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Section

"A"


Semester

4th

Department

Civil engineering

Sign



paper

fluid mechanics

Energy Head :

It is the sum of all energy heads at a point in a fluid.

Form of Energy Head :

There are various form of energy head which are as follow.

- 1) Kinetic Head
- 2) Potential Head
- 3) Pressure Head

Kinetic Head :

It is the kinetic energy per unit weight of the fluid.

Mathematical Form:

$$\frac{K.E}{w} = \frac{1/2 mv^2}{mg}$$

$$\frac{K.E}{w} = 1/2 \frac{v^2}{g}$$

This is also known as velocity head.

UNIT: is meter (m).

Potential Head:

It is the potential energy per unit weight of the fluid.

Mathematical Form:

$$\frac{P.E}{w} = \frac{mgh}{mg} = h$$

PRESSURE HEAD:

The vertical height of the free surface above any point in a liquid at rest is pressure Head.

OR
Level of fluid due to pressure exerted by fluid.

Mathematical Form:

pressure Head = $\frac{P \cdot E}{\text{weight}} = \frac{P}{\gamma}$

OR
 $= \frac{F \cdot ds}{w}$

$= \frac{P \cdot A \cdot ds}{w}$

$= \frac{P \cdot V}{w} = \frac{P}{\gamma}$ is pressure



Hydraulic grade line :

The surface or profile of water flowing in an open channel or a pipe flowing partially full. If a pipe is under pressure, the hydraulic grade line is that ~~the~~ level water would rise to in a small, vertical tube connected to the pipe. Also see energy grade line.

Energy grade line :

A line that represent elevation of energy head (in feet or meters) of water

Flowing in a pipe, conduit or channel. The line is drawn above the hydraulic grade line (gradient) a distance equal to the velocity head $(\frac{v^2}{2g})$ of the water flowing at each section or point along the pipe or channel. Also see hydraulic grade line.

Hydraulic Radius:

The ratio of the cross-sectional area of a channel or pipe in which a fluid is flowing to the wetted perimeter of the conduit.

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Q2 (Part a)

Given data:

$$\text{velocity} = v = 2 \text{ m/s}$$

$$\text{pressure} = p = 300 \text{ kPa}$$

$$\text{datum} = z = 5 \text{ m}$$

Sol:

$$H = \text{Pressure Head} + \text{KE} + \text{PE}$$

$$H = \frac{p}{\gamma} + \frac{v^2}{2g} + z$$

$$H = \frac{300 \times 10^3}{9810} + \frac{2^2}{2 \times 981} + 5$$

$$H = 35.7849 \text{ m}$$

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Q2 (Part B)

Given data :

$$\text{Diameter} = d_1 = 300 \text{ mm}$$

$$\text{Diameter} = d_2 = 200 \text{ mm}$$

$$\text{pressure} = P_1 = 300 \text{ kPa} = 300 \times 10^3 \text{ N/m}^2$$

$$\Rightarrow P_2 = 120 \text{ kPa} = 120 \times 10^3 \text{ N/m}^2$$

$$\text{Datum} = z = ?$$

$$Q = \frac{40 \text{ m}^3/\text{sec}}{1000}$$

$$d_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$d_2 = 200 \text{ mm} = 0.2 \text{ m}$$

Required :

$$z_2 = ?$$

Sol :

$$A_1 = \frac{\pi d_1^2}{4}$$

$$A_1 = \frac{3.14 \times (0.3)^2}{4}$$

$$A_1 = 0.0706 \text{ m}^2$$

$$A_2 = \frac{\pi d_2^2}{4}$$

$$A_2 = \frac{3.14 \times (0.2)^2}{4}$$

$$A_2 = 0.0314 \text{ m}^2$$

we know that

$$Q_1 = V_1 A_1$$

$$V_1 = \frac{Q}{A_1}$$

$$V_1 = \frac{0.04}{0.0706}$$

$$V_1 = 0.566$$

$$Q = \frac{40}{1000} \\ \Rightarrow 0.04$$

$$V_2 = \frac{Q}{A_2}$$

$$V_2 = \frac{0.04}{0.0314}$$

$$V_2 = 1.27$$

Now

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + Z_2$$

$$Z_1 = 0$$

$$\gamma = 9810$$

$$\frac{300 \times 10^3}{9810} + \frac{0.566^2}{2(9.81)} + 0 = \frac{120 \times 10^3}{9810} + \frac{1.27^2}{2(9.81)} + Z_2$$

$$30.59 = 12.314 + Z$$

$$\boxed{Z_2 = 18.276 \text{ m}}$$

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Given data :

Length of pipe = $l = 500\text{m}$

dia = $d = 0.2\text{m}$

Specific gravity of oil = 0.9

flow rate = $Q = 0.06\text{ m}^3/\text{s}$

viscosity = $\mu = 6 \times 10^{-5}\text{ N}\cdot\text{s}/\text{m}^2$

Required :

pressure loss = $\Delta P = ?$

As we know that

$$f = \left(0.0032 + \left(\frac{0.221}{R^{0.2}} \right) \right)$$

where $R = \text{Reynold's No}$ and
is given as:

$$R = \frac{v \times d}{\nu} \rightarrow (1)$$

and

$$V = \frac{\mu}{\rho} = \frac{6 \times 10^{-5}}{900}$$

$$V = 6.67 \times 10^{-8} \text{ m}^2/\text{s}$$

and $v = \frac{Q}{A}$

$$V = \frac{0.06}{0.031}$$

$$v = 1.95 \text{ m/s}$$

\therefore for circular pipe

$$A = \frac{\pi}{4} d^2$$

$$= \frac{\pi}{4} (0.2)^2$$

$$A = 0.031 \text{ m}^2$$

Now

$$\text{eq (1)} \Rightarrow R = \frac{1.95 \times 0.7}{6.67 \times 10^{-5}} = 5.73 \times 10^6$$

Now

$$f = 0.0032 + \frac{0.221}{(5.73 \times 10^6) \cdot 0.237}$$

$$\Rightarrow f = 8.79 \times 10^{-3}$$

$$f = 0.00879$$

Now from Bernouli's equation

$$\text{Head loss} = h_2 = \frac{fLV^2}{2gD} \rightarrow (ii)$$

Putting values in eq (2)

$$h_2 = \frac{(0.00879)(500)(1.95)^2}{2(9.81)(0.2)}$$

$$h_2 = 4.259 \text{ m}$$

Now to find pressure loss due to friction:

pressure head formula is used

$$h_2 = \frac{\Delta P}{\rho g}$$

$$\Rightarrow \Delta P = h_2 \times \rho g$$

Put values

$$\Delta P = 4.259 \times 900 \times 9.81$$

$$\Delta P = 37602.7 \text{ Pa}$$

$$\Delta P = 37.602 \text{ kPa}$$