

Name : Alam Zeb

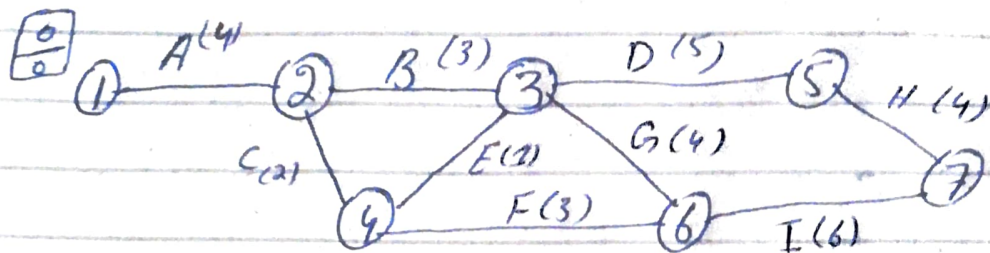
I.D : 14481

Section : BS (SE-4) (A)

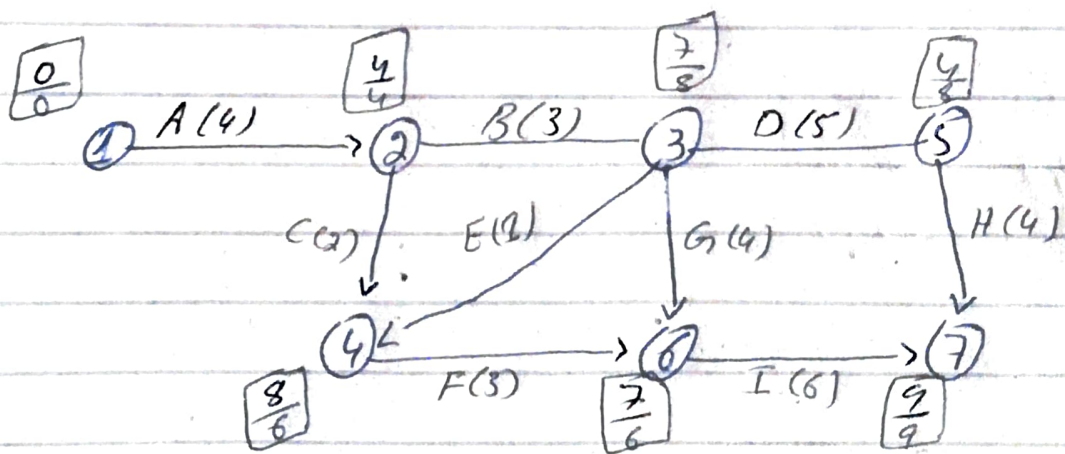
Subject : Operation Research

Q1. Answer.

a) Calculate the CPM network



b) Determine the critical path and Project completion time



we know that

$$E_{sj} = \max (E_{si} + D_{ij})$$

$$\text{for Node 1} = E_{S1} = 0$$

$$\text{Node 2} = 0 + 4 = 4$$

$$\text{Node 3} = 4 + 3 = 7$$

$$\text{Node 4} = 3 + 1 = 4$$

$$\text{Node 5} = 3 + 5 = 8$$

$$\text{Node 6} = 3 + 4 = 7$$

$$\text{Node 7} = 5 + 4 = 9$$

(C) Compute total floats and free floats for non-critical activities

$TF = LF - EF$ Finish

$TF = L_s - E_s$ Start

$TF = 0$

0	A	4
0	4	4

4	B	7
5	3	8

22	F	21
23	3	21

8	0	12
8	5	12

5	C	8
5	2	8

13	E	15
16	1	15

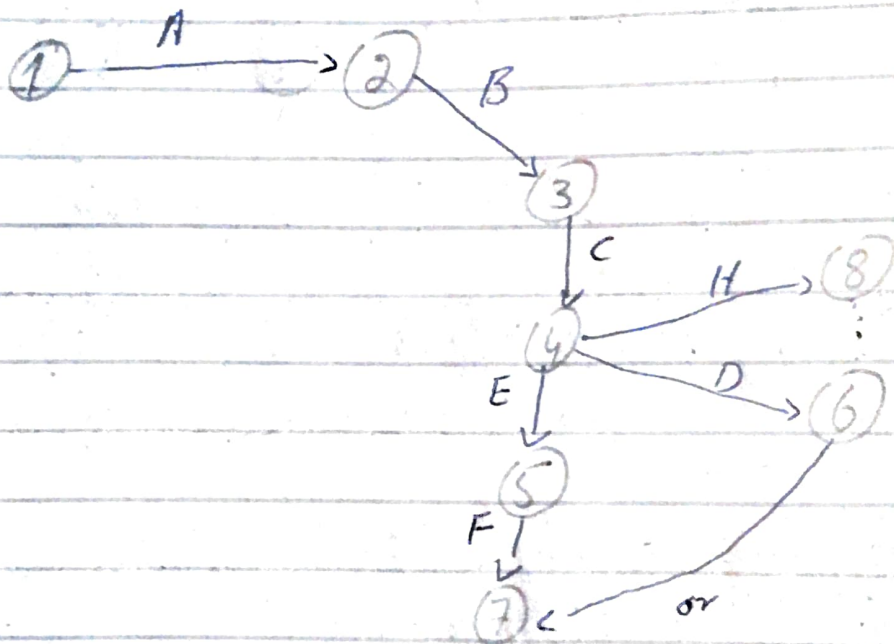
19	6	17
19	4	17

28	11	23
25	4	23

32	1	26
3	6	26

Question 2

a) Solution



b) Solution:

By formula

$$\text{(Mean) } te_1 = \frac{t_o + 4t_m + t_p}{6}$$

$$= \frac{4 + 4(5) + 12}{6} = \frac{4 + 20 + 12}{6} = 6$$

$$te_2 = \frac{2 + 4(3) + 4}{6} = \frac{2 + 12 + 4}{6} = 3$$

$$te_3 = \frac{6 + 4(8) + 22}{6} = \frac{6 + 32 + 22}{6} = 10$$

$$t_{e4} = \frac{4 + 4(6) + 8}{6} = \frac{4 + 24 + 8}{6} = 6$$

$$t_{e5} = \frac{3 + 4(4) + 5}{6} = \frac{3 + 16 + 5}{6} = 4$$

$$t_{e6} = \frac{2 + 4(4) + 6}{6} = \frac{2 + 16 + 6}{6} = 4$$

$$t_{e7} = \frac{2 + 4(3) + 4}{6} = \frac{2 + 12 + 4}{6} = 3$$

$$t_{e8} = \frac{5 + 4(7) + 15}{6} = \frac{5 + 28 + 15}{6} = 8$$

Variance (σ^2):

By formula

$$\sigma^2 = \left(\frac{t_p - t_0}{6} \right)^2$$

$$\sigma_1^2 = \left(\frac{12 - 4}{6} \right)^2 = \left(\frac{8}{6} \right)^2 = (1.33)^2 = 1.77$$

$$\sigma_2^2 = \left(\frac{4 - 2}{6} \right)^2 = \left(\frac{2}{6} \right)^2 = 0.11$$

$$\sigma_3^2 = \left(\frac{22 - 6}{6} \right)^2 = \left(\frac{16}{6} \right)^2 = 7.09$$

$$\sigma_4^2 = \left(\frac{8 - 4}{6} \right)^2 = \left(\frac{4}{6} \right)^2 = 0.44$$

$$\sigma_5^2 = \left(\frac{5 - 3}{6} \right)^2 = \left(\frac{2}{6} \right)^2 = 0.11$$

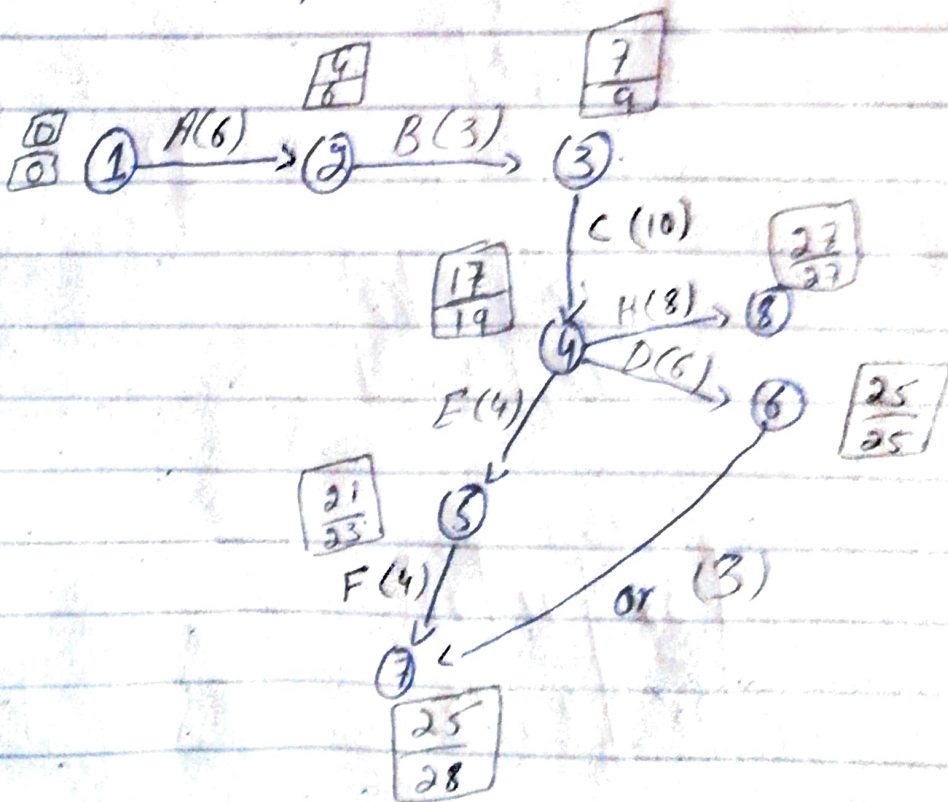
$$\sigma_6^2 = \left(\frac{6 - 2}{6} \right)^2 = \left(\frac{4}{6} \right)^2 = 0.44$$

$$\sigma_7^2 = \left(\frac{4-2}{6}\right)^2 = \left(\frac{2}{6}\right)^2 = 0.11$$

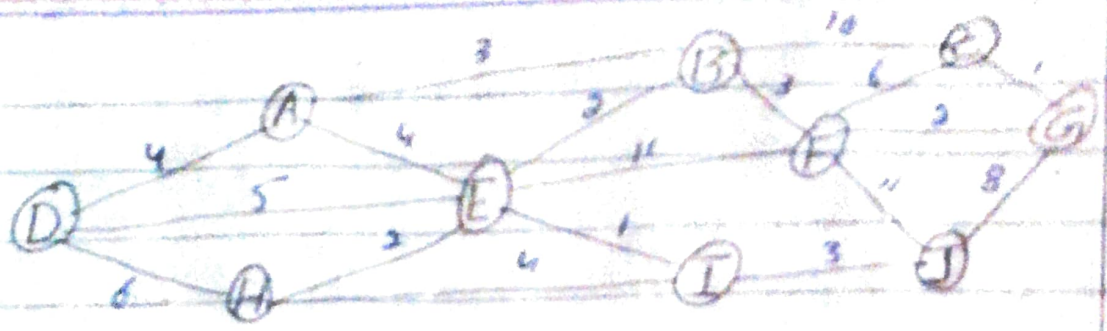
$$\sigma_8^2 = \left(\frac{15-5}{6}\right)^2 = \left(\frac{10}{6}\right)^2 = 2.76$$

c) Find the critical path and expected project completion time.

Critical path



Q3

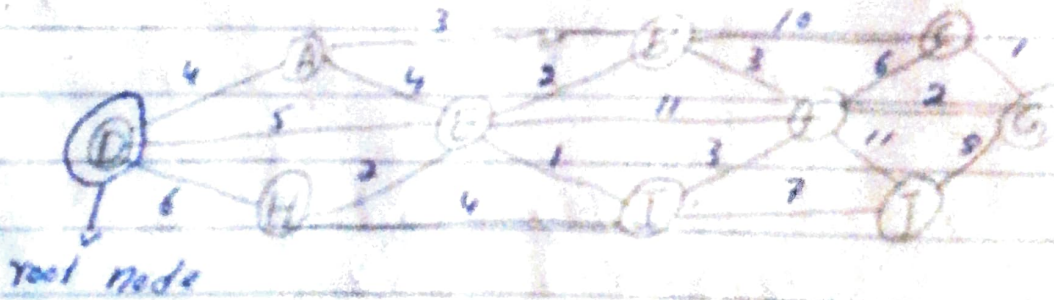


Step 1:

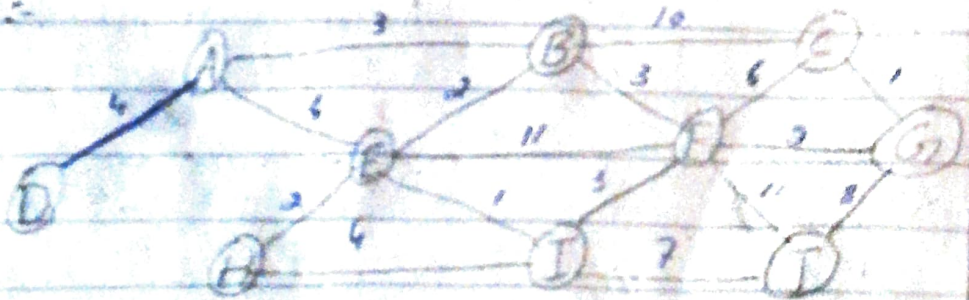
Removing all loops and parallel edges

Step 2:

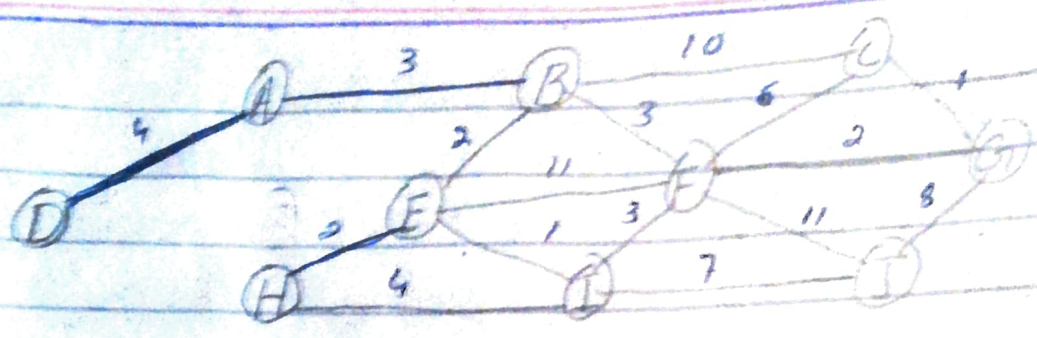
Choosing arbitrary node as root node



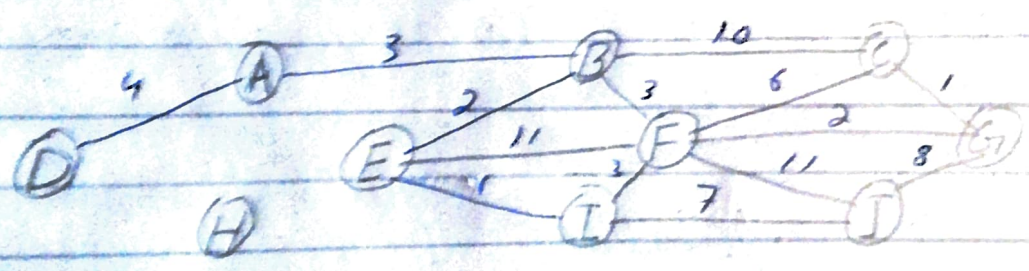
Step 3:



Now the tree D-A is treated as one node and we are checking for all edges.

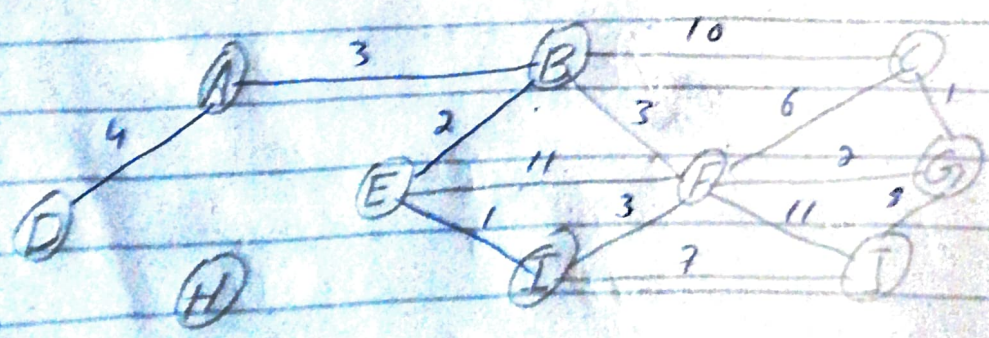


after this step D-4-A-3 tree is formed now we will again traverse it as a node and will check the edges again



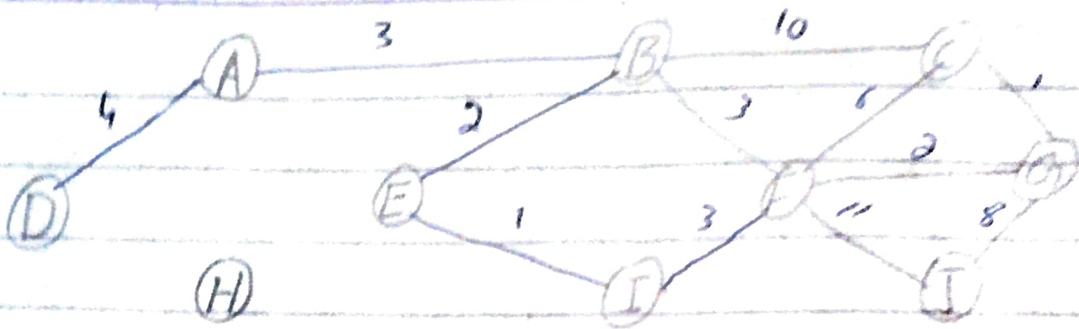
after adding Node E
D-4-A-3-B-2

Now



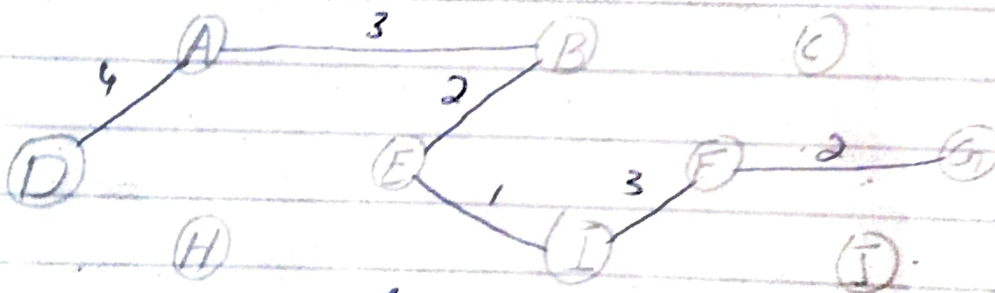
After adding root (E)
D-4-A-3-E-2-I-1

Now



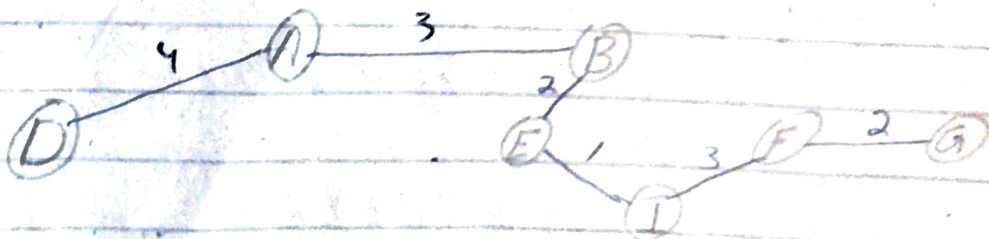
Now after adding root (F)
 $D-4-A-3-E-2-I-1-F-3$

Now



Now we find that the output Spanning tree of the graph using two different algorithm is same

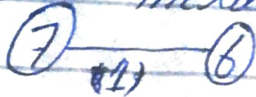
$$4 + 3 + 2 + 1 + 3 + 2 = 15$$



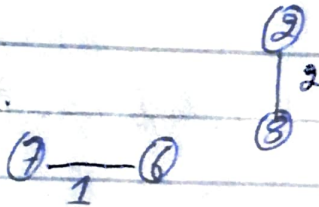
Q4. For the following graph find the minimum spanning tree using Kruskal's algorithm.

Sol.

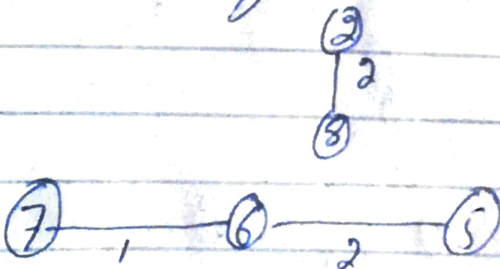
1) Formed include



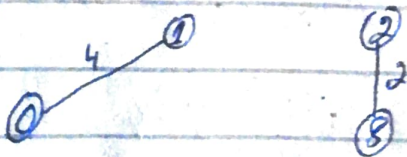
2) Picking edge 8-2: No cycle is formed include it



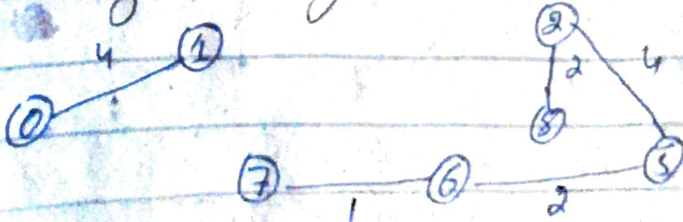
3) Picking edge 6-5: again no cycle is forming including it



4) edge 0-1

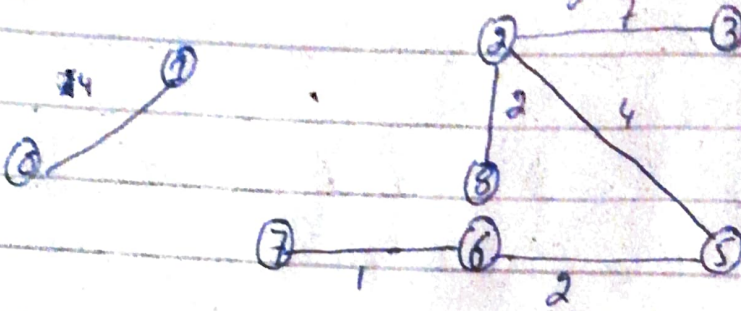


5) Picking edge 2-5



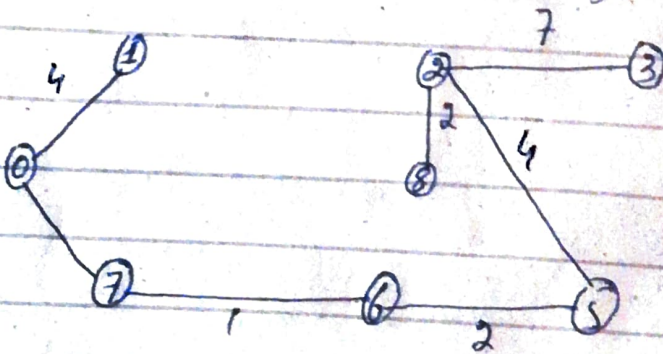
6) edge 8-6 including this edge results into cycle

7) edge 2-3 No cycle



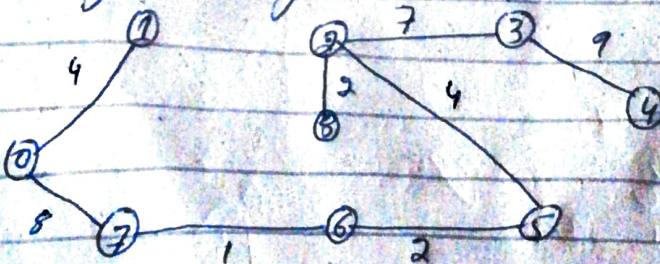
8) edge 7-8 including this edge results into cycle.

9) edge 0-7 No cycle forming



10) Picking this edge 1-2 including this edge results into cycle.

11) Picking edge 3-4



Since the number of edge included equals the algorithm stop here

Q5 Write a detailed note on how this course (Operations Research) will help you in your professional life?

Ans. Def.:

It is the method of analysis by which management receives aid for their decisions. Though the name of this method operation Research (O.R) is relatively new. The subject of operation was born during Second World War in U.K, and was used for military strategy. During World War II a group of scientists having representatives from mathematics, statistics, physical and social science were entrusted to the study of various military operations.

In life it can be used for solving different types of problems.

Such as:

- i) Problems dealing with the waiting line, the arrival of units or persons requiring service.
- ii) Problems dealing with the allocation of material or activities among limited facilities.

- iii) Equipment replacement Problems
 iv) Problems dealing with production processing i.e. production control and material shipment.

In the more wide sense, operation Research does not deal with the everyday problems such as output by the one worker or machine capacity; instead it is concerned with the overall aspect of business, operation such as Somethings as the relationship b/w inventory sales, production and Scheduling. It may also deal with the overall flow of goods and services from plants to consumers.

The main objective of operation research is to be providing better quantitative information's for making decision. Now our aim is to learn how we can have better decision.

Scope of operation Research:

In its recent years of organised development, O.R has solved successfully many cases of research for military, the government and industry.

Some of problems which can be analysed by operations research:

- i) Finance, Budgeting and Investment
- ii) Cash Flow, Long range Capital requirement, investment portfolios, dividend policies
- iii) Claims procedure, and
- iv) Credit policies
- v) Marketing
 - i) Product Selection, competitive actions
 - ii) Number of Salesman, frequencies of calling on and
 - iii) Advertising strategies with respect to cost and time.

Application of operation Research:

- i) Distribution or Transportation problems
- ii) Product mix
- iii) Production planning
- iv) Assignment of personnel
- v) Agricultural production.
- vi) Financial Application.