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Subject : structure
Analysis - II

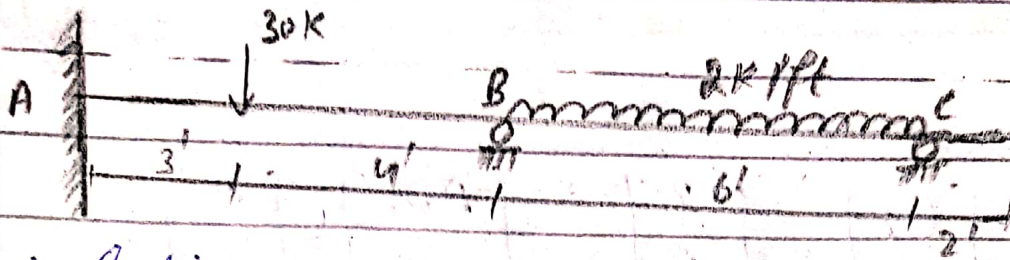
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Department : Civil
Engineering

Date : 25 sept 2020

(2)

Q NO. 1.



Solution:-

Step # 1.

Determining Kinematic Indeterminacy

$$K.I = 5^{\circ}$$

So we have to reduce the extended portion.



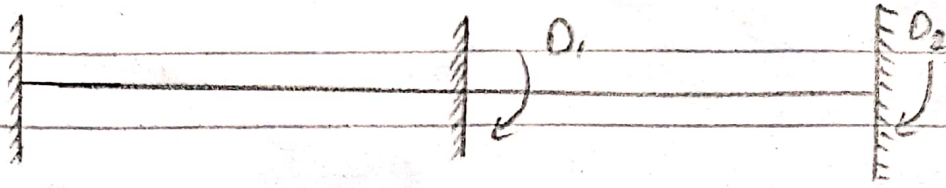
$$\frac{2(2)}{1} = 4K \cdot ft.$$

Now $K.I = 2^{\circ}$.

Step # 2:

Determine unknown joint Displacement.

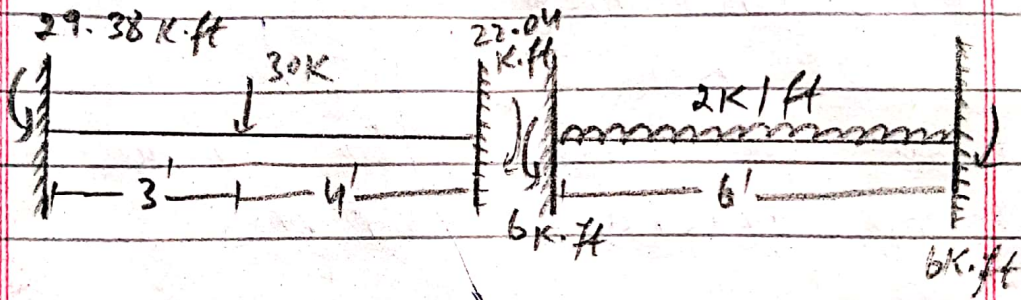
(3)



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

step #3:

compute $[ADL]$ matrix.



→ For Point Load (not at mid)

→ For Left end:-

$$\frac{Pab^2}{L^2} = \frac{(30)(3)(4)^2}{7^2} \Rightarrow 29.38 \text{ K-ft}$$

→ For right end:-

$$\frac{Pa^2b}{L^2} = \frac{(30)(3^2)(4)}{(7)^2} \Rightarrow 22.04 \text{ K-ft}$$

For uniformly Distributed load :-

(4)

$$\frac{WL^2}{12} \Rightarrow \frac{(2 \times 6)^2}{12} = 6 \text{ K.ft}$$

$$ADL_1 = +22.04 - 6 = 16.04 \text{ K.ft}$$

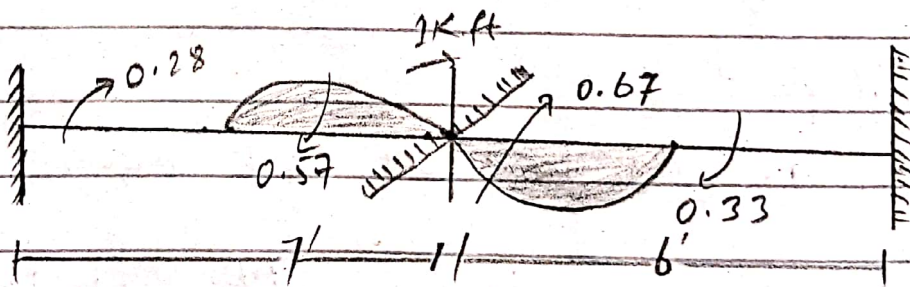
$$ADL_2 = 6 \text{ K.ft}$$

Step # 4:

Now compute [S]
Matrix.

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

a) $D_1 = 1 \text{ K}$, $D_2 = 0$.



$$\frac{4EI}{7} = 0.57$$

$$\frac{2EI}{6} = 0.33$$

$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{7} = 0.28$$

$$S_{11} = 0.57 + 0.67$$

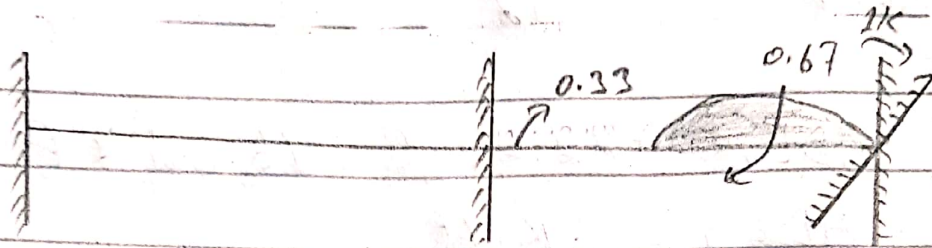
$$S_{11} = 1.24 EA$$

$$S_{21} = 0.33 EA$$

(5)

b) $D_1 = 0$

$D_2 = 1K$



$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$S_{12} = 0.33$$

$$S_{22} = 0.67$$

$$S = \begin{bmatrix} 1.94 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$$

Step # 5:

Now compute [D] Matrix.

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}^{-1} \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$\Rightarrow \frac{1}{\begin{bmatrix} 1.94 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}} \times \text{Adj } A \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

(6)

$$[S] = (1.24 \times 0.67) - (0.33 \times 0.33)$$
$$\Rightarrow 0.8308 - 0.1089$$

$$[S] = 0.7219$$

$$\text{Adj } A = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}$$

Now

$$\begin{bmatrix} AD_1 - ADL_1 \\ AD_2 - ADL_2 \end{bmatrix} = \begin{bmatrix} 0 - 16.04 \\ 4 - 6 \end{bmatrix} = \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} E$$

$$\Rightarrow \begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \frac{1}{|S|} \times \text{Adj } A \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

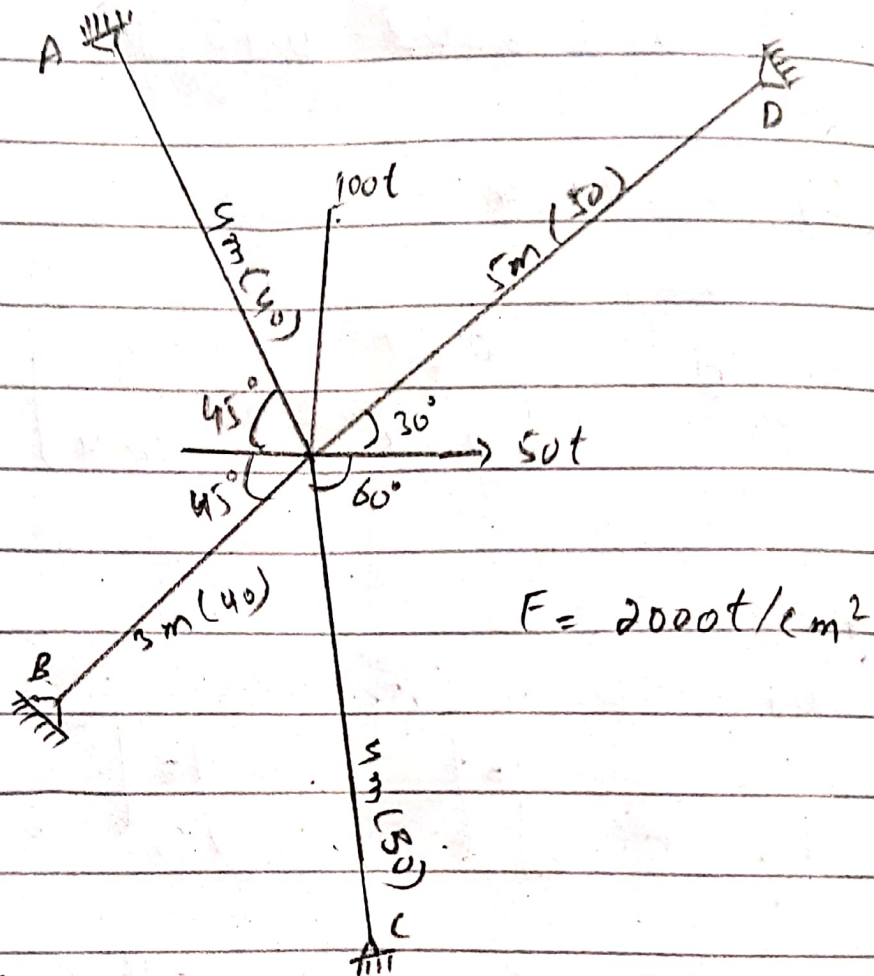
$$\Rightarrow \frac{\begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}}{0.7219}$$

$$\begin{bmatrix} 0.919 & -0.452 \\ -0.452 & 1.70 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.83 \\ 3.85 \end{bmatrix}$$

(7)

QNO 2.



Sol :-

For A

$$\sin 45^\circ = P/H = P/4$$

$$\rightarrow P = 2.828 \text{ m}$$

$$\cos 45^\circ = b/H = \frac{b}{4}$$

$$\rightarrow b = 2.828 \text{ m}$$

(8)

For B.

$$\sin 45 = P/H = P/3$$

$$\rightarrow P = 2.12 \text{ m}$$

$$\cos 45 = b/H = b/3$$

$$\rightarrow b = 2.12 \text{ m}$$

For C.

$$\sin 60 = P/H = P/4$$

$$\sin (60) \cdot (4) = P$$

$$\rightarrow P = 3.46$$

$$\cos 60 = b/H = \frac{b}{4}$$

$$\cos 60 = b/H = b/4$$

$$\cos 60 \times 4 = b$$

For D

$$\sin 30 = P/5$$

$$\rightarrow P = 2.5 \text{ m}$$

(9)

$$\cos 30^\circ = \frac{b}{5}$$

$$\rightarrow \cancel{a = 2.5 \text{ m}}$$

$$b = 4.33 \text{ m}$$

Now

$$EA(A) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(B) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(C) = 2000 \times 50 = 100,000 \text{ t}$$

$$EA(D) = 2000 \times 50 = 100,000 \text{ t}$$

Step # 1 :-

$$KI = 2j - 8$$

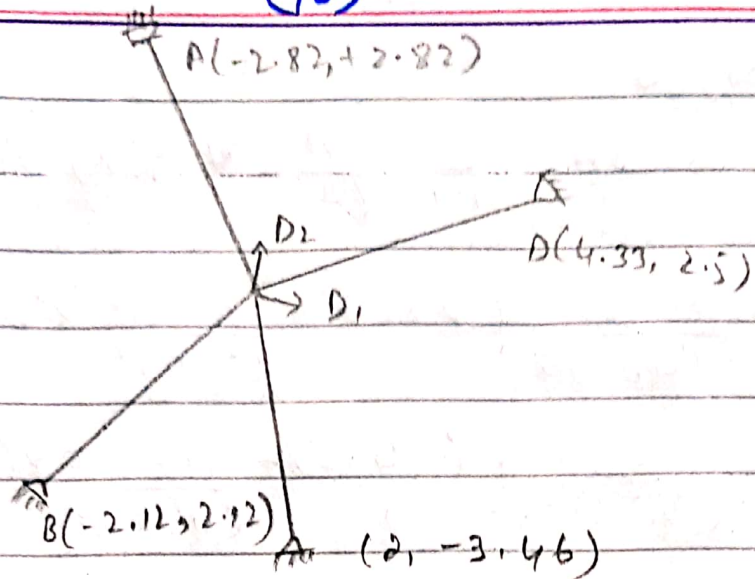
$$= 2(5) - 8$$

$$KI = 2^0$$

Step # 2 :-

select Unknown joint displacement

(10)



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

Step # 3 :-

$$[AMD]_{4 \times 3} [S]_{2 \times 2}$$

i) $D_1 = 1K$, $D_2 = 0$

$$AMD = \frac{EA}{L^2} (X_k - X_j)$$

$$AMD_{11} = \frac{80,000 \times (0 + 282)}{(400)^2} = 142$$

$$AMD_{21} = \frac{80,000 \times (0 + 212)}{(300)^2} = 188.44$$

$$AMD_{31} = \frac{100,000 \times (0 - 433)}{(500)^2} = -173.2$$

$$AMD_{41} = \frac{100,000 \times (0 - 200)}{(400)^2} = -125$$

(11)

Now

$$S_{11} = \sum_{i=1}^m \frac{EA}{L^3} (x_k - x_j)^2$$

$$= \frac{80,000}{(400)^3} (282)^2 + \frac{80,000}{(300)^2} (212)^2$$

$$+ \frac{100,000}{(500)^3} (-433)^2 + \frac{100,000}{(400)^3} (-200)^2$$

$$S_{11} = 99.405 + 133.107 + 149.991 + 62.5$$

$$\boxed{S_{11} = S_{21} = 445.063}$$

$$\boxed{S_{11} = 445.063}$$

$$\Rightarrow S_{12} = S_{21} = \sum_{i=1}^m \frac{EA}{L^3} x (x_k - x_j) (y_k - y_j)$$

$$\Rightarrow \frac{80,000}{(400)^3} (282)(-282) + \frac{80,000}{(300)^3} (212)$$

$$(212) + \frac{100,000}{(500)^3} (-433)(0-250) +$$

$$\frac{100,000}{(400)^3} (-200)(0+346)$$

$$\boxed{S_{12} = S_{21} = 12.237}$$

(12)

$$ii) D_1 = 0 \quad D_2 = 1K'$$

$$AMD = \frac{EA}{L^2} (Y_K - Y_j)$$

$$AMD_{12} = \frac{80,000}{(400)^2} (-282) = -141$$

$$AMD_{22} = \frac{80,000}{(300)^2} (212) = 188.44$$

$$AMD_{32} = \frac{100,000}{(500)^2} (-250) = -100$$

$$AMD_{42} = \frac{100,000}{(400)^2} (346) = 216.25$$

$$\text{Now, } S_{22} = \sum_{i=1}^m \frac{EA}{L^3} (Y_K - Y_j)^2$$

$$= \frac{80,000}{(400)^3} (-282)^2 + \frac{80,000}{(300)^3} (212)^2$$

$$+ \frac{100,000}{(500)^3} (-250)^2 + \frac{100,000}{(400)^3} (346)^2$$

$$S_{22} = 469.628$$

(13)

Step # 4:

$$[D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.003 & 12.237 \\ 12.237 & 469.628 \end{bmatrix}^{-1} \times \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

Step # 5:

$[AM]$

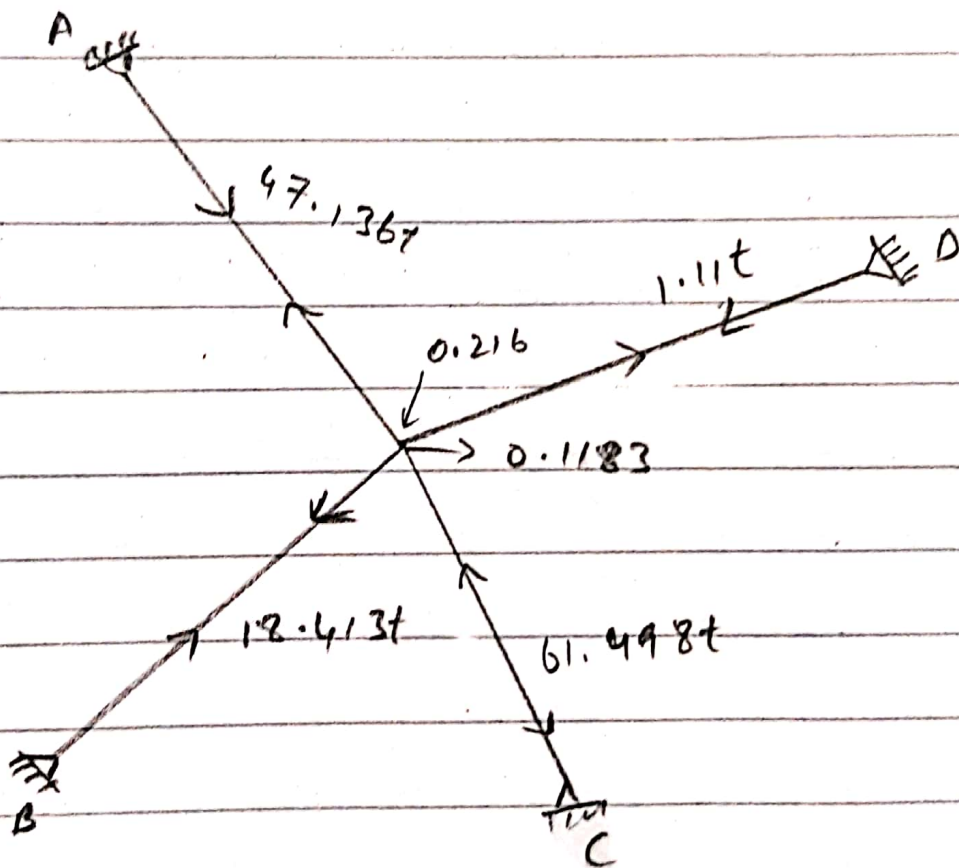
$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.44 & 188.44 \\ -173.2 & -100 \\ -125 & 216.25 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + (188.44) \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ -125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 16.68 + 30.46 \\ 22.29 - 40.70 \\ -20.49 + 21.6 \\ -14.79 + 46.71 \end{bmatrix}$$

(14)

$$\Rightarrow \begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 47.136t \\ -18.413t \\ 1.11t \\ -161.498t \end{bmatrix}$$



QNO. 3.

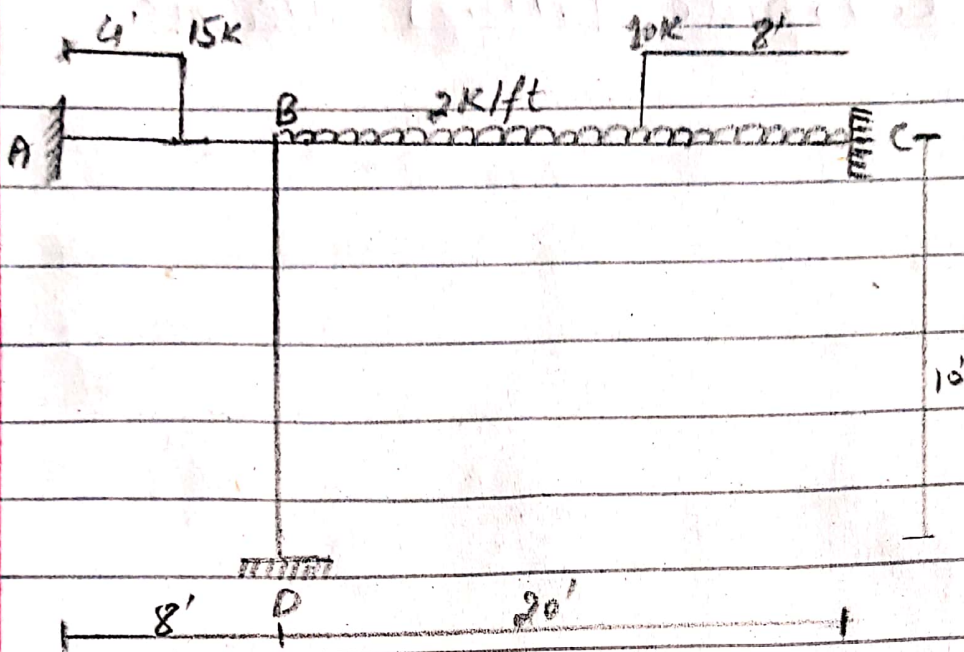


Figure - 2.

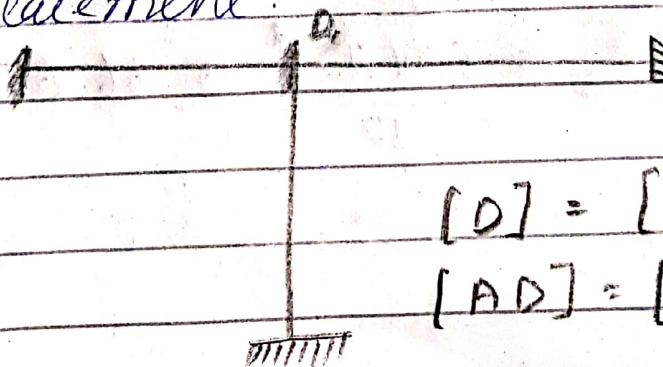
sol:-

Step # 1.

Determine Kinematic
indeterminacy.

$$K.I = 1^{\circ}$$

Step # 2:

Determine Unknown Joint
Displacement.

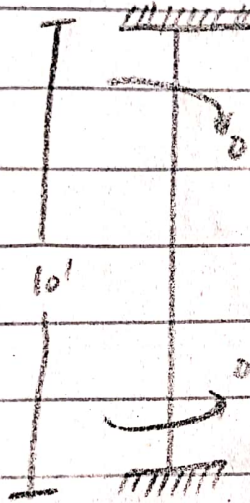
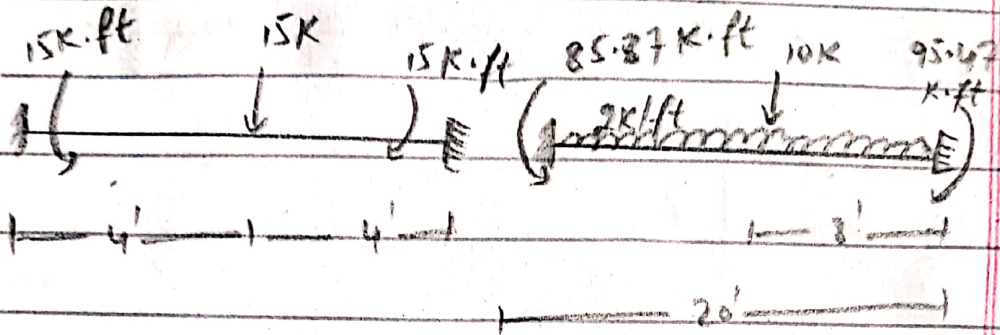
$$[0] = [?]$$

$$[AD] = [0]$$

(16)

Step # 3 :-

Compute [ADL] Matrix



⇒ Point load at center =

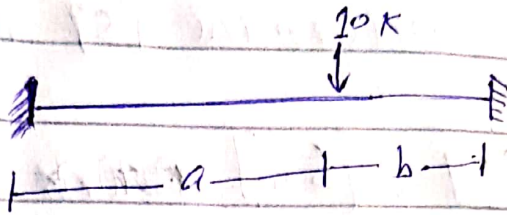
$$\frac{PL}{8} \Rightarrow \frac{(15)(8)}{8} = 15 \text{ Kip}\cdot\text{ft}$$

⇒ Uniformly Distributed load :-

$$\frac{WL^2}{12} \Rightarrow \frac{(2)(20)^2}{12} \Rightarrow 66.67 \text{ K}\cdot\text{ft}$$

(17)

⇒ Point load (Not at mid) :-
Suppose



For left end :-

$$\frac{P a b^2}{L^2} \Rightarrow \frac{(10)(12)(8)^2}{(20)^2} = 19.2 \text{ K.ft}$$

For Right End :-

$$\frac{P a^2 b}{L^2} = \frac{(10)(12)^2(8)}{(20)^2} = 28.8 \text{ K.ft}$$

So total moment at left end :-

$$19.2 + 66.67 = 85.87 \text{ K.ft.}$$

Similarly at right End :-

$$28.8 + 66.67 = 95.47 \text{ K.ft}$$

$$\text{So } [ADL] = -85.87 + 15 = -70.87 \text{ K.ft}$$

(18)

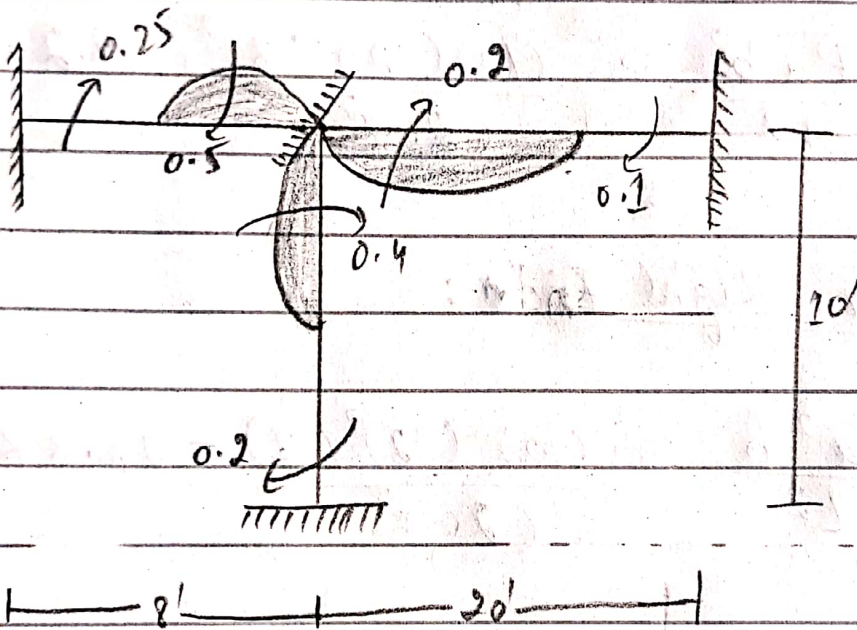
Step # 4 :-

Determine $[S]$ Matrix.

$$[S] = [S_{11}]$$

Now

$$D = 1K$$



$$\Rightarrow \frac{4EI}{8} = 0.5 \quad \frac{2EI}{8} = 0.25$$

$$\Rightarrow \frac{4EI}{20} = 0.2 \quad \frac{2EI}{20} = 0.1$$

$$\Rightarrow \frac{4EI}{10} = 0.4 \quad \frac{2EI}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2) EI$$

$$= 1.1 EI$$

(19)

$$[S] = 1.1 EI$$

Step # 5 :-

Comput [D] Matrix

$$[D] = [S]^{-1} \times [AD] - [ADL]$$

$$[D] = \frac{1}{1.1} \times [0] - [-70.87]$$

$$\Rightarrow \frac{70.87}{1.1}$$

$$[D] = [64.42] \text{ I/EI}$$