

Course Details

Course Title: Power System Analysis  
 Instructor:

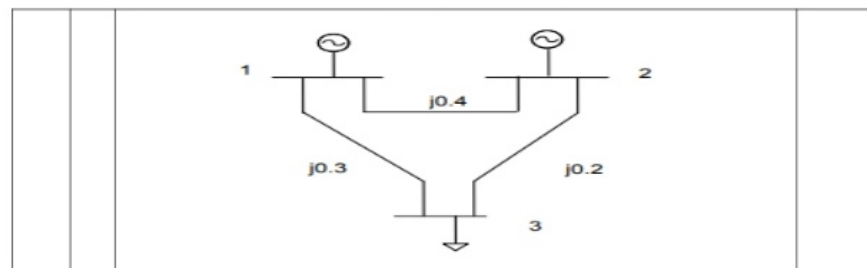
Module: 6th  
 Total Marks: 30

Student Details

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Student ID:  
 13909

Q1.	(a)	A 3 $\Phi$ transformer is connected with a residential load of 28.56 KV; the primary side of a transformer is connected with 130 KV feeder while secondary side is stepped down to 10 KV. The transformer is rated with 30 MVA. Find impedance $Z_{br}$ .	Marks 05 CLO 1
	(b)	Find the Per Unit equivalent impedance of an 11/132 KV transformer having 10 $\Omega$ and 1440 $\Omega$ , the equivalent impedance. The primary and secondary currents are 909 Amp and 75.75 Amps respectively.	Marks 05 CLO 1
.Q2	(a)	Single line diagram of a 3 $\Phi$ power system is shown in the below figure. Draw an impedance and reactance diagram in P.U.	Marks 10 CLO 2
Q3	(a)	For the single line diagram shown below, Generators are connected to high tension buses 1 and 2 and supply to load connected at bus 3. Find the reactance diagram, then convert it into equivalent current sources and shunt admittances. Then find the admittance matrix and find the total current.	Marks 10 CLO 2



Q1

(A) - A  $3\phi$  T/F is connected with a residential load of 28.56 kW. The primary side of T/F is connected with 130 kV feeder while secondary side is stepped down to 10 kV. The T/F is rated with 30 MVA. Find impedance  $Z_b$ .

Solution  $\Rightarrow$ 

$$\text{Primary} = 130 \text{ kV}$$

$$\text{Secondary} = 10 \text{ kV}$$

$$\text{T/F Rated} = 30 \text{ MVA}$$

$Z_b$  across  $V_{base1}$  (130 kV)

$$Z_b = \frac{(130 \times 10^3)^2}{30 \text{ MVA}} = \frac{16900000000}{30000000}$$

$$Z_b = 56.33 \text{ Ans}$$

(B) Find the per unit equivalent impedance of an 11/132 kV Transformer having  $10 \Omega$  and  $1440 \Omega$ . The equivalent impedance. The primary and secondary current are 909 Amp and 75.75 Amps respectively.

Solution =  $\begin{matrix} \text{primary} \\ 11 \end{matrix} / \begin{matrix} 132 \text{ kV} \\ \text{secondary} \end{matrix}$

we know that for  $S_{base1}$

$$I_{base1} = \frac{S_{base1}}{V_{base1}}$$

$$\begin{aligned} S_{base1} &= V_{base1} \times I_{base1} \\ &= 11 \times 10^3 \times 909 \text{ Amp} \end{aligned}$$

$$S_{base1} = 9999000$$

$\Rightarrow Z_b$  across  $V_{base2}$  (10 kV)

$$Z_b = \frac{(10 \times 10^3)^2}{30 \text{ MVA}}$$

$$= \frac{700000000}{30000000}$$

$$\boxed{Z_b = 3.33} \quad \text{Ans} =$$

Now  $S_{base2}$   
~~←~~ // ~~→~~

$$S_{base2} = V_{base2} \times I_{base2}$$

$$= 132 \times 10^3 \times 75.75 \text{ Amp}$$

$$S_{base2} = 9999000$$

Now  $Z_{base1} =$   
 // - //

$$Z_{base1} = \frac{(V_{base1})^2}{S_{base1}} = \frac{(11 \times 10^3)^2}{9999000} = 12.101$$

$$Z_{base1} = 12.101$$

Now  $Z_{base2}$   
 // // //

$$Z_{base2} = \frac{(V_{base2})^2}{S_{base2}} = \frac{(132 \times 10^3)^2}{9999000} = 1742.574$$

$$Z_{base2} = 1742.574$$

=> Now per unit equivalent impedance  
for  $Z_{base1}$

$$\Rightarrow Z_{base1} \text{ eq. p.u.} = \frac{Z_{eq1}}{Z_{base1}} = \frac{10 \Omega}{12.101}$$

$$Z_{base1} \text{ eq. p.u.} = 0.826$$

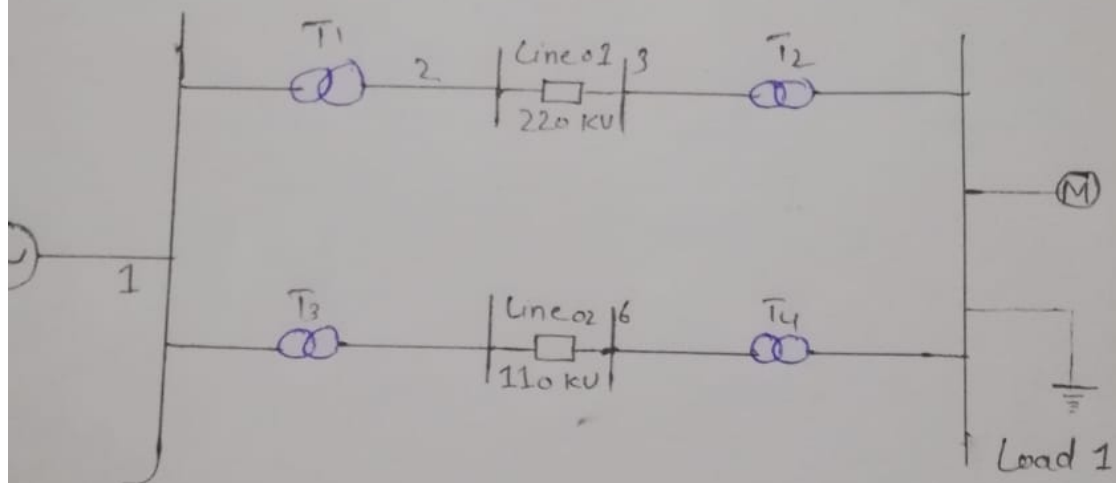
=> for  $Z_{base2}$

$$Z_{base2} \text{ eq. p.u.} = \frac{Z_{eq2}}{Z_{base2}} = \frac{1440 \Omega}{1742.574} = 0.826$$

$$Z_{base2} \text{ eq. p.u.} = 0.826$$

(a) Single line diagram of a 3 $\phi$  power system is shown in the below figure.

Draw an impedance and reactance diagram in p.u.



=> Impedance diagram =>  
" " " "

=> When we convert an single line-  
diagram <sup>convert</sup> into impedance diagram

So we remove circuit breaker

and draw resistor and inductor

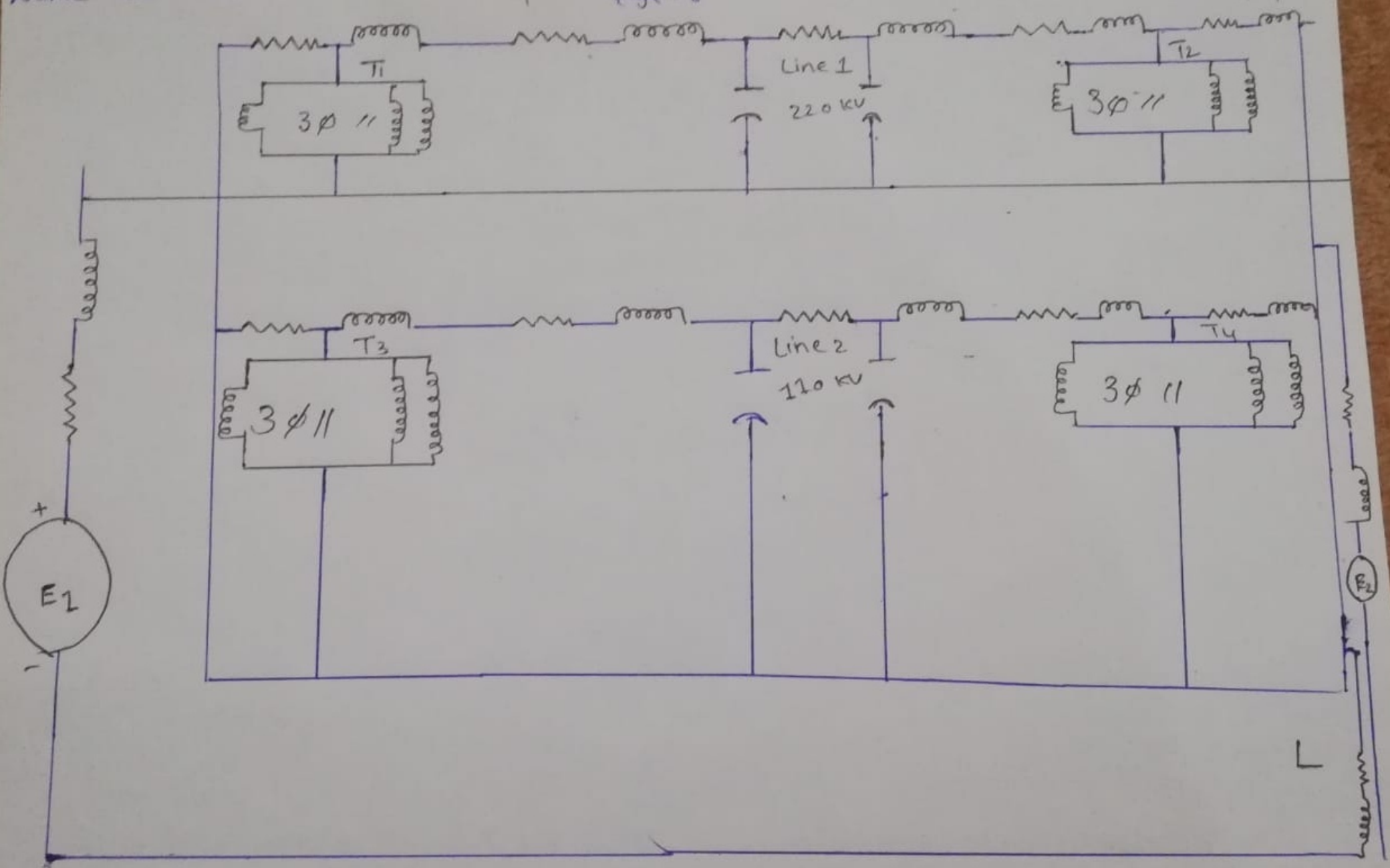
in impedance diagram instead of

circuit breaker and also generator ( $G_1$ )

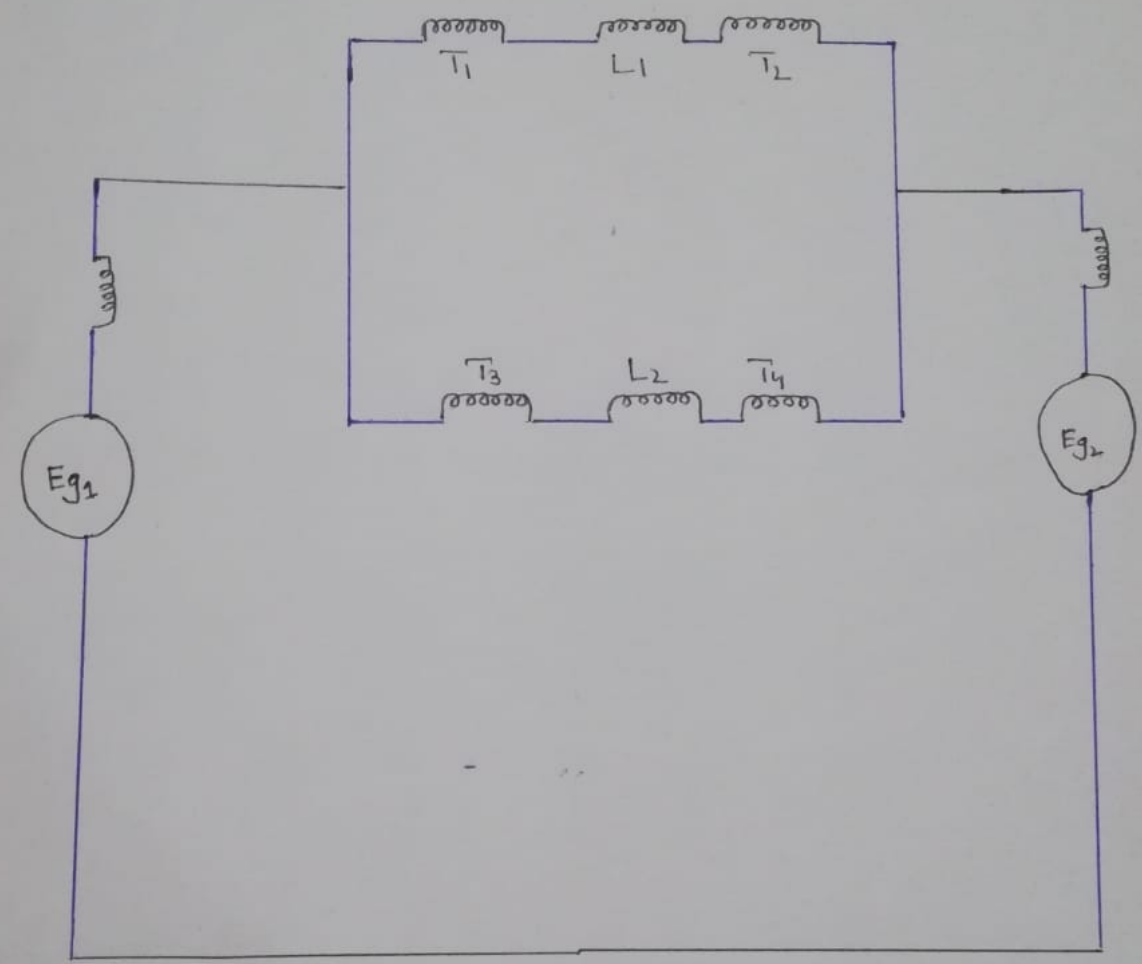
convert into EMF ( $E$ ).

=> So now we explain that  
with the help of diagram



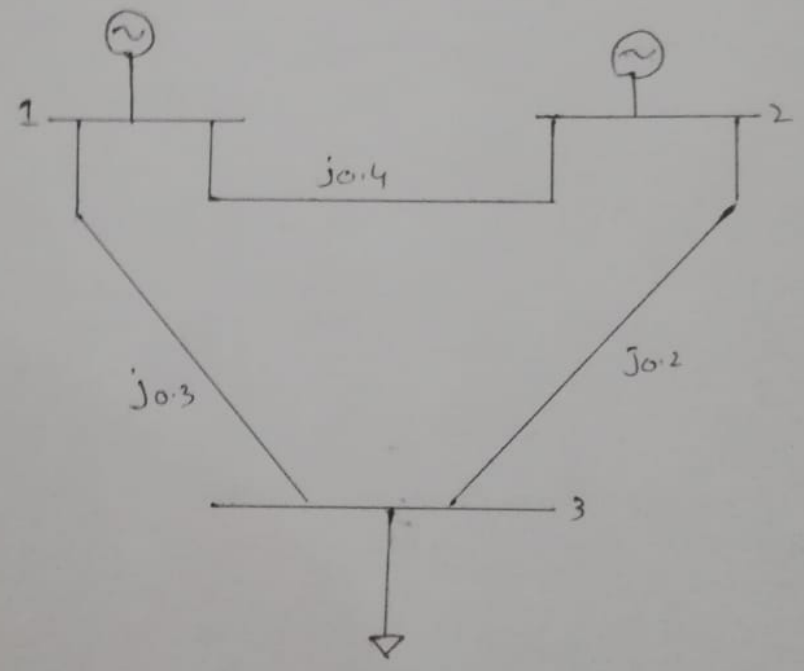


Single Line diagram convert To impedance diagram



Single Line diagram convert into Reactance diagram.

(9) Find the reactance diagram, then convert it into equivalent current source and shunt admittances. then find the admittance matrix and find the total current.



=> Reactance diagram =

=> When we convert an single-line diagram into reactance diagram so all the resistance

capacitor we remove only

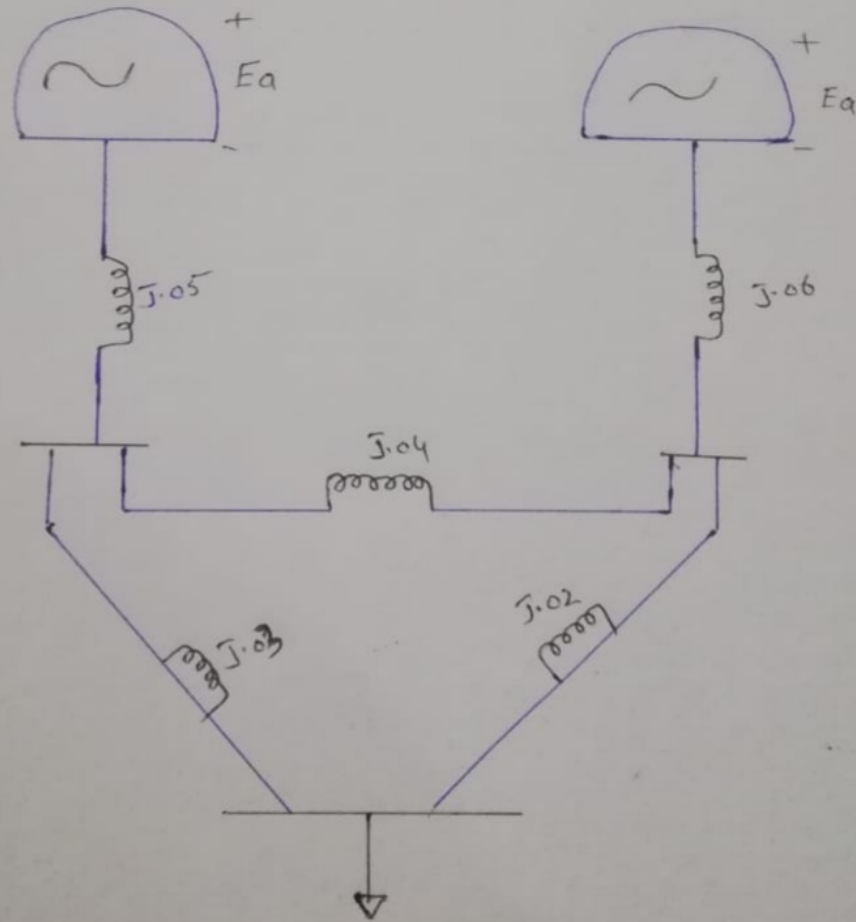
Inductor we draw in

Reactance diagram.

=> Now we explain an

Reactance diagram with

the help of diagram



Now Calculation  $\Rightarrow$

$$\frac{1}{j \cdot 0.8} = 160$$

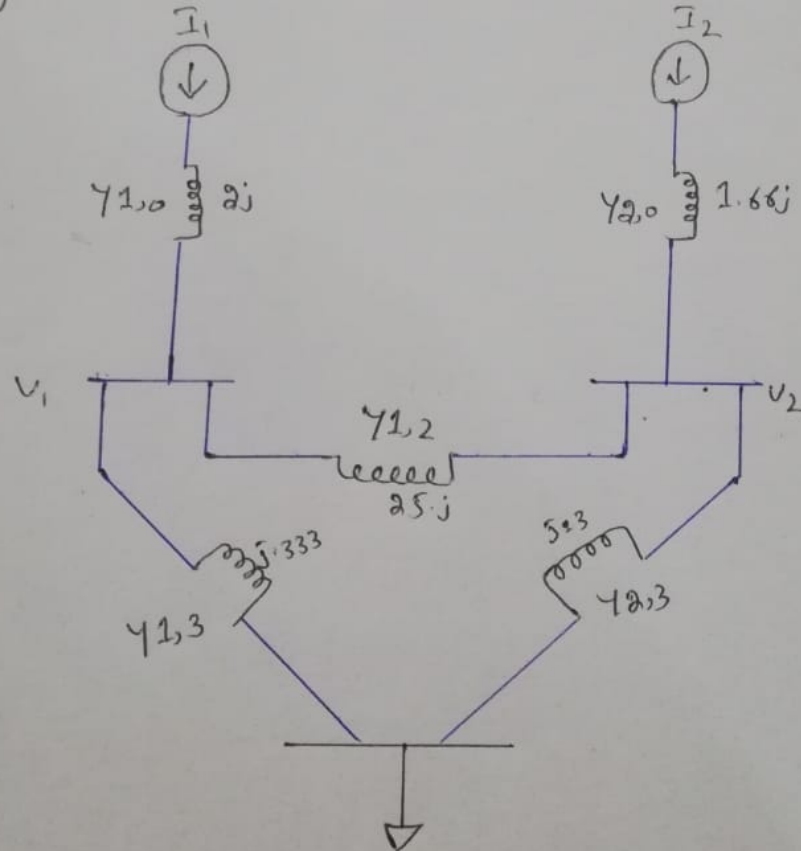
$$\frac{1}{j \cdot 0.5} = 2$$

$$\frac{1}{j \cdot 0.4} = 2.5$$

$$\frac{1}{j \cdot 0.3} = 3.33$$

$$\frac{1}{j \cdot 0.2} = 5$$

$\Rightarrow$  So now we convert the reactance diagram into Admittance.



Node(1)

so

$$\bar{I}_1 = Y_{1,0} v_2 + Y_{1,2} (v_1 - v_2) + Y_{1,3} (v_1 - v_3)$$

$$[Y_{1,0} v_1 + Y_{1,2} v_1 - Y_{1,2} v_2 + Y_{1,3} v_1 - Y_{1,3} v_3]$$

Now  $v_1$  common  $\Rightarrow$

$$v_1 = v_1 (Y_{1,0} + Y_{1,2} + Y_{1,3}) - Y_{1,2} v_2 - Y_{1,3} v_3$$

$$\bar{I}_1 = v_1 [Y_{1,0} + Y_{1,2} + Y_{1,3}] - Y_{1,2} v_2 - Y_{1,3} v_3$$

$\rightarrow$  eq (1)

Now

Node(2)

$$\bar{I}_2 = Y_{2,0} v_2 + Y_{1,2} (v_2 - v_1) + Y_{2,3} (v_2 - v_3)$$

$$\text{Common} \rightarrow [-Y_{1,2} v_1]$$

$$= -Y_{1,2} v_1 (Y_{2,0} + Y_{1,2} + Y_{2,3})$$

$$[v_2 - v_{2,3} - v_3]$$



$$\bar{I}_2 = Y_{1,2} V_1 [Y_{2,0} + Y_{1,2} + Y_{2,3}]$$

$$V_2 - V_{2,3} V_3 \rightarrow \text{eqn (2)}$$

Now nod (3)

$$0 = Y_{2,3} [V_3 - V_2] + Y_{1,3} [V_3 - V_1]$$

$$0 = [Y_{2,3} V_3 - Y_{2,3} V_2 + Y_{1,3} V_3 - Y_{1,3} V_1]$$

→ equation (3)

Now admittance matrix

$$\begin{bmatrix} \bar{I}_1 \\ \bar{I}_2 \\ \bar{I}_3 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} & Y_{13} \\ Y_{21} & Y_{22} & Y_{23} \\ Y_{31} & Y_{32} & Y_{33} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix}$$

⇒ So  $Y_{11}$ ,  $Y_{22}$ ,  $Y_{33}$  admittance is called self admittance.