

# Assignment

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Subject

Differential Equation

(1)

# Application of ODEs In

Engineering:

An equation which contains derivative of one or more dependent variable of a single independent variable.

① Physical Application of ODE:

(1) Its velocity  $(v) = \frac{dx}{dt}$

(2) Its acceleration  $(a) = \frac{dv}{dt}$  or  $d^2x/dt^2$

however if a body is moving along a curve then

(1) its velocity  $(v) = \frac{ds}{dt}$

(2) Newton's second law: The rate of change of momentum encountered by a moving object equal to the Net force Applied to it in mathematical.

$$F = \frac{d(mu)}{dt} \Rightarrow m \frac{dv}{dt} + v \frac{dm}{dt} \Rightarrow F = m \frac{dv}{dt}$$

$$= F = ma$$

2)  
(3) Newton Law of cooling:  
The rate of change of the temperature of an object is proportional to the difference between its own temperature and the temperature of its surroundings.

Therefore  $d\theta/dt = EA(\theta - \theta_1)$ ;  $E$  - A constant that depends upon the object,  $A$  - surface area,  $\theta$  - A certain temperature,  $\theta_1$  - room/ambient temperature and temperature of the surrounding.

4) Radioactive half life: A stochastic (random) process.

The rate of decay is dependent upon the number of molecules/atoms that are there.

• Negative because the number is decreasing.

•  $k$  is the constant for proportionality.

$$dN/dt = -kN$$

5) Macaulay's method:

of bending becomes. The differential equation  
importantly without expanding  
the term into square brackets

$$EI_{yy} \frac{d^2 u_z}{dx^2} = -M_x = -R_A x + f_2(x-2)$$

this expression can be  
integrated twice.

6) No Damping

7) Electrical circuits

8) Light Damping

9) Computer exercise

10) Beam

11) modeling forced mech oscillation.

(4)

An equation contain partial derivatives of one or dependent variables of two or more independent variable.

## Application of PDEs in engineering

(1) Laplace equation:- Laplace equation is used to describe the steady state distribution of heat in body

• Also used to describe the steady state distribution of electric charge in body

$$\frac{\partial^2 u(x,y,z)}{\partial x^2} + \frac{\partial^2 u(x,y,z)}{\partial y^2} + \frac{\partial^2 u(x,y,z)}{\partial z^2} = 0$$

(2) heat equation:-

The function  $u(x,y,z,t)$  is used to represent the temperature at time  $t$  in a physical body at a point with coordinates  $(x,y,z)$

$\alpha$  is the thermal diffusivity it is sufficient to consider the case  $\alpha = 1$ .

$$\frac{\partial u(x,y,z,t)}{\partial t} = \alpha \left[ \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right]$$

(5) Wave equation:

The function  $u(x, y, z, t)$  is used to represent the displacement at time  $t$  of a particle whose position at rest is  $(x, y, z)$

The constant  $c$  represent the propagation speed of the wave

$$\frac{\partial^2 u(x, y, z, t)}{\partial t^2} = c^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right)$$