

MID TERM

Summer

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Section: "B"

Semester: 6th

Subject: Structure Analysis - II

Instructor: Engr. Adeed Khan

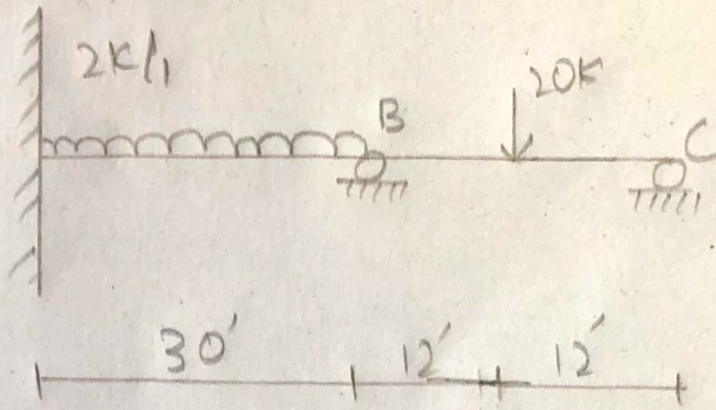
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Question # 01

Question # 01

1:

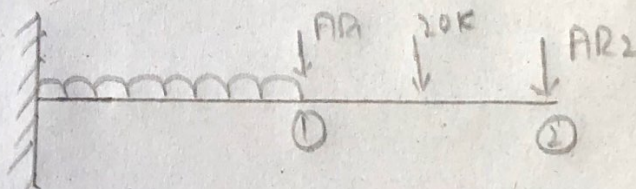


EI constant

S.I = 2°

Step # 01

select redundant actions



$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \quad \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

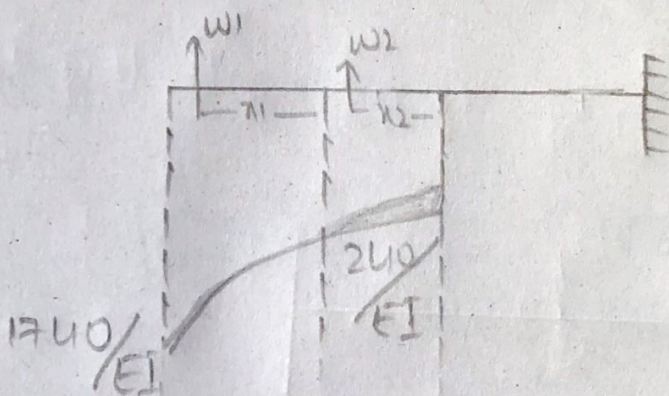
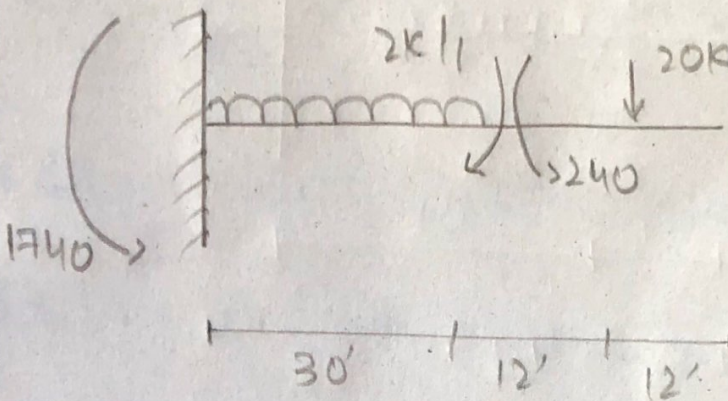
$$[DRS] = [DRL] + F \cdot AR$$

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Question #01

Step #02 compute the values of [DRL]



$$w_1 = \left(\frac{240 + 0}{2EI} \right) \times 12 = 1440/EI$$

$$w_2 = \frac{1}{n+1} \times (b \times h) = \frac{1}{2+1} \left(\frac{1100}{EI} \right) \times 30 = 11000$$

$$x_1 = \frac{L}{3} \left(\frac{a+2b}{a+b} \right)$$

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Question # 01

$$x_1 = \frac{12}{3} \left(\frac{240 + 2(0)}{240 + 0} \right) = 4$$

$$x_2 = \frac{3}{r+2} \times b = \frac{3}{2+2} (30) = 22.5'$$

$$DRL_1 = w_1 (x_1 + 30) = 1440 (4 + 30) = 48960$$

$$\begin{aligned} DRL_2 &= w_1 (x_1 + 40) + w_2 (x_2 + 12) \\ &= 1440 (4 + 40) + 1100 (22.5 + 12) \end{aligned}$$

$$DRL_2 = 442860$$

$$[DRL] = \frac{1}{EI} \begin{bmatrix} 48960 \\ 442860 \end{bmatrix}$$

Step # 03

Construct Flexibility
co-efficient matrix

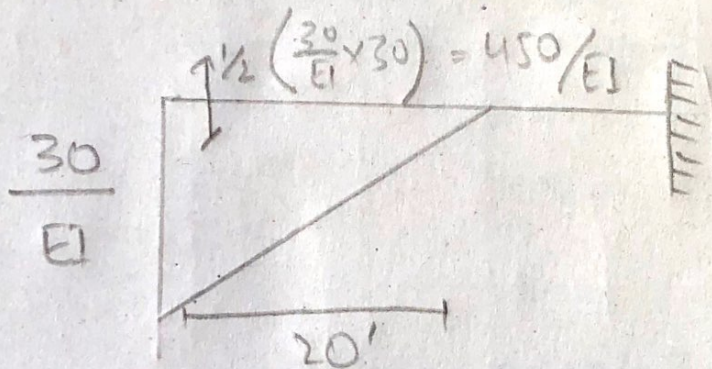
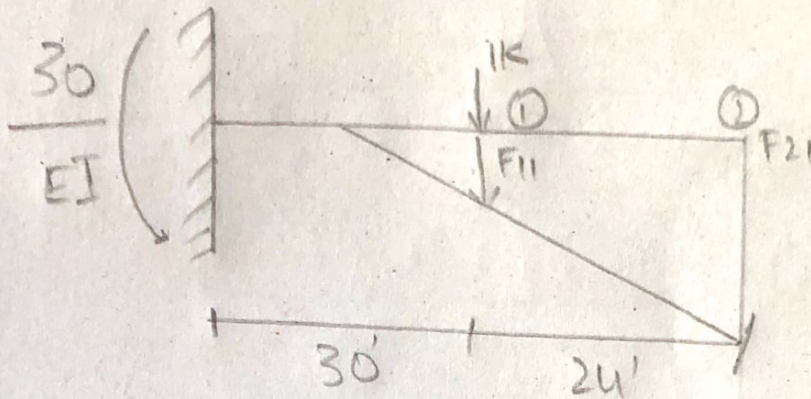
$$F_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

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Question # 01

a) Apply a unit value of F_{11} at reference point i - complete the value of F_{11} and F_{21}



$$\frac{2}{3}(30) = 20'$$

$$F_{11} = \frac{450}{EI} (20) = \frac{9000}{EI}$$

$$F_{21} = \frac{450}{EI} (20+24) = \frac{19800}{EI}$$

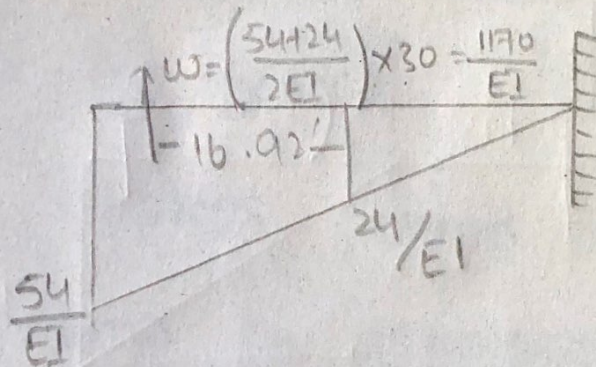
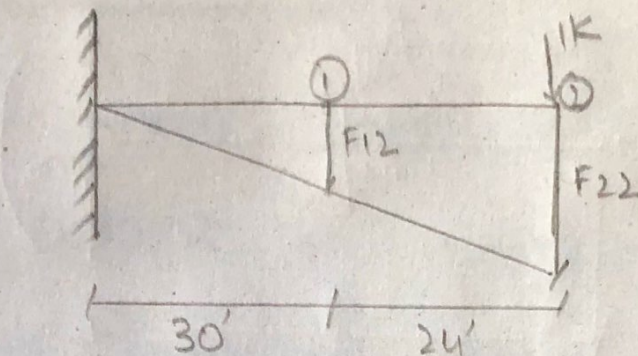
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Question #01

b) Apply 1 unit of AB_2 at reference point ②

ii- Compute the value of F_{12} & F_{22}



$$\alpha = \frac{30}{3} \left[\frac{24 + 2(54)}{54 + 24} \right] = 16.92'$$

$$F_{12} = \frac{1170}{EI} \times 16.92 = \frac{19800}{EI}$$

$$F_{22} = \frac{1}{2} (54 \times 54) \times \frac{1}{3} (30) + 24 = \frac{49572}{EI}$$

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Question #02

Question #02

Answer:

Force method:

In force method forces are redundant on unknowns

Force method starts with equilibrium of forces.

Forces bound by compatibility equation of displacement

$$\text{no of redundants} = D_s$$

not suitable for compute.

It strain energy method.

$$D_s < D_K$$

known as flexibility method.

Displacement Method:

Also known as stiffness matrix method
slope deflection method
moment distribution method
 $DS > DK$

Displacement are redundants are unknowns.

Starts with compatible deformations
Displacement bound by equilibrium equation of forces.

NO of redundants = DK
not suitable of ELOSS.

Suggest:

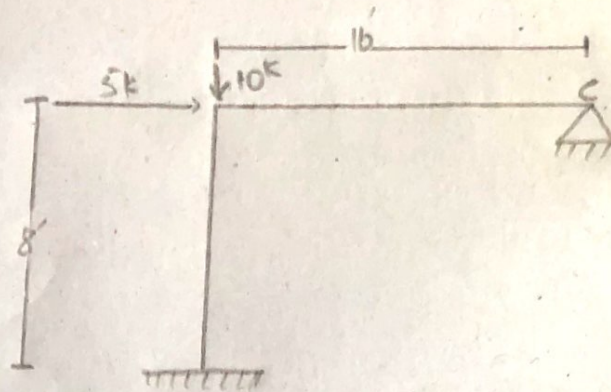
Displacement method is better and suitable because it is used globally and is easy too.

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Question # 03

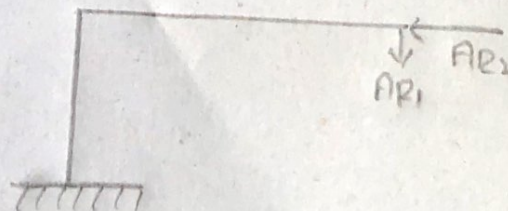
Pb#

 $E = \text{constant}$ $I = I$ $I_B = 2I$ Solution:

Total Statical indeterminacy
 $\Rightarrow R - 3 = 5 - 3 = 2^{\circ}$

Step # 01

Identify Redundant Actions



$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Step #02

compute value of [DRL]

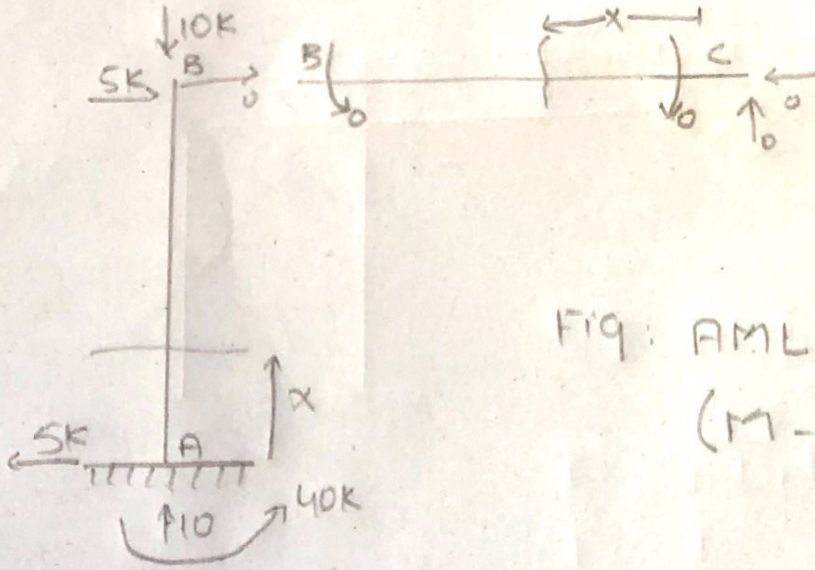


Fig: AML values (M-values)

Step #03

~~compute value of [DRL]~~
[F] or [AMR]

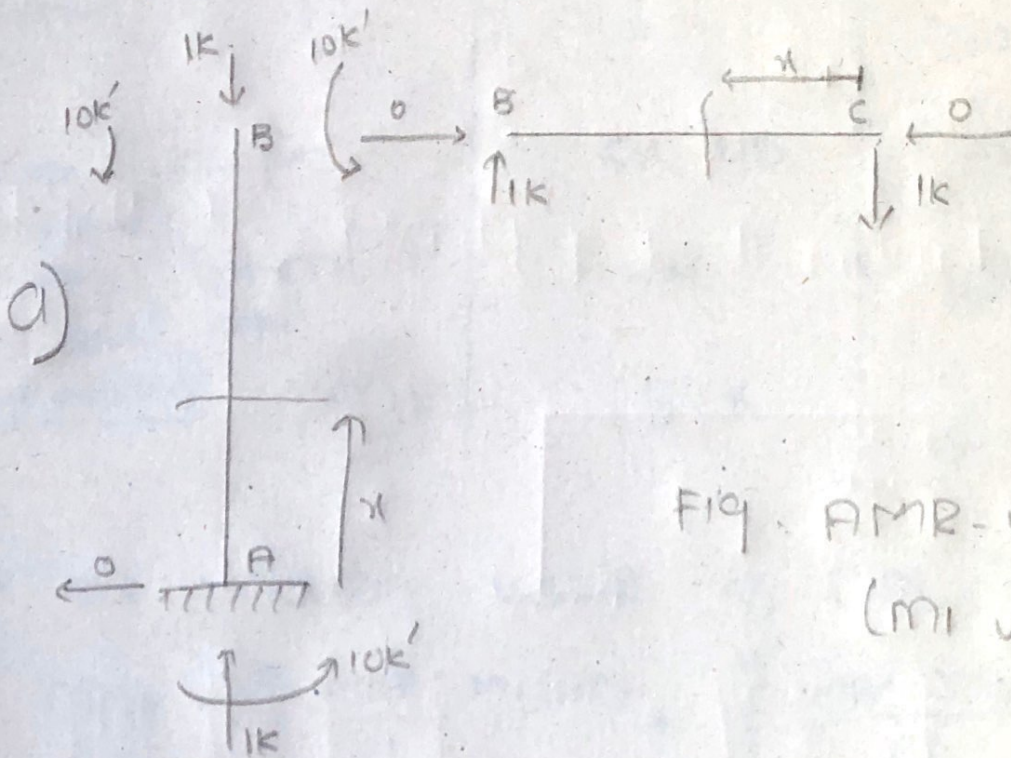


Fig: AMR-values (mi values)

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Question # 03

b)

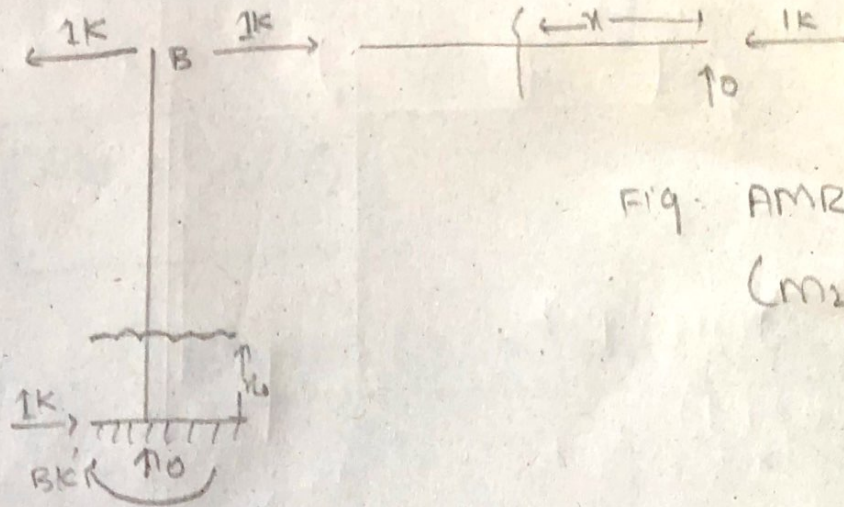


Fig: AMR values
(m₂ values)

Member	AB	BC
select origin (should be select the support)	A	C
Limits	0-8	0-16
I	I	2I
Take x-section on AML Fig and find moment	5x-40	0
from MI origin	-16	0
m ₂	8-x	0

x → take x-section on m₁ Fig from the origin

⇒ For finding value of DRL:

$$DRLI = \int_0^8 \frac{M_{AB} \cdot m_1(AB)}{EI} + \int_0^{16} \frac{M_{BC} \cdot m_2(BC)}{EI}$$

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Question #03

$$= \int_0^8 \frac{(5x-40)(-18)}{EI} dx + \int_0^{16} \frac{0 \cdot x}{E(2I)} dx$$

$$\boxed{DRL_1 = \frac{2560}{EI}}$$

$$DRL_2 = \int_0^8 \frac{(5x-40)(8-x)}{EI} dx + \int_0^{16} \frac{0 \cdot 0}{E(2I)} dx$$

$$\boxed{DRL_2 = \frac{-853.33}{EI}}$$

⇒ compute flexibility matrix:

$$F_{2 \times 2}^{\rightarrow 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

$$\Rightarrow \underline{F_{11}} = \int_0^8 \frac{m_1^2(AB)}{EI} + \int_0^{16} \frac{m_1^2(BC)}{EI} = \int_0^8 \frac{(-16)^2}{EI} dx + \int_0^{16} \frac{x^2}{E(2I)}$$

$$\boxed{F_{11} = \frac{2730.67}{EI}}$$

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Question # 03

$$F_{12} = F_{21} = \int_0^8 \frac{m_1(AB) \cdot m_2(AB)}{EI} dx + \int_0^{16} \frac{m_1(BC) \cdot m_2(BC)}{2EI} dx$$

$$= \int_0^8 \frac{(-16)(8-x)}{EI} dx + \int_0^{16} \frac{(x)(0)}{2EI} dx$$

$$F_{12} = F_{21} = \frac{-512}{EI}$$

$$F_{22} = \int_0^8 (m_2)_{AB}^2 dx + \int_0^{16} (m_2)_{BC}^2 dx$$

$$= \int_0^8 \frac{(8-x)^2}{EI} dx + \int_0^{16} \frac{0^2}{2EI} dx$$

$$F_{22} = 170.67$$

As we know that

$$[DRS] = [DRL] + [AR] \times [F]$$

$$\Rightarrow [AR] = \frac{[DRS] - [DRL]}{[F]}$$

$$2) [AR] = [F]^{-1} \times [DRS - DRL]$$

$$= \begin{bmatrix} 2730.67 & -512 \end{bmatrix}^{-1} \times \begin{bmatrix} 0 - 2560 \\ 0 + 853.33 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} -0.00005 \\ 4.997 \end{bmatrix} = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$

- ~~1) draw the static~~
- ~~2) Mod A (I)~~
- ~~3) select order~~
- ~~4) put values and~~
- ~~select~~
- ~~5) press (on)~~
- ~~6) shift + 4~~