

Course Details

Course Title

EN A

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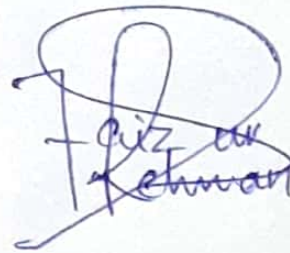
Model

4th

Student ID

14623

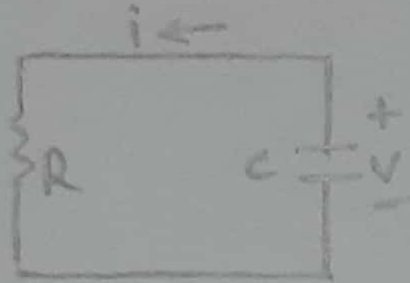
Student Sign



Faiz-ur-Rehman

Q1: For the circuit in Fig 1,
if $v = 10e^{-4t}$ & $0.2e^{-4t}$ $t > 0$

(a) Find R & C (b) (c) (d)
50% of the initial energy.



Step 1

(A) $\tau = RC = \frac{1}{4}$

$\Rightarrow -1 = C \frac{dv}{dt}$

$\Rightarrow -0.2e^{-4t} = C(10)(-4)e^{-4t}$

$\Rightarrow C = 5 \text{ mF}$

$R = \frac{1}{4C} = 50 \Omega$

Step 2

(B) $\tau = RC = \frac{1}{4} = 0.250$

Step 3

(C) $W_C(0) = \frac{1}{2} C v^2$

$\Rightarrow \frac{1}{2} (5 \times 10^{-3}) (100)$

$\Rightarrow 250 \text{ mJ}$

Step 4

$$(D) \quad W_R = \frac{1}{2} \times \frac{1}{2} C V_0^2$$

$$\Rightarrow \frac{1}{2} C V_0^2 (1 - e^{-\frac{2t_0}{\tau}})$$

$$0.5 = 1 - e^{-8t} \Rightarrow e^{-8t_0} = \frac{1}{2}$$

OR

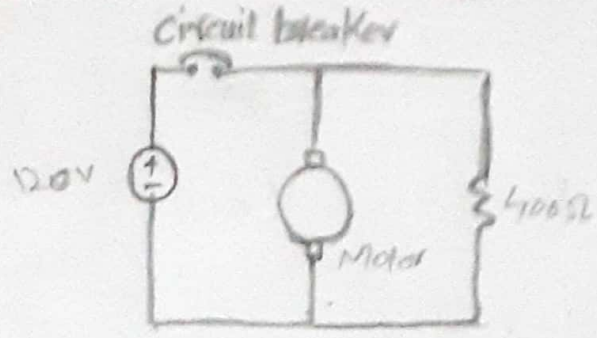
$$e^{8t_0} = 2$$

$$t_0 = \frac{1}{8} \ln(2)$$

$$\Rightarrow 88.6 \text{ ms}$$

Q2

A 120-v dc generator energize a motor whose coil _____ the Breaker is tripped.



Step 1

Let the inductor current,

For $t < 0$

$$i(0) = \frac{120}{100} = \frac{12}{10}$$

$$\Rightarrow \frac{6}{5} = 1.2 \text{ A}$$

For $t > 0$ We have an RL circuit

$$\tau = \frac{L}{R} = \frac{50}{100+400}$$

$$\Rightarrow \frac{50}{500} \Rightarrow \frac{5}{50}$$

$$\Rightarrow \frac{1}{10} = 0.1$$

$$i(\infty) = 0$$

$$i(t) = i(\infty) + [i(0) - i(\infty)] e^{-t/\tau}$$

$$i(t) = 1.2 e^{-10t}$$

$$\text{At } t = 100 \text{ ms} = 0.1 \text{ s}$$

$$i(0.1) = 1.2 e^{-1} = 0.441 \text{ A}$$

Which is the same as the current through the resistor

Step 2

(B)

$$\tau = R_{\text{rms}} = 60 \mu\text{s}$$

An integrator

$$\tau < 0.1 \quad \tau = 6 \mu\text{s}$$

$$\tau_{\text{max}} = 6 \mu\text{s}$$

Q3

The Response of RLC series RLC circuit

Determine the value of R, L, C

Step 1

Series RLC Circuit

$$v_L(t) = 30 - 10e^{-20t} + 30e^{-10t} \text{ V}$$

$$V(t) = V_s + A_1 e^{s_1 t} + A_2 e^{s_2 t} \quad [\alpha > \omega_0]$$

$$40e^{-20t} - 60e^{-30t} \text{ mA}$$

$$\Leftrightarrow i(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t} \quad [\alpha > \omega_0]$$

Comparing these equ... we get

$$V_s = 30$$

$$A_1 = -10 ; A_2 = 30 ;$$

$$s_1 = -20 ; s_2 = -10 \rightarrow (a)$$

$$A_1' = 40 ; A_2' = -60 ;$$

$$s_1' = -20 ; s_2' = -10 \rightarrow (b)$$

Step 2

NO IN Equ (a) & (b)

$$s_1 = -\alpha + \sqrt{\alpha^2 - \omega_0^2} \quad \text{And} \quad s_2 = -\alpha - \sqrt{\alpha^2 - \omega_0^2}$$

$$s_1 + s_2 = -2\alpha \quad \& \quad s_1 s_2 = \omega_0^2$$

$$\left[\text{where } \alpha = \frac{R}{2L} ; \omega_0 = \frac{1}{\sqrt{LC}} \right]$$

$$\Rightarrow -30 = -2\alpha$$

$$\Rightarrow \alpha = 15$$

$$\Rightarrow \frac{R}{2L} = 15 \rightarrow (c)$$

$$200 = \omega_0^2 \Rightarrow \frac{1}{LC} = 200 \rightarrow (d)$$

Step 3//

$$i(t) = C \frac{dv(t)}{dt} = C [200e^{-20t} - 300e^{-30t}]$$

$$(A_1 e^{s_1 t} + A_2 e^{s_2 t}) \times 10^{-3} A = C \{ [200e^{-20t} - 300e^{-30t}] v \}$$

OR

$$[s_1 = s_1' \quad s_2 = s_2']$$

$$\Rightarrow 200C = A_1' = 40 \times 10^{-3}$$

$$\Rightarrow C = 200 \times 10^{-6} F \Rightarrow C = 200 \mu F$$

Using Equ (c) & (d)

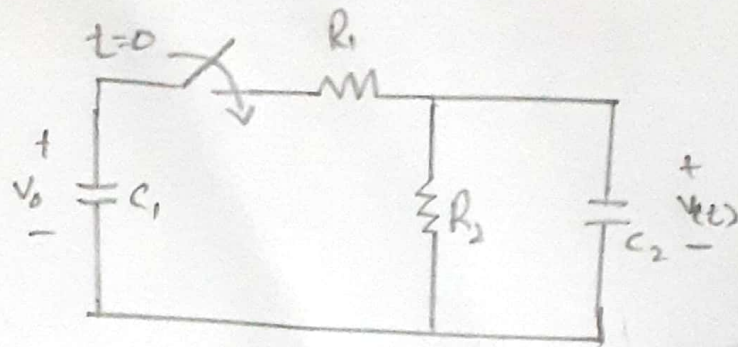
$$L = \frac{1}{200C} F = \frac{1}{200 \times 200 \times 10^{-6}} \Rightarrow L = 25 H$$

$$\Sigma \quad R = 30L = 30 \times 25 = 750 \Omega$$

$$\left. \begin{array}{l} C = 200 \mu F \\ L = 25 H \\ R = 750 \Omega \end{array} \right\}$$

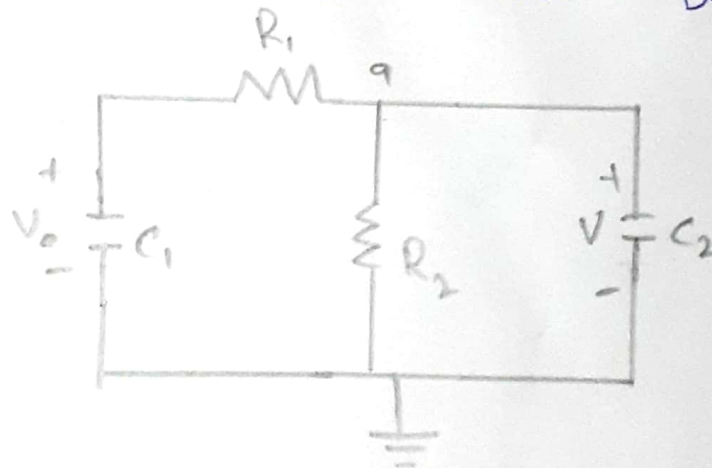
Answer.

Q4 The circuit in Fig. 3 is the electrical analog of body Function



For $t = 0^-$, $v(0) = 0$

For $t > 0$ the circuit is shown below.



$$V_0 - v/R_1 = (v/R_2) + C_2 dv/dt$$

$$V_0 = v(1 + R_1/R_2) + R_1 C_2 dv/dt$$

$$60 = (1 + 5/2.5) + (5 \times 10^6 \times 5 \times 10^6) dv/dt$$

$$60 = 3v + 25 dv/dt$$

$$v(t) = v_s + [Ae^{-3t/25}]$$

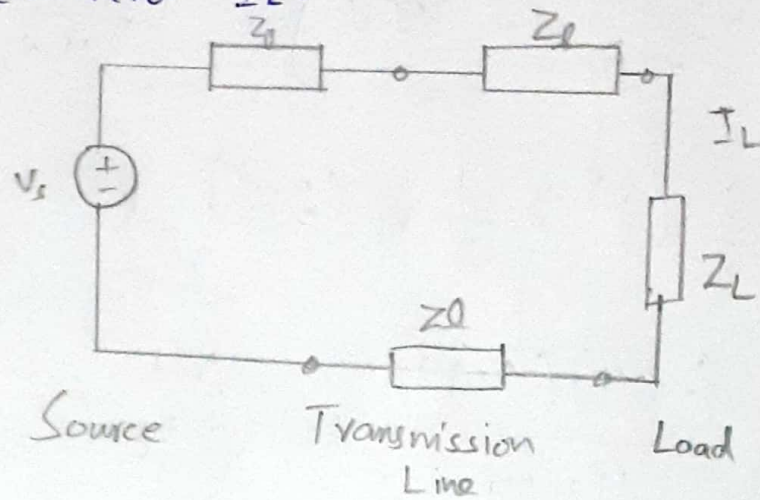
where

$$3v_s = 60 \text{ yields } v_s = 20$$

$$V(0) = 0 = 20 + A \text{ or } A = -20$$

$$V(t) = 20(1 - e^{-3t/25}) \text{ V.}$$

Q5 A power transmission system is modeled as shown. Find the load current I_L .



$$Z = Z_a + 2Z + Z_e$$

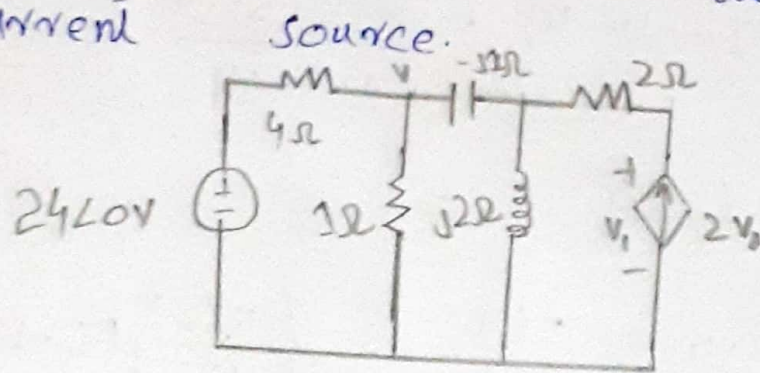
$$= (1 + 0.8 + 23.2) + j(0.5 + 0.6 + 18.9)$$

$$Z = 25 + j20$$

$$I_L = \frac{V_s}{Z} = \frac{115 \angle 0^\circ}{32.02 \angle 38.66^\circ}$$

$$I_L = 3.592 \angle -38.66^\circ \text{ A}$$

Q6) For the circuit in Fig. 5 find the average current



Consider the circuit as shown

At node 0

$$\frac{24 - V_0}{4} = \frac{V_0}{1} + \frac{V_0 - V_1}{-j}$$

$$24 = (5 + j4)V_0 - j4V_1 \rightarrow (1)$$

At node 1

$$\frac{V_0 - V_1}{-j} + 2V_0 = \frac{V_1}{j2}$$

$$V_1 = (2 - j4)V_0 \rightarrow (2)$$

Substituting (2) into (1)

$$24 = (5 + j4 - j8 - 16)V_0$$

$$V_0 = \frac{-24}{11 + j4}, \quad V_1 = \frac{(-24)(2 - j4)}{11 + j4}$$

Voltage across the dependent source is

$$V_2 = V_1 + (2)(2V_0) = V_1 + 4V_0$$

$$V_2 = \frac{-24}{11+j4} (2 - \cancel{4}j4 +) = \frac{(-24)(6-j4)}{11+j4}$$

$$S = \frac{1}{2} V_2 I^* = \frac{1}{2} V_2 (2V_0^*)$$

$$S = \frac{(-24)(6-j4)}{11+j4} \cdot \frac{-24}{11-j4}$$

$$= \left(\frac{576}{137} \right) (6-j4)$$

$$S = 25.23 - j16.82 \text{ VA}$$

Q7

A balanced Y-load to a 60Hz three phase ————— Phase draw 5KW.

(a) Determine the load impedance Z

(b) Find I_a , I_b & I_c .

(a) Step 1

$$|V_{ab}| = \sqrt{3}V_p = 240 \rightarrow V_p = \frac{240}{\sqrt{3}} = 138.56$$

$$V_{ab} = V_p \angle -30^\circ$$

$$P_f = 0.5 = \cos\phi \rightarrow \phi = 60^\circ$$

$$P = S \cos\phi \rightarrow S = \frac{P}{\cos\phi} = \frac{5}{0.5} = 10 \text{ KVA}$$

$$Q = S \sin\phi = 10 \sin 60 = 8.66$$

$$S_p = 5 + j8.66 \text{ KVA}$$

But

$$S_p = \frac{V_p^2}{Z_p} \rightarrow Z_p = \frac{V_p^2}{S_p} = \frac{138.56^2}{(5 + j8.66) \times 10^3}$$

$$= 0.96 - j1.663$$

$$Z_p = 0.96 + j1.663 \Omega$$

(b) Step 2

$$I_a = \frac{V}{Z_r} = \frac{138.56 \angle -30^\circ}{0.96 + j1.6627} = 72.17 \angle -90^\circ \text{ A}$$

$$I_b = I_a \angle -120^\circ = 72.17 \angle -210^\circ \text{ A}$$

$$I_c = I_a \angle +120^\circ = 72.17 \angle 30^\circ \text{ A}$$