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#### Abstract

Modern Technology like Wi-Fi community helps us to connect right away with humans somewhere and at any time. Security of Wireless network is the predominant undertaking confronted by way of today's world. It is the place cryptography play a fundamental position to provide protection to the wireless network. Numerous encryption calculations are on hand to tightly close the information. This paper offers with normally utilized symmetric encryption calculation which is DES Algorithm. Test effects are given to illustrate the execution of this calculation.


## Introduction

Cryptography is an artwork of conveying messages in coded shape which is understood totally via the supposed recipient. The recipient in flip decodes to have a look at the message. The swap of records by way of public community with safety problems can be protected with cryptography. There are numerous popular symmetric and uneven algorithms which are fantastically secured and time tested.

## Types of Cryptography:

## DES:

The Data Encryption Standard (DES) is a symmetric-key block cipher published by the National Institute of Standards and Technology (NIST).
DES is an implementation of a Feistel Cipher. It uses 16 round Feistel structure. The block size is 64 -bit. Though, key length is 64-bit, DES has an effective key length of 56 bits, since 8 of the 64 bits of the key are not used by the encryption algorithm (function as check bits only)

## TDES:

Triple DES (aka 3DES, 3-DES, TDES) is based on the DES (Data Encryption Standard) algorithm, therefore it is very easy to modify existing software to use Triple DES. It also has the advantage of proven reliability and a longer key length that eliminates many of the attacks that can be used to reduce the amount of time it takes to break DES. However, even this more powerful version of DES may not be strong enough to protect data for very much longer (due in particular to the small block size). As such, the DES algorithm itself has become obsolete and is no longer used.


#### Abstract

AES: The more popular and widely adopted symmetric encryption algorithm likely to be encountered nowadays is the Advanced Encryption Standard (AES). It is found at least six time faster than triple DES. A replacement for DES was needed as its key size was too small. With increasing computing power, it was considered vulnerable against exhaustive key search attack. Triple DES was designed to overcome this drawback but it was found slow. The features of AES are as follows - - Symmetric key symmetric block cipher - 128-bit data, 128/192/256-bit keys - Stronger and faster than Triple-DES - Provide full specification and design details - Software implementable in C and Java


## Blowfish:

Blowfish is an encryption algorithm that can be used as a replacement for the DES or IDEA algorithms. It is a symmetric (that is, a secret or private key) block cipher that uses a variable-length key, from 32 bits to 448 bits, making it useful for both domestic and exportable use.

## RSA (Rivest-Shamir-Adleman)

Is one of the first public-key cryptosystems and is widely used for secure data transmission. In such a cryptosystem, the encryption key is public and distinct from the decryption key which is kept secret (private). In RSA, this asymmetry is based on the practical difficulty of factoring the product of two large prime numbers, the "factoring problem". The acronym RSA is the initial letters of the surnames of Ron Rivest, Adi Shamir, and Leonard Adleman, who publicly described the algorithm in 1977. Clifford Cocks, an English mathematician working for the British intelligence agency Government Communications Headquarters (GCHQ), had developed an equivalent system in 1973, which was not declassified until 1997.

### 3.1 DATA ENCRYPTION STANDARD

The DES has the following steps involved.
a. 64 bit plain text is taken as input and initial permutation is done on the input by re-arranging the bits to get the permuted input.
b. The next step involves 16 rounds of the same function along with permutation and substitution.
c. The $16^{t} h$ output contains 64 bits as a result of function of input plain text and key.
d. The output of left and right side are swapped producing thepreoutis.
e. The preoutis have gone through IP, i.e. Opposite of initial
f. Permutation to produce 64 bit cipher text.

> SINGLE ROUND DES


## Key Transformation:

We have noted initial 64-bit key is transformed into a 56-bit key by discarding every 8th bit of the initial key. Thus, for each a 56 -bit key is available. From this 56 -bit key, a different 48 -bit Sub Key is generated during each round using a process called as key transformation. For this the 56 bit key is divided into two halves, each of 28 bits. These halves are circularly shifted left by one or two positions, depending on the round.
For example, if the round number $1,2,9$ or 16 the shift is done by only position for other rounds, the circular shift is done by two positions. The number of key bits shifted per round is show in figure.

| Round | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| \#key bits <br> shifted | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |

Figure - number of key bits shifted per round

## Step-2: Expansion Permutation

Recall that after initial permutation, we had two 32-bit plain text areas called as Left Plain Text (LPT) and Right Plain Text (RPT). During the expansion permutation, the RPT is expanded from 32 bits to 48 bits. Bits are permuted as well hence called as expansion permutation. This happens as the 32 bit RPT is divided into 8 blocks, with each block consisting of 4 bits. Then, each 4 bit block of the previous step is then expanded to a corresponding 6 bit block, i.e., per 4 bit block, 2 more bits are added.


## S-box (substitution-box)

Is a basic component of symmetric key algorithms which performs substitution In block ciphers, they are typically used to obscure the relationship between the key and the cipher text - Shannon's property of confusion.
In general, an S-box takes some number of input bits, $m$, and transforms them into some number of output bits, $n$, where $n$ is not necessarily equal to $m .{ }^{[1]} \mathrm{An} m \times n$ S-box can be implemented as a lookup table with $2^{m}$ words of $n$ bits each. Fixed tables are normally used, as in the Data Encryption Standard (DES), but in some ciphers the tables are generated dynamically from the key (e.g. the Blowfish and the Twofish encryption algorithms).


Is a method of bit-shuffling used to permute or transpose bits across S-boxes inputs, retaining diffusion while transposing.
In block ciphers, the S-boxes and P-boxes are used to make the relation between the plaintext and the cipher text difficult to understand (see Shannon's property of confusion). P-boxes are typically classified as compression, expansion, and straight, depending on whether the number of output bits is less than, greater than, or equal to the number of input bits. Only straight P-boxes are invertible.

## P- box Permutation

Straight permutation:
Each input bit is moved to a new position in the output


> Rearrangement used in DES

| Bits | Goes to position |  |  |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $1-8$ | 9 | 17 | 23 | 31 | 13 | 28 | 2 | 18 |
| $9-16$ | 24 | 16 | 30 | 6 | 26 | 20 | 10 | 1 |
| $17-24$ | 8 | 14 | 25 | 3 | 4 | 29 | 11 | 19 |
| $25-32$ | 32 | 12 | 22 | 7 | 5 | 27 | 15 | 21 |

## XOR (Whitener).

After the expansion permutation, DES does XOR operation on the expanded right section and the round key. The round key is used only in this operation.


### 3.2 DES-Feistel Function:

## Ans:

## Encryption Process:

The encryption process uses the Feistel structure consisting multiple rounds of processing of the plaintext, each round consisting of a "substitution" step followed by a permutation step.

Feistel Structure is shown in the following illustration.


- The input block to each round is divided into two halves that can be denoted as $L$ and $R$ for the left half and the right half.
- In each round, the right half of the block, R, goes through unchanged. But the left half, L, goes through an operation that depends on R and the encryption key. First, we apply an encrypting function ' $f$ ' that takes two input - the key $K$ and $R$. The function produces the output $f(R, K)$. Then, we XOR the output of the mathematical function with L .
- In real implementation of the Feistel Cipher, such as DES, instead of using the whole encryption key during each round, a round-dependent key (a sub key) is derived from the encryption key. This means that each round uses a different key, although all these sub keys are related to the original key.
- The permutation step at the end of each round swaps the modified $L$ and unmodified $R$. Therefore, the $L$ for the next round would be R of the current round. And R for the next round be the output L of the current round.
- Above substitution and permutation steps form a 'round'. The numbers of rounds are specified by the algorithm design.
- Once the last round is completed then the two sub blocks, ' $R$ ' and ' $L$ ' are concatenated in this order to form the cipher text block.

The difficult part of designing a Feistel Cipher is selection of round function ' f '. In order to be unbreakable scheme, this function needs to have several important properties that are beyond the scope of our discussion.

## Decryption Process

The process of decryption in Feistel cipher is almost similar. Instead of starting with a block of plaintext, the cipher text block is fed into the start of the Feistel structure and then the process thereafter is exactly the same as described in the given illustration.
The process is said to be almost similar and not exactly same. In the case of decryption, the only difference is that the sub keys used in encryption are used in the reverse order.
The final swapping of ' L ' and ' $R$ ' in last step of the Feistel Cipher is essential. If these are not swapped then the resulting cipher text could not be decrypted using the same algorithm.

## 3 (3.2)

The F-function, depicted in Figure 4, operates on half a block (32 bits) at a time and consists of four stages:


Figure 4:

1. Expansion: the 32 -bit half-block is expanded to 48 bits using the expansion permutation, denoted E in the diagram, by duplicating half of the bits. The output consists of eight 6 -bit ( $8 \times 6=48$ bits) pieces, each containing a copy of 4 corresponding input bits, plus a copy of the immediately adjacent bit from each of the input pieces to either side.
2. Key mixing: the result is combined with a sub key using an XOR operation. Sixteen 48-bit sub keys-one for each round-are derived from the main key using the key schedule (described below).
3. Substitution: after mixing in the sub key, the block is divided into eight 6-bit pieces before processing by the S-boxes, or substitution boxes. Each of the eight $S$-boxes replaces its six input bits with four output bits according to a non-linear transformation, provided in the form of a lookup table. The S-boxes provide the core of the security of DES-without them, the cipher would be linear, and trivially breakable.
4. Permutation: finally, the 32 outputs from the $S$-boxes are rearranged according to a fixed permutation, the P-box. This is designed so that, after permutation, the bits from the output of each S -box in this round are spread across four different $S$-boxes in the next round.

The alternation of substitution from the S -boxes, and permutation of bits from the P -box and E-expansion provides so-called "confusion and diffusion" respectively, a concept identified by Claude Shannon in the 1940s as a necessary condition for a secure yet practical cipher.

## Key-Schedule:



Figure 5:

Figure 5 illustrates the key schedule for encryption-the algorithm which generates the subkeys. Initially, 56 bits of the key are selected from the initial 64 by Permuted Choice 1 (PC-1)-the remaining eight bits are either discarded or used as parity check bits. The 56 bits are then divided into two 28-bit halves; each half is thereafter treated separately. In successive rounds, both halves are rotated left by one and two bits (specified for each round), and then 48 sub key bits are selected by Permuted Choice 2 (PC-2)-24 bits from the left half, and 24 from the right. The rotations (denoted by " $\lll$ " in the diagram) mean that a different set of bits is used in each sub key; each bit is used in approximately 14 out of the 16 subkeys.

The key schedule for decryption is similar-the subkeys are in reverse order compared to encryption. Apart from that change, the process is the same as for encryption. The same 28 bits are passed to all rotation boxes.

## 3.4: Initial Permutation

It is done on every block of input data in the beginning stage of encryption.

| 58 | 50 | 42 | 34 | 26 | 18 | 10 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 60 | 52 | 44 | 36 | 28 | 20 | 12 | 4 |
| 62 | 54 | 46 | 38 | 30 | 22 | 14 | 6 |
| 64 | 56 | 48 | 40 | 32 | 24 | 16 | 8 |
| 57 | 49 | 41 | 33 | 25 | 17 | 9 | 1 |
| 59 | 51 | 43 | 35 | 27 | 19 | 11 | 3 |
| 61 | 53 | 45 | 37 | 29 | 21 | 13 | 5 |
| 63 | 55 | 47 | 39 | 31 | 23 | 15 | 7 |

## Answer:

There is an initial permutation IP of the 64 bits of the message data $\mathbf{M}$. This rearranges the bits according to the following table, where the entries in the table show the new arrangement of the bits from their initial order. The 58th bit of $\mathbf{M}$ becomes the first bit of IP. The 50th bit of $\mathbf{M}$ becomes the second bit of IP. The 7th bit of $\mathbf{M}$ is the last bit of IP.
Example: Applying the initial permutation to the block of text $\mathbf{M}$, given previously, we get
$\mathbf{M}=0000000100100011010001010110011110001001101010111100110111101111$
$\mathbf{I P}=1100110000000000110011001111111111110000101010101111000010101010$
Here the 58th bit of $\mathbf{M}$ is " 1 ", which becomes the first bit of IP. The 50 th bit of $\mathbf{M}$ is " 1 ", which becomes the second bit of IP. The 7th bit of $\mathbf{M}$ is " 0 ", which becomes the last bit of IP.
Next divide the permuted block IP into a left half $\mathbf{L}_{\mathbf{0}}$ of 32 bits, and a right half $\mathbf{R}_{\mathbf{0}}$ of 32 bits.
Example: From IP, we get $\mathbf{L}_{\mathbf{0}}$ and $\mathbf{R}_{\mathbf{0}}$
$\mathbf{L}_{\mathbf{0}}=11001100000000001100110011111111$
$\mathbf{R}_{\mathbf{0}}=11110000101010101111000010101010$
We now proceed through 16 iterations, for $1<=\mathbf{n}<=16$, using a function $\mathbf{f}$ which operates on two blocks--a data block of 32 bits and a key $\mathbf{K}_{\mathbf{n}}$ of 48 bits--to produce a block of 32 bits. Let + denote XOR addition, (bit-by-bit addition modulo 2). Then for $\mathbf{n}$ going from 1 to 16 we calculate
$\mathbf{L}_{\mathbf{n}}=\mathbf{R}_{\mathrm{n}-1}$
$\mathbf{R}_{\mathrm{n}}=\mathbf{L}_{\mathrm{n}-1}+\mathbf{f}\left(\mathbf{R}_{\mathrm{n}-1}, \mathbf{K}_{\mathrm{n}}\right)$
This results in a final block, for $\mathbf{n}=16$, of $\mathbf{L}_{\mathbf{1 6}} \mathbf{R}_{\mathbf{1 6}}$. That is, in each iteration, we take the right 32 bits of the previous result and make them the left 32 bits of the current step. For the right 32 bits in the current step, we XOR the left 32 bits of the previous step with the calculation $\mathbf{f}$.
Example: For $\mathbf{n}=1$, we have
$\mathbf{K}_{1}=000110110000001011101111111111000111000001110010$
$\mathbf{L}_{\mathbf{1}}=\mathbf{R}_{\mathbf{0}}=11110000101010101111000010101010$
$\mathbf{R}_{1}=\mathbf{L}_{\mathbf{0}}+\mathbf{f}\left(\mathbf{R}_{\mathbf{0}}, \mathbf{K}_{\mathbf{1}}\right)$

It remains to explain how the function $\mathbf{f}$ works. To calculate $\mathbf{f}$, we first expand each block $\mathbf{R}_{\mathbf{n} 1}$ from 32 bits to 48 bits. This is done by using a selection table that repeats some of the bits in $\mathbf{R}_{\mathrm{n}-1}$. We'll call the use of this selection table the function $\mathbf{E}$. Thus $\mathbf{E}\left(\mathbf{R}_{\mathbf{n}-1}\right)$ has a 32 bit input block, and a 48 bit output block.

## 3.5: Permutation Key PC-1

From 64-bit key only 56 bits are selected. The key is then divided as left half and right half. Bit shifting is done on every part. (Every eight bit can be used for parity control which is excluded from encryption.

## Answer:

In general, a 64 -bit key is used as input for DES, of which only 56 -bits are used. 16 subkeys, with 48 -bit each, will then be created from this 56-bits.
The first step is to permute the key using the PC-1 table above. This is, the first bit of our 56-bit permutation key will be the 57th bit of our original key, and so on.

| Left half |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 57 | 49 | 41 | 33 | 25 | 17 | 9 |
| 1 | 58 | 50 | 42 | 34 | 26 | 18 |
| 10 | 2 | 59 | 51 | 43 | 35 | 27 |
| 19 | 11 | 3 | 60 | 52 | 44 | 36 |
| Right half |  |  |  |  |  |  |
| 63 | 55 | 47 | 39 | 31 | 23 | 15 |
| 7 | 62 | 54 | 46 | 38 | 30 | 22 |
| 14 | 6 | 61 | 53 | 45 | 37 | 29 |
| 21 | 13 | 5 | 28 | 20 | 12 | 4 |

Input Key: 0011011000110100011000100110100101110100010010110110010101111001
Would Become: 0000000011111100110111111001000000100101010100111010100000110000
Next we divide the key in two parts, left $\mathbf{C}_{\boldsymbol{0}}$ and right $\mathbf{D}_{\mathbf{0}}$.

## $C_{0}: 00000000111111001101111110010000$

$D_{0:} 00100101010100111010100000110000$

| Iteration <br> Number | Number of lift <br> shift |
| :--- | :--- |
| 1 | 1 |
| 2 | 1 |
| 3 | 2 |
| 4 | 2 |
| 5 | 2 |
| 6 | 2 |
| 7 | 2 |
| 8 | 2 |
| 9 | 1 |
| 10 | 2 |
| 11 | 2 |
| 12 | 2 |
| 13 | 2 |
| 14 | 2 |
| 15 | 2 |
| 16 | 1 |

To do a left shift we move each bit one place to the left, except for the first bit which goes to the end of the block.
In our example, we would have the following 16 keys
$C_{0}: 00000000111111001101111110010000 \quad D_{0}$ : 00100101010100111010100000110000 Would originate:
C $1: 00000001111110011011111100100000$
$D_{1:} 01001010101001110101000001100000$
$C_{2}$ : 00000011111100110111111001000000
$D_{2:} 10010101010011101010000011000001$
C3: 00001111110011011111100100000000
D3: 01010101001110101000001100100001
C4: 00111111001101111110010000000001
D4: 01010100111010100000110010010001
C5: 11111100110111111001000000000001
D5: 01010011101010000011001001010001
C6: 11110011011111100100000000110001
D6: 01001110101000001100100101010000
$\mathrm{C}_{7} \mathbf{1 1 0 0 1 1 0 1} 111110010000000011110000$
D7: 00111010100000110010010101010001 C8: 00110111111001000000001111110001 C9: 01101111110010000000011111100000

D8: 11101010000011001001010101000000
D9: 11010100000110010010101010010001 $\mathrm{C}_{10}$ : 10111111001000000001111110010001

D 10 : 01010000011001001010101001110001 $\mathrm{C}_{11}$ : 11111100100000000111111001100001

D 11 : 01000001100100101010100111010000 $\mathrm{C}_{12}$ : 11110010000000011111100110110001

D12: 00000110010010101010011101010000 C13: 11001000000001111110011011110000

D13: 00011001001010101001110101000001 C14: 00100000000111111001101111110000

D14: 01100100101010100111010100000000 $\mathrm{C}_{15}$ : 10000000011111100110111111000000 D15: 10010010101010011101010000010001 C16: 00000000111111001101111110010000

## 3.6: Permutation Expansion

Every round Feistel function is initiated by expansion. The right half of data is expanded from 32 to 48 bits.

## Answer:

The Permutation Expansion is used to expand the 32 -bit input to a round's F function into a 48 -bit block. The E function is fairly straightforward and is implemented as shown in the Table below.

| 32 | 1 | 2 | 3 | 4 | 5 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | 7 | 8 | 9 | 8 | 9 | 10 | 11 |
| 12 | 13 | 12 | 13 | 14 | 15 | 16 | 17 |
| 16 | 17 | 18 | 19 | 20 | 21 | 20 | 21 |
| 22 | 23 | 24 | 25 | 24 | 25 | 26 | 27 |
| 28 | 29 | 28 | 29 | 30 | 31 | 32 | 1 |

As shown in the Table, the first two bits of each eight-bit block are the same as the last two bits of the previous block (wrapping around to the last block in the case of the first row). The remaining 4 columns are the bits of the input in order starting with the second bit.

As an example, let's expand the 32-bit string: 11010100000001001101010011110011 . For the purposes of this example, we'll break the steps into two parts: the left two columns repeated from the previous round and the right four columns which are unique. The symbol ' $:$ ' is used to represent a range that is inclusive and wraps around, i.e. $30: 2$ is ( $30,31,1,2$ ).

## In: 11010100000001001101010011110011

## Left Right

$P[32: 1]=11 \quad P[2: 5]=1010$
$P[4: 5]=10 \quad P[6: 9]=1000$
$P[8: 9]=00 \quad P[10: 13]=0000$
$P[12: 13]=00 \quad P[14: 17]=1001$
$P[16: 17]=01 \quad P[18: 21]=1010$
$P[20: 21]=10 \quad P[22: 25]=1001$
$P[24: 25]=01 \quad P[26: 29]=1110$
$P[28: 29]=10 \quad P[30: 1]=0111$
Out: 111010101000000000001001011010101001011110100111

## Binary Shifting

The 48 bits are rotated left by one or 2 bits.

| No. of <br> cycle | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Amount <br> of bits | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 2 | 2 | 2 | 2 | 2 | 1 | 16 |

Binary shifting is just as its name suggests; we are shifting or moving binary values left or right. Each 1 or 0 is called a bit; which is short for Binary digit. BIT: The smallest unit of data in a computer. It is either a 0 or a 1. Eight bits are called a byte

## Permutation Key PC-2

From the 56 bit sub key which is output of a given round of Feistel function only 48 bit sub key are selected.

| 14 | 17 | 11 | 24 | 1 | 5 | 3 | 28 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | 6 | 21 | 10 | 23 | 19 | 12 | 4 |
| 26 | 8 | 16 | 7 | 27 | 20 | 13 | 2 |
| 41 | 52 | 31 | 37 | 47 | 55 | 30 | 40 |
| 51 | 45 | 33 | 48 | 44 | 49 | 39 | 56 |
| 34 | 53 | 46 | 42 | 50 | 36 | 29 | 32 |

Key C $C_{1} D_{1}: 0000000011111100110111111001000000100101010100111010100000110000$ will become:
$K 1=00000011001011100010001100110000$
The other keys are:
$K_{2}=00011100001110010000010100101000$
$K_{3}=00001011001101000000010000010111$
$K_{4}=00001000001110110010001000000011$
$K_{5}=00000111001101100011110000000101$
$K_{6}=00110101000100010011000100001010$
$\mathrm{K}_{7}=00101100001100000010000000001001$
$K_{8}=00111001000111010010010000011111$
$K_{9}=00101101001001110010100100000101$
$K_{10}=00110011000011000010011000001100$
$K_{11}=00111001000110110010011000100000$
$K_{12}=00101010000011010001010000011110$
$K_{13}=00010101001010110000001000001001$

## $K_{14}=00001011000010110001111000100100$

$K_{15}=00110101000110000010011100011010$
$K_{16}=00101100001001110011100000000000$

## S-Boxes

- 48 bit input is divided into 6 bit input of 8 blocks.
- From each 6 bit the first and the last bit is taken as a row value and the remaining 4 bits are taken as a column value. - The resultant $S$ - box value is a 4 bit output. For ex, for a 6 bit input 001110 the row value is $0(00)$ and the column value is $7(0111)$ and the resultant S1 box is 8 whose 4 bit output is 1000 .


## Answer:

The first and last bits of $\mathbf{B}$ represent in base 2 a number in the decimal range 0 to 3 (binary 00 to 11 ). Let that number be $\mathbf{i}$. The 4 bits in the middle of $\mathbf{B}$ represent in base 2 a number in the decimal range 0 to 15 (binary 0000 to 1111). Let that number be $\mathbf{j}$.
Look up in the table the number in the $\mathbf{i}$-th row and $\mathbf{j}$-th column. It is a number in the range 0 to 15 and is uniquely represented by a 4 bit block. That block is the output $\mathbf{S}_{\mathbf{1}}(\mathbf{B})$ of $\mathbf{S}_{\mathbf{1}}$ for the input $\mathbf{B}$. For example, for input block $\mathbf{B}=011011$ the first bit is " 0 " and the last bit " 1 " giving 01 as the row. This is row 1 . The middle four bits are " 1101 ". This is the binary equivalent of decimal 13 , so the column is column number 13 . In row 1 , column 13 appears 5 . This determines the output; 5 is binary 0101 , so that the output is 0101 . Hence $\mathbf{S}_{1}(011011)=0101$.

The tables defining the functions $\mathbf{S}_{\mathbf{1}}, \ldots, \mathbf{S}_{\mathbf{8}}$ are the following:

$$
\mathrm{S}_{1}
$$

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 14 | 4 | 13 | 1 | 2 | 15 | 11 | 8 | 3 | 10 | 6 | 12 | 5 | 9 | 0 | 7 |
| 1 | 0 | 15 | 7 | 4 | 14 | 2 | 13 | 1 | 10 | 6 | 12 | 11 | 9 | 5 | 3 | 8 |
| 2 | 4 | 1 | 14 | 8 | 13 | 6 | 2 | 11 | 15 | 12 | 9 | 7 | 3 | 10 | 5 | 0 |
| 3 | 15 | 12 | 8 | 2 | 4 | 9 | 1 | 7 | 5 | 11 | 3 | 14 | 10 | 0 | 6 | 13 |


|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 15 | 1 | 8 | 14 | 6 | 11 | 3 | 4 | 9 | 7 | 2 | 13 | 12 | 0 | 5 | 10 |
| 1 | 3 | 13 | 4 | 7 | 15 | 2 | 8 | 14 | 12 | 0 | 1 | 10 | 6 | 9 | 11 | 5 |
| 2 | 0 | 14 | 7 | 11 | 10 | 4 | 13 | 1 | 5 | 8 | 12 | 6 | 9 | 3 | 2 | 15 |
| 3 | 13 | 8 | 10 | 1 | 3 | 15 | 4 | 2 | 11 | 6 | 7 | 12 | 0 | 5 | 14 | 9 |


|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 10 | 0 | 9 | 14 | 6 | 3 | 15 | 5 | 1 | 13 | 12 | 7 | 11 | 4 | 2 | 8 |
| 1 | 13 | 7 | 0 | 9 | 3 | 4 | 6 | 10 | 2 | 8 | 5 | 14 | 12 | 11 | 15 | 1 |
| 2 | 13 | 6 | 4 | 9 | 8 | 15 | 3 | 0 | 1 | 1 | 2 | 12 | 5 | 10 | 14 | 7 |
| 3 | 1 | 10 | 13 | 0 | 6 | 9 | 8 | 7 | 4 | 15 | 14 | 3 | 11 | 5 | 2 | 12 |


|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 7 | 13 | 14 | 3 | 0 | 6 | 9 | 10 | 1 | 2 | 8 | 5 | 11 | 12 | 4 | 15 |
| 1 | 13 | 8 | 11 | 5 | 6 | 15 | 0 | 3 | 4 | 7 | 2 | 12 | 1 | 10 | 14 | 9 |
| 2 | 10 | 6 | 9 | 0 | 12 | 11 | 7 | 13 | 15 | 1 | 3 | 14 | 5 | 2 | 8 | 4 |
| 3 | 3 | 15 | 0 | 6 | 10 | 1 | 13 | 8 | 9 | 4 | 5 | 11 | 12 | 7 | 2 | 14 |


|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 2 | 12 | 4 | 1 | 7 | 10 | 11 | 6 | 8 | 5 | 3 | 15 | 13 | 0 | 14 | 9 |
| 1 | 14 | 11 | 2 | 12 | 4 | 7 | 13 | 1 | 5 | 0 | 15 | 10 | 3 | 9 | 8 | 6 |
| 2 | 4 | 2 | 1 | 11 | 10 | 13 | 7 | 8 | 15 | 9 | 12 | 5 | 6 | 3 | 0 | 14 |
| 3 | 11 | 8 | 12 | 7 | 1 | 14 | 2 | 13 | 6 | 15 | 0 | 9 | 10 | 4 | 5 | 3 |


|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 12 | 1 | 10 | 15 | 9 | 2 | 6 | 8 | 0 | 13 | 3 | 4 | 14 | 7 | 5 | 11 |
| 1 | 10 | 15 | 4 | 2 | 7 | 12 | 9 | 5 | 6 | 1 | 13 | 14 | 0 | 11 | 3 | 8 |
| 2 | 9 | 14 | 15 | 5 | 2 | 8 | 12 | 3 | 7 | 0 | 4 | 10 | 1 | 13 | 11 | 6 |
| 3 | 4 | 3 | 2 | 12 | 9 | 5 | 15 | 10 | 11 | 14 | 1 | 7 | 6 | 0 | 8 | 13 |


|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 4 | 11 | 2 | 14 | 15 | 0 | 8 | 13 | 3 | 12 | 9 | 7 | 5 | 10 | 6 | 1 |
| 1 | 13 | 0 | 11 | 7 | 4 | 9 | 1 | 10 | 14 | 3 | 5 | 12 | 2 | 15 | 8 | 6 |
| 2 | 1 | 4 | 11 | 13 | 12 | 3 | 7 | 14 | 10 | 15 | 6 | 8 | 0 | 5 | 9 | 2 |
| 3 | 6 | 11 | 13 | 8 | 1 | 4 | 10 | 7 | 9 | 5 | 0 | 15 | 14 | 2 | 3 | 12 |


|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 13 | 2 | 8 | 4 | 6 | 15 | 11 | 1 | 10 | 9 | 3 | 14 | 5 | 0 | 12 | 7 |
| 1 | 1 | 15 | 13 | 8 | 10 | 3 | 7 | 4 | 12 | 5 | 6 | 11 | 0 | 14 | 9 | 2 |
| 2 | 7 | 11 | 4 | 1 | 9 | 12 | 14 | 2 | 0 | 6 | 10 | 13 | 15 | 3 | 5 | 8 |
| 3 | 2 | 1 | 14 | 7 | 4 | 10 | 8 | 13 | 15 | 12 | 9 | 0 | 3 | 5 | 6 | 11 |

In our example we obtain as the output of the eight $S$ boxes:
$\boldsymbol{K}_{1} \oplus \mathrm{E}\left(\boldsymbol{R}_{\boldsymbol{0}}\right)=100000110010111111011101101100000010100000001010$
$\mathbf{S}_{1}\left(\mathbf{B}_{1}\right) \mathbf{S}_{2}\left(\mathbf{B}_{2}\right) \mathbf{S}_{3}\left(\mathbf{B}_{3}\right) \mathbf{S}_{4}\left(\mathbf{B}_{4}\right) \mathbf{S}_{5}\left(\mathbf{B}_{5}\right) \mathbf{S}_{6}\left(\mathbf{B}_{6}\right) \mathbf{S}_{7}\left(\mathbf{B}_{7}\right) \mathbf{S}_{8}\left(\mathbf{B}_{8}\right)=$
01001000110011100111000100011111

## Permutation $\mathbf{P}$

The output block of 32 bit from $S$-box undergo P-Permutation

## Answer:

The Permutation p in DES is another permutation function. It takes a thrity-two bit block as input and outputs a thirty-two bit block. The permutation is shown in the Table below.

| 16 | 7 | 20 | 21 | 29 | 12 | 28 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 15 | 23 | 26 | 5 | 18 | 31 | 10 |
| 2 | 8 | 24 | 14 | 32 | 27 | 3 | 9 |
| 19 | 13 | 30 | 6 | 22 | 11 | 4 | 25 |

As shown, the permutation for the P function is not as structured as other permutation functions in DES. However, the permutation is not random and is the same for all rounds of DES.

As an example, we'll use the S-Box output from our example in the previous section: 101011011110111010010100 01110010.

In: 10101101111011101001010001110010
$\mathrm{P}[16]=0, \mathrm{P}[7]=0, \mathrm{P}[20]=1, \mathrm{P}[21]=0, \mathrm{P}[29]=0, \mathrm{P}[12]=0, \mathrm{P}[28]=1, \mathrm{P}[17]=1$
$\mathrm{P}[1]=1, \mathrm{P}[15]=1, \mathrm{P}[23]=0, \mathrm{P}[26]=1, \mathrm{P}[5]=1, \mathrm{P}[18]=0, \mathrm{P}[31]=1, \mathrm{P}[10]=1$
$\mathrm{P}[2]=0, \mathrm{P}[8]=1, \mathrm{P}[24]=0, \mathrm{P}[14]=1, \mathrm{P}[32]=0, \mathrm{P}[27]=1, \mathrm{P}[3]=1, \mathrm{P}[9]=1$
$\mathrm{P}[19]=0, \mathrm{P}[13]=1, \mathrm{P}[30]=0, \mathrm{P}[6]=1, \mathrm{P}[22]=1, \mathrm{P}[11]=1, \mathrm{P}[4]=0, \mathrm{P}[25]=0$
Out: 00100011110110110101011101011100

## Final Permutation

This is done for every block of data which is the inverse of IP.

| 40 | 8 | 48 | 16 | 56 | 24 | 64 | 32 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 39 | 7 | 47 | 15 | 55 | 23 | 63 | 31 |
| 38 | 6 | 46 | 14 | 54 | 22 | 62 | 30 |
| 37 | 5 | 45 | 13 | 53 | 21 | 61 | 29 |
| 36 | 4 | 44 | 12 | 52 | 20 | 60 | 28 |
| 35 | 3 | 43 | 11 | 51 | 19 | 59 | 27 |
| 34 | 2 | 42 | 10 | 50 | 18 | 58 | 26 |
| 33 | 1 | 41 | 9 | 49 | 17 | 57 | 25 |

The final permutation occurs after the sixteen rounds of DES are completed. It is the inverse of the initial permutation and is shown in the Table below.

As an example, let's undo the initial permutation. Its output was 01001100001100110101011010011110 00111010001001101010000010001110.

The Final Permutation is applied as follows:
In: 0100110000110011010101101001111000111010001001101010000010001110
$\mathrm{P}[40]=0, \mathrm{P}[8]=0, \mathrm{P}[48]=0, \mathrm{P}[16]=1, \mathrm{P}[56]=0, \mathrm{P}[24]=0, \mathrm{P}[64]=0, \mathrm{P}[32]=0$
$\mathrm{P}[39]=1, \mathrm{P}[7]=0, \mathrm{P}[47]=1, \mathrm{P}[15]=1, \mathrm{P}[55]=0, \mathrm{P}[23]=1, \mathrm{P}[63]=1, \mathrm{P}[31]=1$
$\mathrm{P}[38]=0, \mathrm{P}[6]=1, \mathrm{P}[46]=1, \mathrm{P}[14]=0, \mathrm{P}[54]=0, \mathrm{P}[22]=1, \mathrm{P}[62]=1, \mathrm{P}[30]=1$
$\mathrm{P}[37]=1, \mathrm{P}[5]=1, \mathrm{P}[45]=0, \mathrm{P}[13]=0, \mathrm{P}[53]=0, \mathrm{P}[21]=0, \mathrm{P}[61]=1, \mathrm{P}[29]=1$
$\mathrm{P}[36]=1, \mathrm{P}[4]=0, \mathrm{P}[44]=0, \mathrm{P}[12]=1, \mathrm{P}[52]=0, \mathrm{P}[20]=1, \mathrm{P}[60]=0, \mathrm{P}[28]=1$
$\mathrm{P}[35]=1, \mathrm{P}[3]=0, \mathrm{P}[43]=1, \mathrm{P}[11]=1, \mathrm{P}[51]=1, \mathrm{P}[19]=0, \mathrm{P}[59]=0, \mathrm{P}[27]=0$
$\mathrm{P}[34]=0, \mathrm{P}[2]=1, \mathrm{P}[42]=0, \mathrm{P}[10]=0, \mathrm{P}[50]=0, \mathrm{P}[18]=1, \mathrm{P}[58]=0, \mathrm{P}[26]=0$
$\mathrm{P}[33]=0, \mathrm{P}[1]=0, \mathrm{P}[41]=0, \mathrm{P}[9]=0, \mathrm{P}[49]=1, \mathrm{P}[17]=0, \mathrm{P}[57]=1, \mathrm{P}[25]=1$
Out: 0001000010110111011001111100001110010101101110000100010000001011

## Conclusion

In this paper we have explained mathematical manner for DES algorithm and have also given examples for the same. The essential concern in DES algorithm safety is about 2 areas such as nature of algorithm and key size. It is clear that DES can be damaged the use of 255 encryptions. However, nowadays most purposes use both 3DES with two keys or 3DES with three keys. These two a couple of DES versions make DES resistant to brute- force attacks.

