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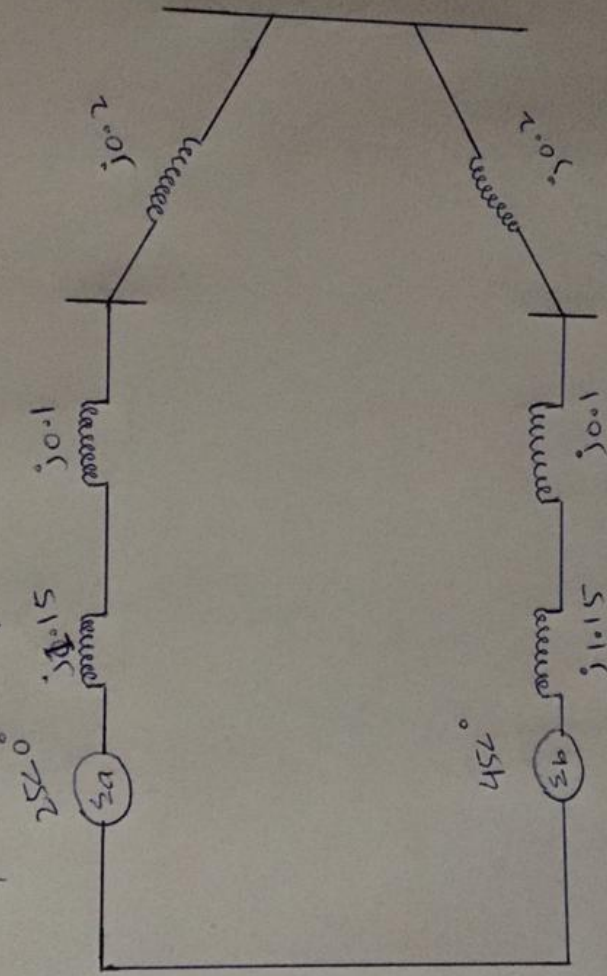
①

Q1: Ans

$$Z_a = 2.5 \angle 0^\circ$$

$$Z_b = 4.5 \angle 0^\circ$$

$\Rightarrow I_n$ per unit



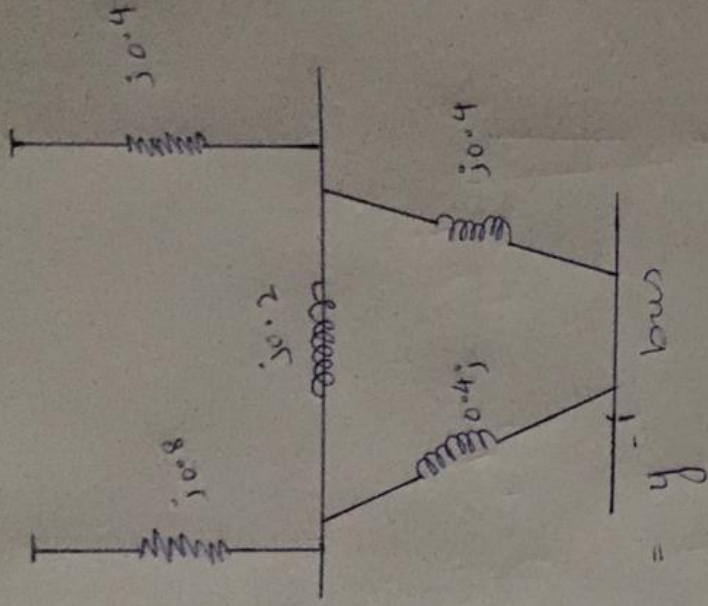
$$I_1 = I_2 = \frac{2.5 \angle 0^\circ}{j0.2}$$

$$I_2 = \frac{4.5 \angle 0^\circ}{j0.2}$$

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Q2: Ans

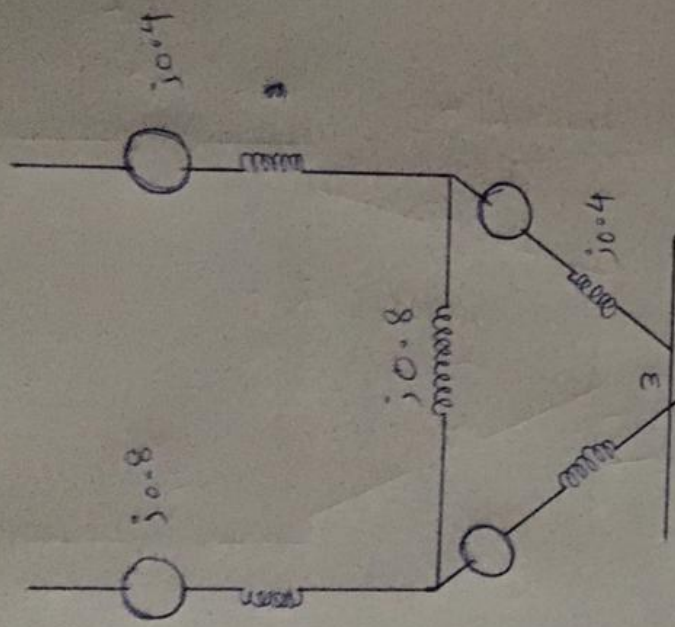


$Z_{base} = Y^{-1}_{bus}$

$$Z_{base} \begin{bmatrix} Z_{11} & Z_{12} & Z_{13} \\ Z_{21} & Z_{22} & Z_{23} \\ Z_{31} & Z_{32} & Z_{33} \end{bmatrix}$$

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$$\begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} & Z_{13} \\ Z_{21} & Z_{22} & Z_{23} \\ Z_{31} & Z_{32} & Z_{33} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}$$

Now

$$V_1 = Z_{11} I_1 + Z_{12} I_2 + Z_{13} I_3 \quad \text{①}$$
$$V_2 = Z_{21} I_1 + Z_{22} I_2 + Z_{23} I_3 \quad \text{②}$$
$$V_3 = Z_{31} I_1 + Z_{32} I_2 + Z_{33} I_3 \quad \text{③}$$

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Q3 : Ans :

→ A 10 kw generator is connected which inject P_{GK} , Q_{GK} to the 11kV Busbar.

→ A 20 kw load is connected which takes P_{LK} , Q_{LK} from the busbar^{of} 11kV. This 11kV busbar is connected to other busbar i.e through lines.

The voltage at 11kV busbar is V_L , where V_L is equal to the magnitude V_K and the angle δ_{LK} .

→ Now we will take the algebraic sum of generation and load i.e subtract the load from generation.

i.e ; $P_K = P_{GK} - P_{LK}$ & Q_{LK} is power injection

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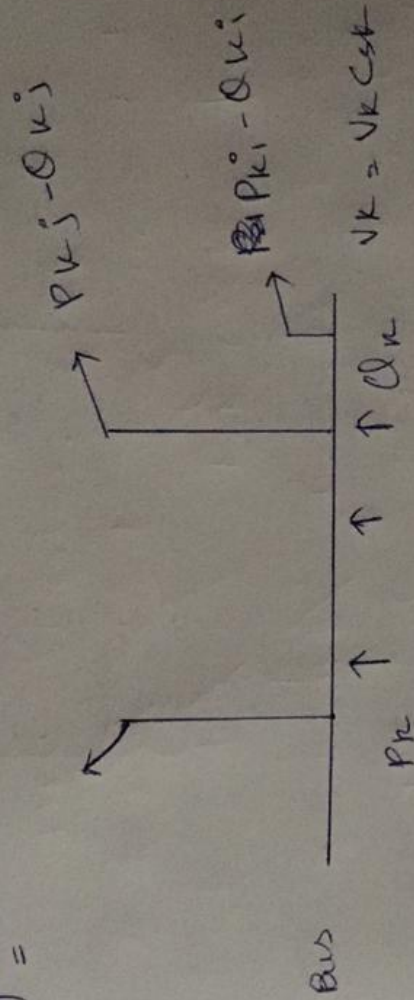
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⑤

Similarly reactive power injection

$$\text{is } Q_k = Q_{Gk} = Q_{Lk}$$

Figure =



⇒ Now as we see the injection into 11 kV busbar rather saying the generation & loads, if a particular busbar is there then there is no generation input & only load is connected

then the injection to that will be $11kV$

$$\therefore P_k = 0 - P_{Lk}$$

$$P_k = P_{Lk}$$

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∴ Real & relative power is equal to algebraic sum of P_{eD} , power going out.
→ Network equation;

$$\therefore I_{bus} = Y_{bus} V_{bus} \quad \text{--- (1)}$$

⇒ For a particular bus k , we can write an equation;

$$I_k = \sum_{n=1}^n Y_{kn} V_n \quad \text{--- (2)}$$

where n = No of bus bars.

Y_{kn} = admittance of the

element V_n = voltage phasor at

bus n .

→ From equation we can write complex power injection at bus k is;

$$S_k = P_k + jQ_k = V_k I_k \quad \text{--- (3)}$$

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⇒ All of them are negative of conjugate we can separate out the real & imaginary parts then we can write real power injection into

Bus k as

$$P_k = V_k \sum_{n=1}^N Y_{kn} V_n \cos(\delta_k - \delta_n - \theta_{kn})$$

Similarly reactive power injection

$$Q_k = V_k \sum_{n=1}^N Y_{kn} V_n \sin(\delta_k - \delta_n - \theta_{kn})$$

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Sol:

To overcome we choose

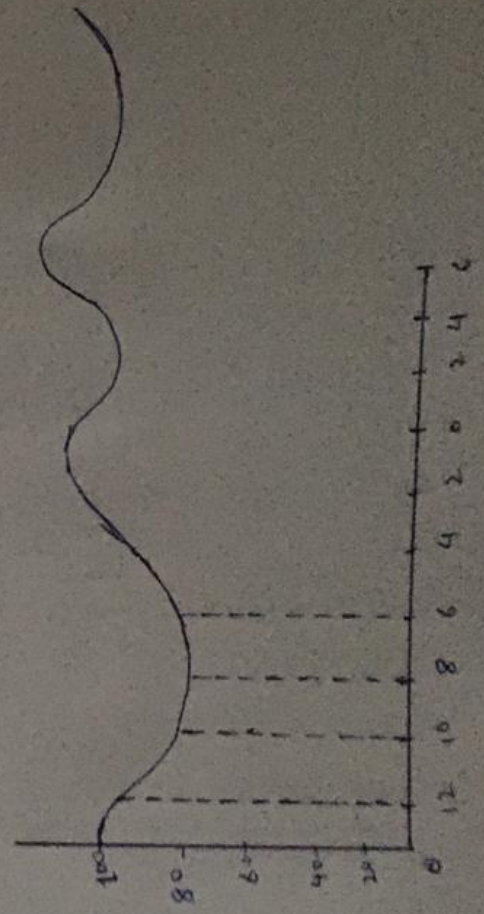
one bus as reference bus which takes poses which can find after solution so at one

bus we cannot specify the generation generally this is

a bus which has very large generation available so that there will be no problem for it.

→ this bus in power system is called slack bus.

→ Load Curve:



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Also $\sum_{n=1}^N Y_{kn} V_n$ or

$$I_k = Y_{k1} V_1 + Y_{k2} V_2 + Y_{kk} V_k + Y_{kj} V_j$$

⇒ From Above Equation;

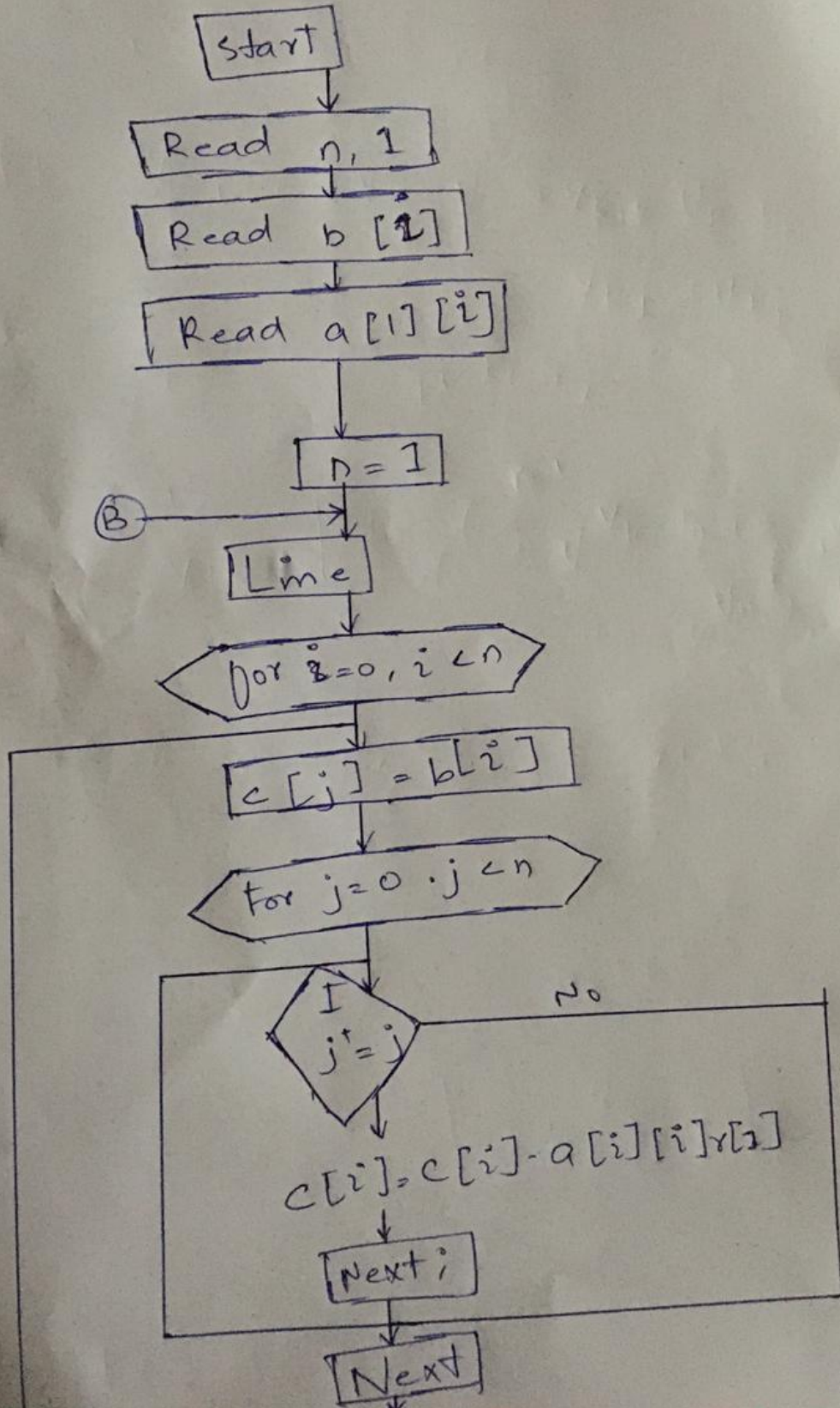
$$V_k = \frac{1}{Y_{kk}} \left[I_k - \left(\sum_{n=1, n \neq k}^N Y_{kn} V_n + \sum_{n=1, n \neq k}^N Y_{kn} V_n \right) \right]$$

where $k = 1, 2, \dots, N$.

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Q5: Ans:

⇒ This is the 1st iterative method to find power flow equation. Do this method again start with the basic of network equation.

i.e $I_{bus} = Y_{bus} V_{bus}$
for any particular bus k

$$I_k = \sum_{n=1}^N Y_{kn} V_n$$

⇒ Complex Power:

$$S_k = P_k + jQ_k = V_k I_k^*$$

$$P_k + jQ_k = V_k \left[\sum_{n=1}^N Y_{kn} V_n \right]^*$$

⇒ From Complex power:

$$I_k = \frac{P_k - jQ_k}{V_k}$$

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Q4: Ans:

⇒ There is one problem in doing power flow solution that we cannot know all the generations.

All the loads are known to us but generation are in our control and one can say that all generation are available we don't know what is the loss in the system.

⇒ we don't know the sum of loads & no. of losses must be equal to total generation

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⇒ Now we know that the value

of I_k is from eq ① when substituting I_k in eq ②

$$P_k + jQ_k = V_k \left[\sum_{n=1}^N Y_{kn} \right]$$

where $k = 1, 2, \dots, N$

⇒ V_n is a phasor which has magnitude and angles

$$V_n = V_n e^{j\theta_n}$$

$$\xi Y_{kn} = Y_{kn} e^{j\theta_{kn}}, \quad k, n = 1, 2, \dots, N$$

⇒ Substituting V_n in Y_{kn} values in

eq ③

$$P_k + jQ_k = V_k \sum_{n=1}^N Y_{kn} V_n e^{j\theta_n}$$

∴ All angles with V_k S_n with

V_n
 Q_{kn} with Y_{kn} .

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$$\therefore Q_k = 0 - Q_{Lk}$$

$$Q_k = Q_{Lk}$$

→ From the figure we see that there are three ongoing lines, to 11k0 busbar, 2nd is going to j and 3rd to mm. these lines will carry the power P_{ki} , Q_{ki} to bus j & P_{km} , Q_{km} to bus m.

→ Some of this power may be in the reverse direction i.e bus k, so the value of P_{kj} , Q_{kj} will be negative.

$$\therefore P_k = P_{ki} + P_{kj} + P_{km}$$

$$Q_k = Q_{ki} + Q_{kj} + Q_{km}$$