

Name = M. IKRAM

ID = 7874

Sec = B

Sub = Hydraulic

Six = Fawad

✓

$$Q = 1''$$

①

Ans:

Sol:-

$$b = 8 \text{ m}$$

$$Q = 7874 \text{ m}^3/\text{sec} = 7.874 \text{ m}^3/\text{sec}$$

$$V = R - 2000 = 7874 - 2000 = 5874 \text{ m}^3/\text{sec}$$
$$= 2339.6 \text{ m}^3/\text{sec}$$

As we know that

$$Q = Av$$

$$v = \frac{Q}{b} = \frac{7.874}{8} = 0.984 \text{ m}^3/\text{sec}$$

$$y_c = \left( \frac{v^2}{g} \right)^{1/3} \Rightarrow \left( \frac{0.984^2}{9.81} \right)^{1/3} = 0.462 \text{ m}$$

$$y_c = 0.462 \text{ m}$$

As this is rectangular section

$$Q = vb \quad \text{--- (1)}$$

$$Q = Av \quad \text{--- (2)}$$

$$vb = Av$$

$$vb = Av$$

$$Q = ybV$$

$$Q = yv$$

(2)

$$V_c = \frac{Q}{y_c} = \frac{0.9843}{0.42} = 2.344 \text{ m/s}$$

$\therefore V > V_c$  (Supercritical flow)

Height of hydraulic jump on upstream side

As  $Q = AV$ ,  $Q = byv$

$$y_1 = \frac{Q}{bV_1} = \frac{7.874}{8 \times 2339.6} = 0.0004 \text{ m}$$

$$y_2 = -\frac{y_1}{2} + \sqrt{\frac{y_1^2}{4} + \frac{2y_1V_1}{g}}$$

$$= -\frac{0.0004}{2} + \sqrt{\frac{(0.0004)^2}{4} + \frac{2(0.0004)(2339.6)}{9.81}}$$

$$y_2 = 1.3698 \text{ m}$$

$$\Delta y = y_2 - y_1 = 1.3698 - 0.0004 = 1.3694$$

$$\therefore \Delta E = E_1 - E_2$$

As we know that

$$Q_1 = Q_2$$

$$A_1 V_1 = A_2 V_2 = \gamma y_1 V_1 = \gamma y_2 V_2$$

(3)

$$V_2 = \frac{y_1 V_1}{y_2} = \frac{(0.0004)(2339.6)}{1.3698} = 0.683 \frac{m}{s}$$

$$\Delta E = E_1 - E_2 = \left( y_1 + \frac{V_1^2}{2g} \right) - \left( y_2 + \frac{V_2^2}{2g} \right)$$

$$= \left( 0.0004 + \frac{(2339.6)^2}{2(9.81)} \right) - \left( 1.369 + \frac{(0.683)^2}{2(9.81)} \right)$$

$$= 278987.2 - 1.393 \Rightarrow 278985.81 \text{ m}$$

→ Power absorbed:

$$\Delta P = \rho g Q (E_1 - E_2)$$

$$= 1000 \times 9.81 \times 7.874 \times (278985.81)$$

$$\left[ \Delta P = 2.15 \times 10^{10} \text{ W} \right]$$

$$\Delta P = 2.15 \times 10^7 \text{ kW}$$

Q: 1"

(B)

(4)

(B)

Sol:-

$$b = 4 \text{ m}$$

$$Q = 7874 \frac{\text{ft}^3}{\text{sec}} = \frac{7874}{(3.28)^3}$$
$$= 223.816 \frac{\text{m}^3}{\text{sec}}$$

$$y_1 = 2.9 \text{ m}, \quad y_2 = 1.1 \text{ m}$$

Specific energy at upstream } down  
- stream side.

$$E_1 = E_2$$

$$y_1 + \frac{V_1^2}{2g} = y_2 + \frac{V_2^2}{2g} \quad \text{--- (1)}$$

We know that

$$Q = A_1 V_1 = A_2 V_2$$

$$b y_1 V_1 = b y_2 V_2 \quad \therefore b_2 = b_1 = b$$

$$V_2 = \frac{y_1 V_1}{y_2} = \frac{2.9}{1.1} V_1$$

$$V_2 = 2.634 V_1 \quad \text{--- (2)}$$

Put Value of  $v_2$  in (1)

(5)

$$2.9 + \frac{v_1^2}{2 \times 9.81} = 1.1 + \frac{(2.63v_1)^2}{2 \times 9.81}$$

$$2.9 - 1.1 = \frac{6.938}{19.62} - \frac{v_1^2}{19.62}$$

$$1.8 = \frac{6.938v_1^2}{19.62} - \frac{v_1^2}{19.62}$$

$$\sqrt{v_1^2} = \sqrt{\frac{1.8 \times 19.62}{5.938}}$$

$$v_1 = 2.44 \text{ m/sec}$$

Put Value of  $v_1$  in eq (1)

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$2.9 + \frac{(2.44)^2}{2g} = 1.1 + \frac{v_2^2}{2g}$$

$$\cancel{2.9 + \frac{(2.44)^2}{2g}}$$

6

~~2.9~~

$$2.9 - 1.1 = \frac{V_2^2}{2g} - \frac{5.95}{2g}$$

$$1.8 \times 2 \times 9.81 = V_2^2 - 5.95$$

$$\sqrt{V_2^2} = \sqrt{41.266}$$

$$V_2 = 6.42 \text{ m/sec}$$

Now to determine type of flow using Froude no.

### UPSTREAM SIDE:

$$F_{r1} = \frac{V_1}{\sqrt{g y_1}} = \frac{2.44}{\sqrt{9.81 \times 2.9}} = 0.457 < 1$$

Sub Critical flow

### DOWSTREAM SIDE:

$$F_{r2} = \frac{V_2}{\sqrt{g y_2}} = 1.95 > 1$$

Super Critical flow

Q: 2 (a)

(7)

$$y_1 = 1.8 \text{ m} \quad , \quad b = 66' = \frac{66}{3.28} = 20.12 \text{ m}$$

$$Q = \frac{7874}{(3.28)^3} = 223.186 \text{ m}^3/\text{sec}$$

Minimum height (P) of weir

$$Q = AV \Rightarrow V = \frac{Q}{A} = \frac{Q}{by}$$

$$V_1 = \frac{223.186}{(20.12)(1.8)} \Rightarrow 6.163 \text{ m/sec}$$

As we know that

$$y_c = \left( \frac{Q^2}{g} \right)^{1/3} = \left( \frac{11.091}{9.81} \right)^{1/3}$$

$$\therefore \begin{aligned} v &= Q/b \\ v &= 11.09 \end{aligned}$$

$$y_c = 2.323 \text{ m}$$



Also  $V = \sqrt{gy} \Rightarrow V_c = \sqrt{gy_c}$

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$$V_c = \sqrt{9.81 \times 2.32} = 4.75 \text{ m/sec}$$

Now according to specific energy  $\epsilon_1 = \epsilon_2$

$$y_1 + \frac{V_1^2}{2g} = \frac{V_c^2}{2g} + y_c + P$$

$$1.8 + \frac{(6.663)^2}{2 \times 9.81} = \frac{4.75^2}{2(9.81)} + 2.323 + P$$

$$P = 3.7 - 2.323 - 0.24$$

$P = 1.137 \text{ m}$

Q: 2" (9)

(9)

(B)

Ans:

$$b = 2.8 \text{ m}; \quad d = 1.5 \text{ m}$$

$$H_1 = 5 \text{ m}; \quad H_2 = 5 + 1.5 = 6.5 \text{ m}$$

$$H = 5 + 0.6 = 5.6 \text{ m}$$

$$C_d = 0.7874$$

$$Q = ?$$

Discharge through submerged portion

$$Q_1 = C_d \times b \times (H_2 - H_1) \times \sqrt{2gh}$$

$$= 0.7874 \times 2.8 \times (6.5 - 5.6) \times \sqrt{2(9.81)(5.6)}$$

$$Q = 20.794 \text{ m}^3/\text{Sec}$$

⇒ Discharge of free portion

$$Q_2 = \frac{2}{3} \times C_d \times b \times \sqrt{2g} [H_2^{3/2} - H_1^{3/2}]$$

$$= \frac{2}{3} \times 0.7874 \times 2.8 \times \sqrt{2 \times 9.81} [5.6^{\frac{3}{2}} - 5^{\frac{3}{2}}]$$

$$Q_2 = 13.48 \text{ m}^3/\text{sec}$$

Total discharge

$$Q = Q_1 + Q_2 = 20.794 + 13.48$$

$$Q = 34.27 \text{ m}^3/\text{sec}$$

Q: 3" (a)

(11)

(A)

$$P_1 = R + 800 = 7874 + 800$$

$$P_1 = 8674 \text{ N/m}^2$$

$$d_1 = R - 200 = 7874 - 200 \\ = 7674 \text{ mm}$$

$$A_1 = \frac{\pi}{4} d_1^2 = \frac{\pi}{4} (7674)^2 \\ = 46.23 \text{ m}^2 \Rightarrow V_1 = 0.02 \text{ m/s}$$

$$d_2 = R + 300 = 7874 + 300 \\ = 10874 \text{ mm}$$

~~$d_2 = R + 300$~~   $d_2 = 10.874 \text{ m}$

$$A_2 = \frac{\pi}{4} (10.874)^2 = 92.82 \text{ m}^2$$

(12)

$$V_2 = \frac{Q}{A} = \frac{0.95}{92.82} = 0.01 \text{ m/sec}$$

(1) Head loss due to Sudden enlargement

$$h_e = \left(1 - \frac{A_1}{A_2}\right)^2 \left(\frac{V_1 - V_2}{2g}\right)^2$$

$$h_e = \left(\frac{1 - 46.23}{92.75}\right)^2 \left(\frac{0.02 - 0.01}{2 \times 9.81}\right)^2$$

$$h_e = 6.5 \times 10^{-7} \text{ m}$$

(2) power lost due to sudden enlargement

$$P = \rho g Q h_e = 1000 \times 9.81 \times 0.95 \times 6.5 \times 10^{-7}$$

$$P = 0.006052 \text{ W}$$

(13)

③ pressure in the smallest pipe  
apply Bernoulli's equation

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + h$$

$$\frac{8674}{1000 \times 9.81} + \frac{(0.02)^2}{2 \times 9.81} = \frac{P_2}{1000 \times 9.81} + \frac{(0.01)^2}{2 \times 9.81} + 6$$

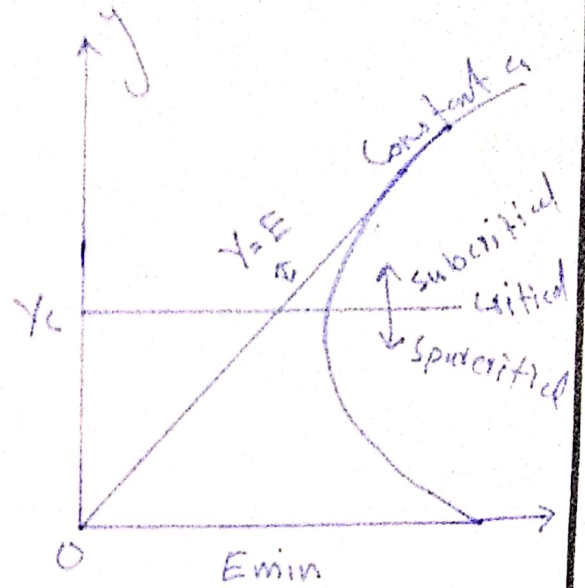
$$P_2 = 8673.995 \text{ N/m}^2$$

Q3: (b)

(14)

(3)

Ans:



The above graph is plot between depth flow ( $y$ ) and Specific Energy ( $E$ ) it is made from three degree polynomial equation which shows us the different specific energy for the depth flow which may be either

- ① sub critical
- ② critical
- ③ supercritical

Specific energy is used to clarify the meaning of the above terms in an open channel.

How is this achieved:

Total energy = potential energy + kinetic energy

$$TE = mgh + \frac{1}{2}mv^2$$

$$= Wh + \frac{1}{2} \frac{W}{g} v^2$$

$$\therefore w = mg$$
  
$$m = w/g$$

ignoring "W" weight of water

$$T.E = h + \frac{v^2}{2g}$$

$$\boxed{T.E = y + \frac{v^2}{2g}} \Rightarrow \textcircled{1}$$

As we know that

$$Q = VA, \quad v = Q/A \quad \text{Squaring b.s}$$

$$v^2 = \frac{Q^2}{A^2} \quad \text{put } v^2 \text{ in eq } \textcircled{1}$$

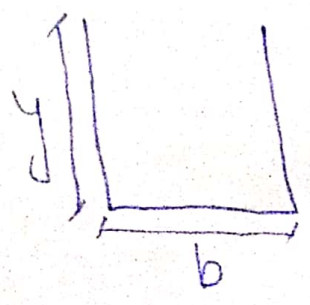
Suppose Channel is rectangular

$$A = y \times b \quad \text{--- } \textcircled{2}$$

$$Q = v \times b \quad \text{--- } \textcircled{3}$$

Putting values of  $\textcircled{2}$  &  $\textcircled{3}$  in  $\textcircled{1}$

$$E = y + \frac{Q^2}{y^3 b^3 2g} \quad \text{(putting } \textcircled{2} \text{)}$$





$$E = y + \frac{v^2}{2g} \Rightarrow \text{Putting } (y)$$

(10)

$$E - y = \frac{v^2}{2g} \Rightarrow y^2 (E - y) = \frac{v^2}{2g}$$

$$(E - y) y^2 = \text{Constant}$$

As 'v' and 'g' are constant

\* Critical depth is the flow depth corresponding to minimum specific energy

$y > y_c \Rightarrow$  Subcritical flow

$y = y_c \Rightarrow$  Critical flow

$y < y_c \Rightarrow$  Supercritical flow