = 1111$$

$$= ABCD' = 1110$$

$$A'B'CD = 0111$$

$$= m_{15} + m_{14} + m_7$$

$$= \sum (m_{15}, 14, 7) \text{ Ans.}$$

Q15 :- Use a Karnaugh map to simplify the following expression to a minimum SOP form

$$\bar{A}\bar{B}\bar{C} + \bar{A}BC + A\bar{B}C + ABC$$

Solution

C \ AB	00	01	11	10
0	1		1	
1		1		1

