

NAME:-

NAVEED AHMAD

I.D:-

7880

SUBJECT:-

STRUCTUR II.

SEMS:-

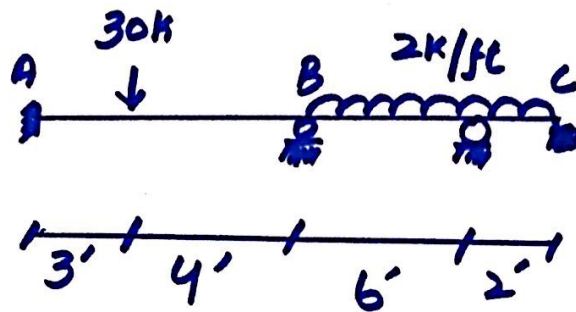
SUMMER - FINAL

DEPT:-

CIVIL.

①

QUESTION- 01

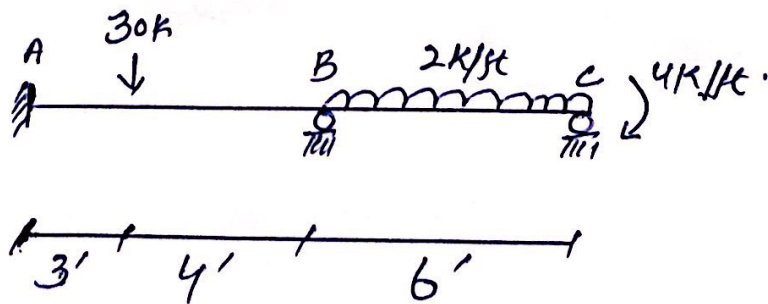


SOLUTION-

$$K \cdot I = ?$$

$$K I = 5^{\circ}$$

we have to reduce the extended portion.



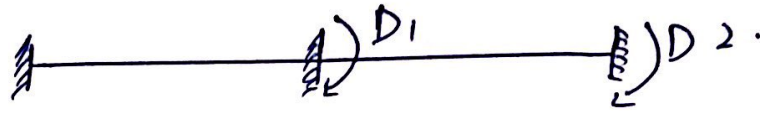
$$\Rightarrow \frac{2(2)}{1} = 4 \text{ k/ft}$$

Now $K \cdot I = 2^{\circ}$

(2)

STEP II:

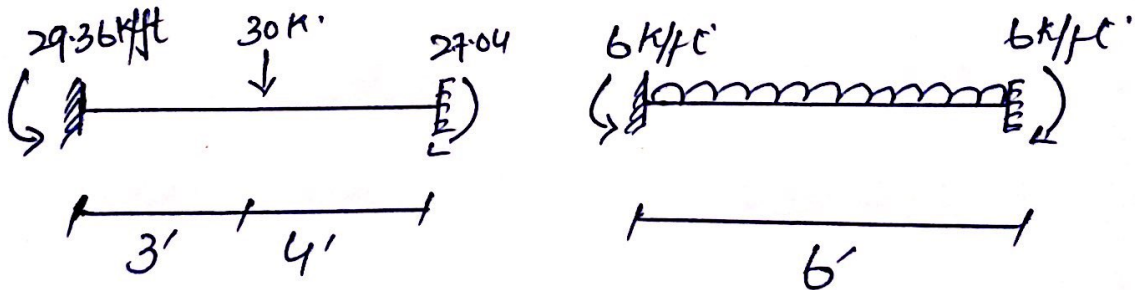
Determine unknown joint displacements



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \cdot \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

STEP III:

Compute ADL matrix



for pointed load

for left ~~hand~~ end.

$$\frac{Pab^2}{L^2} = \frac{(30)(3)(4)^2}{(7)^2} \Rightarrow 29.38 \text{ k/ft.}$$

(3)

for right end

$$\frac{Pa^2b}{L^2} = \frac{(30)(3)^2(4)}{(7)^2} = 22.04 \text{ k/ft.}$$

for UDL

$$\frac{wL^2}{12} \Rightarrow \frac{(2)(6)^2}{12} = 6 \text{ k/ft.}$$

$$ADL_1 = 22.04 - 6 = 16.04 \text{ k/ft.}$$

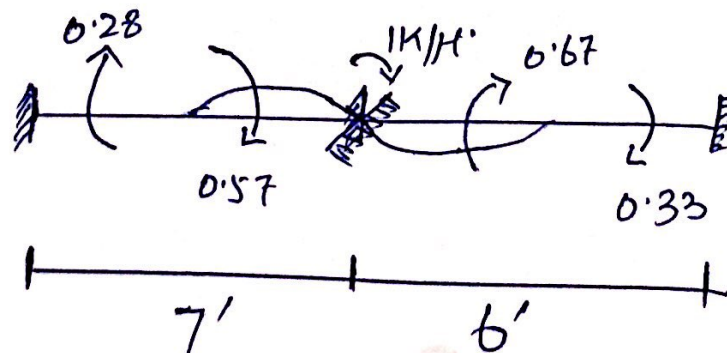
$$ADL_2 = 6 \text{ k.ft.}$$

STEP IV:-

Compute [S] matrix

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

a) $D_1 = 1k$, $D_2 = 0$



(4)

$$\frac{4EI}{7} = 0.57$$

$$\frac{2EI}{6} = 0.33$$

$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{7} = 0.28$$

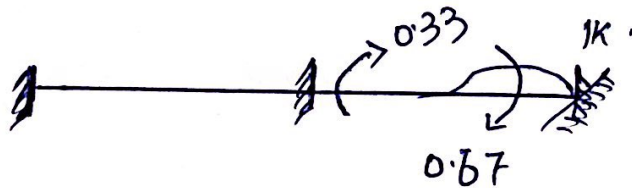
$$S_{11} = 0.57 + 0.67 \\ = 1.24 EA$$

$$S_{21} = 0.33 EA$$

b)

$$D_1 = 0$$

$$D_2 = 1k$$



$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$S_{12} = 0.33$$

$$S_{22} = 0.67$$

$$S = \begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$$

STEP V:-

(5)

Compute [D] matrix

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}^{-1} \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$\frac{1}{\begin{vmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{vmatrix}} \times \text{adj } A \times \begin{bmatrix} 0 \\ 4 \end{bmatrix} - \begin{bmatrix} 16.04 \\ 6 \end{bmatrix}$$

$$|S| = (1.24 \times 0.67) - (0.33 \times 0.33)$$

$$= 0.8308 - 0.1089$$

$$|S| = 0.7219$$

$$\text{Adj } A = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}$$

Now

$$\begin{bmatrix} AD_1 - ADL_1 \\ AD_2 - ADL_2 \end{bmatrix} = \begin{bmatrix} 0 - 16.04 \\ 4 - 6 \end{bmatrix} = \begin{bmatrix} 16.04 \\ -2 \end{bmatrix} \text{ @ } E$$

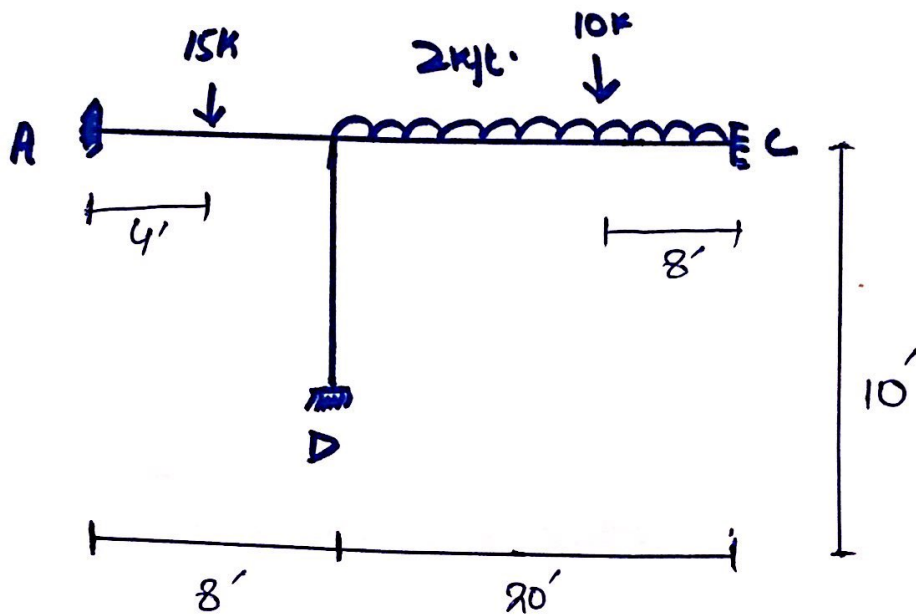
$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.915 \\ 3.894 \end{bmatrix}$$

Answer (1)

⑥

QUESTION - 2



SOLUTION:-

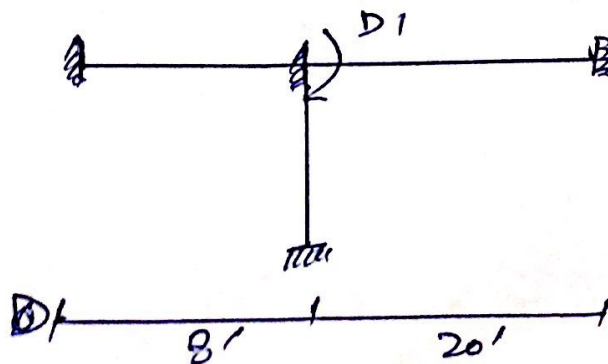
STEP 1:-

$$KI = ?$$

$$KI = 1^0$$

STEP 2:-

Determine unknown joint displacement.



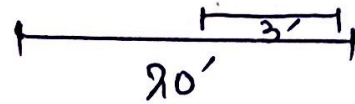
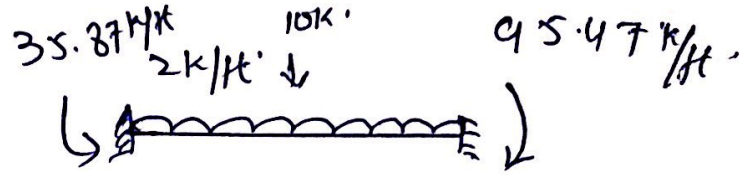
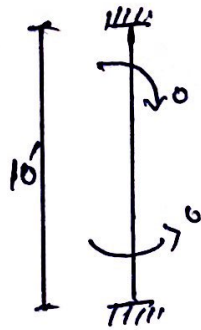
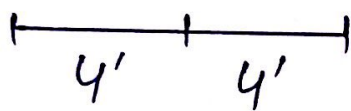
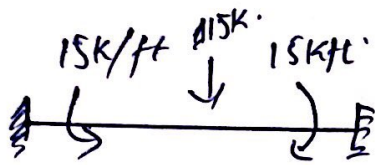
$$[D] = [?]$$

$$[AD] = [0]$$

STEP 3:-

(7)

Compute ADL matrix.



Point load at center

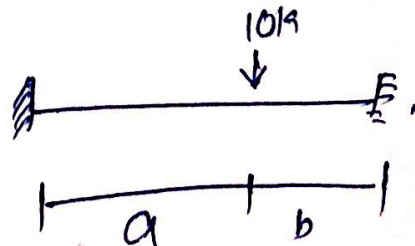
$$\frac{PL}{8} \Rightarrow \frac{(15)(8)}{8} = 15 \text{ k/ft.}$$

Uniformly distributed load

$$\frac{wL^2}{12} \Rightarrow \frac{2(20)^2}{12} \Rightarrow 66.67 \text{ k/ft.}$$

Point load (Not at mid)

Suppose.



⑧

For Left End

$$\frac{Pab^2}{L^2} = \frac{(10)(12)(8)^2}{(20)^2} = 19.2 \text{ k/ft.}$$

For Right End:

$$\frac{Pa^2b}{L^2} = \frac{(10)^2(12)(8)}{(20)^2} \Rightarrow 28.8 \text{ k/ft.}$$

total moment at Left End

$$19.2 + 66.67 = 85.87 \text{ k/ft.}$$

Similarly at Right End

$$28.8 + 66.67 = 95.47 \text{ k/ft.}$$

$$\sum_0 [M] = -85.87 - 15 = -70.87 \text{ k/ft.}$$

9

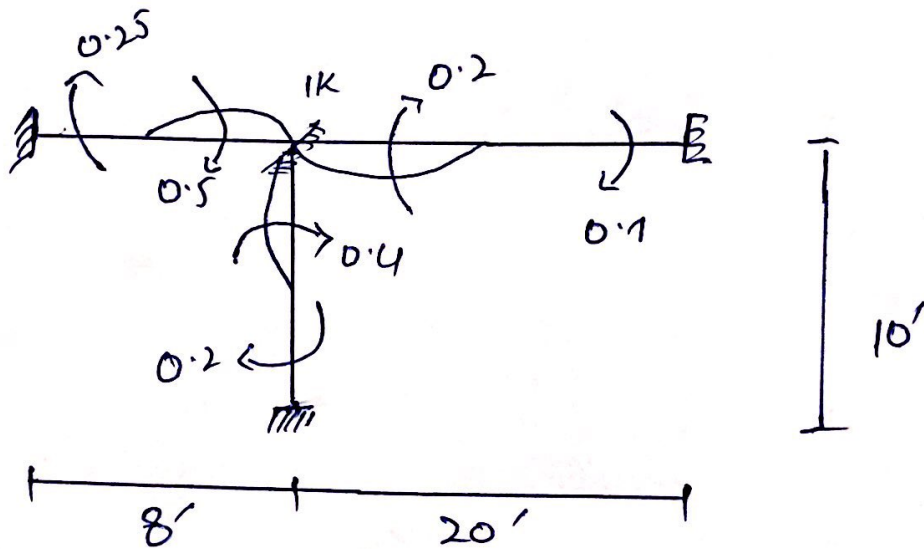
STEP 4:-

Determine $[S]$ matrix.

$$[S] = [S_{11}]$$

Now

$$D = 11k.$$



$$\frac{4EI}{8} = 0.5$$

$$\frac{2EI}{8} = 0.25$$

$$\frac{4EI}{20} = 0.2$$

$$\frac{2EI}{20} = 0.1$$

$$\frac{4EI}{10} = 0.4$$

$$\frac{2EI}{10} = 0.2$$

(10)

$$[S] = (0.5 + 0.4 + 0.2) EI.$$

$$= 1.1 EI$$

$$[S] = 1.1 EI.$$

Step 5:

Compute [D] matrix

$$[D] = [S]^{-1} \times [AD] - [ADU]$$

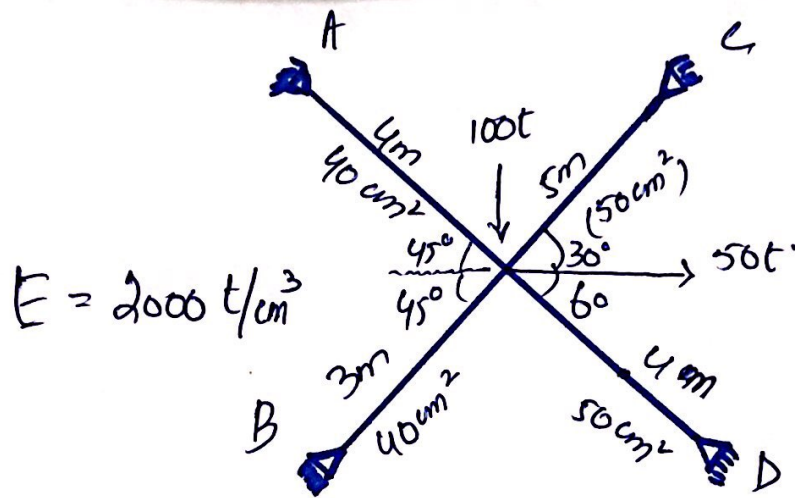
$$D = \frac{1}{1.1} \times [0] - [-70.87]$$

$$= \frac{70.87}{1.1}$$

$$D = [64.42] \text{ } \forall EI$$

QUESTION - 3

(11)



S
OLUTION:

FOR A:

$$\sin 45^\circ = \frac{P}{n} = \frac{P}{4}$$

$$P = 2.828 \text{ m}$$

$$\cos 45^\circ = \frac{b}{4}$$

$$b = 2.828 \text{ m}$$

FOR B:

$$\sin 45^\circ = P/3$$

$$\cos 45^\circ = b/n$$

$$b = 2.12 \text{ m}$$

(12)



For C:

$$\sin 30^\circ = \frac{P}{h=5}$$

$$\therefore D = 2.5 \text{ m}$$

$$\cos 30^\circ = b/5$$

$$= b = 4.33 \text{ m}$$

Now

$$EA(A) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(B) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(C) = 2000 \times 50 = 100,000 \text{ t}$$

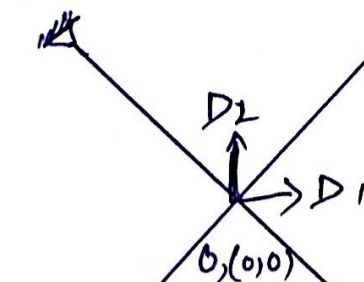
$$EA(D) = 2000 \times 50 = 100,000 \text{ t}$$

STEP 1:

Select Unknown Joint displacements.

$$A = (-2.82, +2.82)$$

$$C = (4.33, 2.5)$$



$$B = (-2.12, 2.12)$$

$$D = 2, -3.464$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

(13) (2)

STEP 3:

$$[AMD]_{4 \times 2} \quad \xi \quad [S]_{2 \times 2}$$

(i) $D_1 = 1, \quad D_2 = 0$

$$AMD_{11} = \frac{EA}{L^2} (2K - X_j)$$

$$AMD_{11} = \frac{80,000}{(400)^2} \times (0 + 2 \cdot 82) = 141$$

$$AMD_{21} = \frac{80,000}{300} \times (0 + 2 \cdot 12) = 138.44$$

$$AMD_{31} = \frac{100,000}{(500)^2} \times (0 - 433) = -173.2$$

$$AMD_{41} = \frac{100,000}{(400)^2} \times (0 - 200) = -125$$

Now

$$S_{11} = \sum_{j=1}^m \frac{EA}{L^2} (X_k - X_j)^2$$

(14) (8)

$$\frac{80,000}{(400)^3} \times (2.82)^2 + \frac{80,000 \times 212}{(300)^3}$$

$$+ \frac{100,000}{(500)^3} \times (-433) + \frac{100,000}{(400)^3} \times (-200)^2$$

$$S_{11} = 99.405 + 1.33 \cdot 107 + 149.991 + 62.5$$

$$\Rightarrow 445.063$$

$$S_{12} = S_{21} = \sum_{i,j} \frac{EA}{L^3} \times (x_k - x_j) (y_k - y_j)$$

$$= \frac{80,000}{(400)^3} \times (282) - 282 + \frac{80,000 \times 212 \times (212)}{(300)^3}$$

$$+ \frac{100,000}{(500)^3} \times (433) (0 - 200) + \frac{100,000}{(400)^3} \times (-200) (0 + 346)$$

$$S_{12} = S_{21} = 17.237$$

(ii)

$$D_1 = 0, \quad D_1 = 1k \cdot'$$

$$AMD = \frac{EA}{L^2} (y_k - y_j)$$

$$AMD_{12} = \frac{80,000}{(300)^2} (-282) = -141$$

(15)

$$AMD_{22} = \frac{80,000}{(300)^2} (212) = 188.44$$

$$AMD_{32} = \frac{100,000}{(500)^2} (-250) = -100$$

$$AMD_{42} = \frac{100,000}{(400)^2} (346) = 216.25$$

$$\text{Now } S_{22} = \sum_{j=1}^m \frac{EA}{L^3} (Y_k - Y_j)^2$$

$$\frac{80,000}{(400)^3} (282)^2 + \frac{80,000}{300^2} (212)^2$$

$$+ \frac{100,000}{(500)^3} (-250)^2 + \frac{100,000}{(400)^3} (346)^2$$

$$S_{22} = 469.628$$

STEP 4:

$$[D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.003 \\ 12.237 \end{bmatrix}$$

$$\begin{bmatrix} 12.237 \\ 469.628 \end{bmatrix}^{-1} \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

Step 5:-

[AM]

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.4 & 188.44 \\ -173.2 & -100 \\ -125 & 216.25 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + 188.44 \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ -125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 16.68 + 30.46 \\ 22.89 - 40.70 \\ -20.49 + 21.6 \\ -14.79 - 46.71 \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 47.136t \\ -18.413t \\ 1.11t \\ -61.498t \end{bmatrix}$$

