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Section B

Deptt BE (C)

Semester 4th

Assignment Column and beam

Subject Structure Analysis

Submitted to Engr. Amjad Islam

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Question No. 1

Determine the slope at point C. Use the moment-area theorem.

Given data:



Required data:

We have to find the slope.

Solution:

As we know that

$$\sum MA = 0 \quad + \curvearrowright$$

$$\Rightarrow (F_B \times 30) - (60 \times 37.5) = 0$$

$$\Rightarrow \boxed{F_B = 75 \text{ k}}$$

Now:

$$\sum F_y = 0 \quad + \uparrow$$

$$\Rightarrow F_A + 75 \text{ k} - 60 \text{ k} = 0$$

$$\Rightarrow \boxed{F_A = -15 \text{ k}}$$

Now

$$\theta_{C/A} = \frac{1}{2} \left(\frac{-750 \text{ k} \cdot \text{ft}}{EI} \right) (45 \text{ ft}) = \frac{33750 \text{ k} \cdot \text{ft}^2}{2EI}$$

$$= \frac{16875 \text{ k} \cdot \text{ft}^2}{EI}$$

$$t_D = \theta_A + \theta_{L/A}$$

$$\theta_L = \frac{-3750 \text{ k}\cdot\text{ft}^2}{EI} + \frac{16875 \text{ k}\cdot\text{ft}^2}{EI}$$

$$\Rightarrow \theta_L = \frac{13125 \text{ k}\cdot\text{ft}^2}{EI}$$

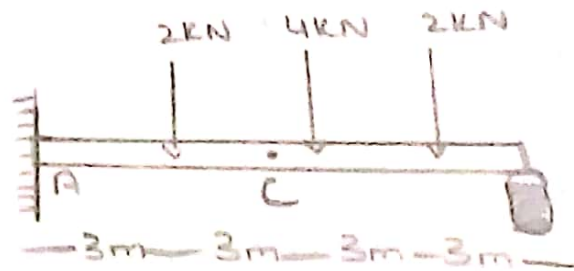
$$\theta_D = |t_{L/A}| \rightarrow \theta' = \frac{337500 \text{ k}\cdot\text{ft}^3}{EI} - \frac{168750 \text{ k}\cdot\text{ft}^3}{EI}$$

$$\theta_D = \frac{168750 \text{ k}\cdot\text{ft}^3}{EI}$$

Question No. 2

Determine the slope at point ----- take $E = 200 \text{ GPa}$, $I = 6 \times 10^6 \text{ mm}^4$

Given data:



$$E = 200 \text{ GPa}$$

$$I = 6 \times 10^6 \text{ mm}^4$$

$$|t_{B/A}| = \left[\frac{1}{2} \left(\frac{750 \text{ k}\cdot\text{ft}}{EI} \right) 30 \text{ ft} \right] \left[\frac{1}{3} (30 \text{ ft}) \right]$$

$$= \frac{112500 \text{ k}\cdot\text{ft}^3}{EI}$$

$$|t_{C/A}| = \left[\frac{1}{2} \left(\frac{750 \text{ k}\cdot\text{ft}}{EI} \right) 30 \text{ ft} \right] \left[15 \text{ ft} + \frac{1}{3} (30 \text{ ft}) \right]$$

$$+ \left[\frac{1}{2} \left(\frac{750 \text{ k}\cdot\text{ft}}{EI} \right) (4.5 \text{ ft}) \right] \left[\frac{2}{3} (15 \text{ ft}) \right]$$

$$= \frac{281250 \text{ k} \cdot \text{ft}^3}{EI} + \frac{56250 \text{ k} \cdot \text{ft}^3}{EI} \Rightarrow \frac{337500 \text{ k} \cdot \text{ft}^3}{EI}$$

Then

$$\begin{aligned} \theta' &= \frac{45}{30} (t_{B/A}) \\ &= \frac{45}{30} \left(\frac{112500 \text{ k} \cdot \text{ft}^3}{EI} \right) \\ &= \frac{168750 \text{ k} \cdot \text{ft}^3}{EI} \end{aligned}$$

$$\begin{aligned} \theta_A &= \frac{t_{B/A}}{AB} = \frac{112500}{30 \text{ ft}} / EI \\ &= \frac{3750 \text{ k} \cdot \text{ft}^2}{EI} \end{aligned}$$

Solution:

$$\theta_{A/C} = \frac{1}{2} \left(\frac{12}{EI} \times 3 \right) + \left(\frac{12}{EI} \times 3 \right) + \frac{1}{2} \left(\frac{6}{EI} \times 3 \right)$$

$$\Rightarrow \theta_{A/C} = \frac{63}{EI}$$

$$\theta_{A/C} = \frac{63}{(200 \times 10^6)(6 \times 10^6)(1/1000)^4}$$

$$\Rightarrow \theta_{A/C} = 0.0525 \text{ radians}$$

$$\begin{aligned} t_{A/C} &= \frac{1}{2} \left(\frac{12}{EI} \times 3 \right) \left(\frac{2 \times 3}{3} \right) + \left(\frac{12}{EI} \times 3 \right) \left(3 + \frac{1}{2} \times 3 \right) \\ &\quad + \frac{1}{2} \left(\frac{6}{EI} \times 3 \right) \left(3 + \frac{2}{3} \times 3 \right) \end{aligned}$$

$$t_{A/C} = 0.202 \text{ m}$$

$$\theta_C = t_{A/C} = 0.202 \text{ m}$$

$$| \text{OL} = 202 \text{ mm} |$$

Result:

$$\text{OL} = 202 \text{ mm.}$$