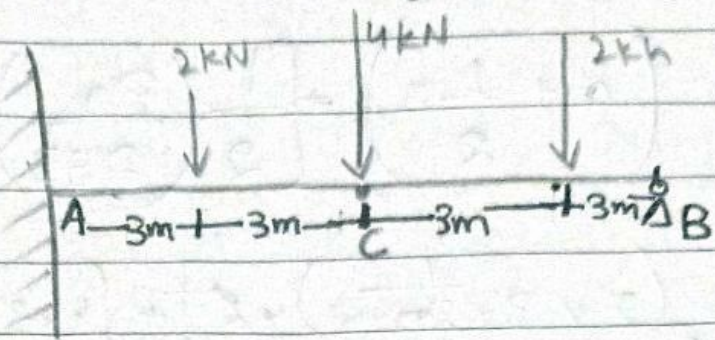


Determine the slope at A and displacement at C of the beam in figure



By Moment Area Theorem \Rightarrow
 Take $E = 200 \text{ GPa}$
 $I = 6(10^6) \text{ mm}^4$

Solution :-

Slope (A) $\Rightarrow ?$ displacement (C) $\Rightarrow ?$

As

$$\frac{1}{2} \left(\frac{Pa}{EI} \right)$$

$$\theta_{AC} = \frac{1}{2} \left(\frac{4 \times 3}{200 \times 10^9 \times 6 \times 10^{-5}} \right)^3 + \left(\frac{4 \times 3}{200 \times 10^9 \times 6 \times 10^{-5}} \right) \times 3$$

$$+ \frac{1}{2} \left(\frac{2 \times 3}{2 \times 200 \times 10^9 \times 6 \times 10^{-5}} \right)$$

$$\theta_{AC} = \frac{1}{200 \times 10^3} \left[\left(\frac{3(4 \times 3)}{2} \right) + (12 \times 3) + \frac{3}{2} \left(\frac{6}{2} \right) \times 3 \right]$$

$$\theta_{AC} = 0.00002925$$

$$t_{BC} = \left[\frac{1}{2} \left(\frac{Pa}{EI} \right) a \right] \left(\frac{2}{3} a \right) + \left[\frac{Pa}{EI} (a) \right]$$

$$\left(a + \frac{1}{2} a \right) + \left[\frac{1}{2} \left(\frac{Pa}{EI} \right) a \right] \left[\frac{a + \frac{2}{3} a}{3} \right]$$

$$t_{BC} = \left[\frac{3}{2} \left(2 \times 3 \times \frac{1}{200 \times 10^4} \right) \times 2 \right] + \left[\frac{4 \times 3 \times 3 \times 1}{200 \times 10^4} \right]$$

$$* \left(3 + \frac{3}{2} \right) + \frac{3}{2} \left(\frac{2 \times 3}{2} \times \frac{1}{200 \times 10^4} \right) \times (3 + 9)$$

$$t_{BC} = 9 \times 10^{-6} * 8.1 \times 10^{-5} + 1.125 \times 10^{-5}$$

$$t_{BC} = 1.0125 \times 10^{-4}$$

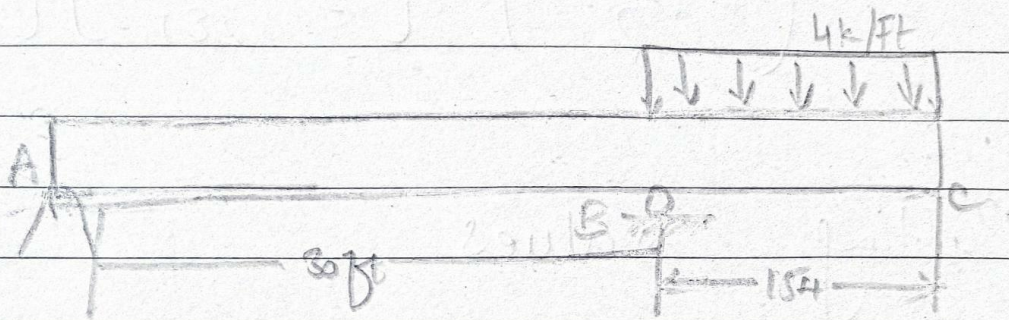
OR

$$t_{BC} = 0.00010125$$



Question 1:

Determine the slope and displacement at C. EI is constant. Use the moment area theorem.



Solution:

Slope and displacement at C = ?

As

$$\Delta = \frac{1}{2} (Pa / EI)$$

$$\theta_{AC} = \frac{1}{2} \left(\frac{4 \times 30}{200 \times 10^6 \times 6 \times 10^{-5}} \right)^3 + \left(\frac{4 \times 30}{200 \times 10^6 \times 6 \times 10^{-5}} \right) \times 3$$

$$\frac{1}{2} = \left[\frac{2 \times 30}{2 \times 200 \times 10^6 \times 6 \times 10^{-5}} \right]$$

$$\theta_{AC} = \frac{1}{200 \times 10^6} \left[\frac{30}{2} (4 \times 30) + (12 \times 3) + \frac{30}{2} \left(\frac{6}{2} \right) \times 3 \right]$$

$$\Delta A_c = \boxed{0.0001285}$$

$$t_{BC} = \left[\frac{1}{2} \left(\frac{P_0}{EI} \right) a \right] \left(\frac{2}{3} \right) + \frac{P_0(a)}{CI}$$

$$\left(a + \frac{1}{2} a \right) + \left[\frac{1}{2} \frac{P_0 a}{2EI} \right] \left[\frac{a+2}{3} \right]$$

Putting values

$$t_{BC} = \left[\frac{4}{15} \left(\frac{2 \times 3 \times 1}{200 \times 10^4} \right) \times 15 \right] \left[\frac{4 \times 3 \times 3}{200 \times 10^4} \right]$$

$$\times \left(3 + \frac{3}{15} \right) + \frac{3}{15} \left(\frac{15 \times 3 \times 1}{4 \times 200 \times 10^4} \right) (3 + 15)$$

$$t_{BC} = \boxed{0.000143}$$