

ID

7655

Name

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Subject

Structure advance

Submitted
to

Engr Adeed

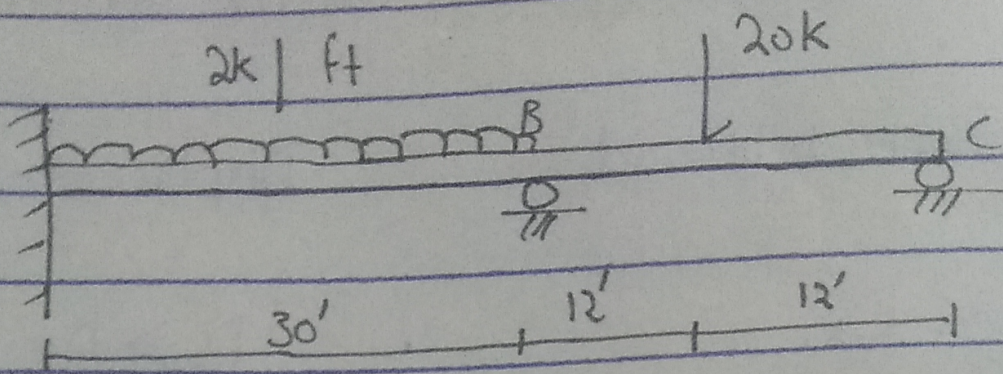
Date

21/8/20

Semester

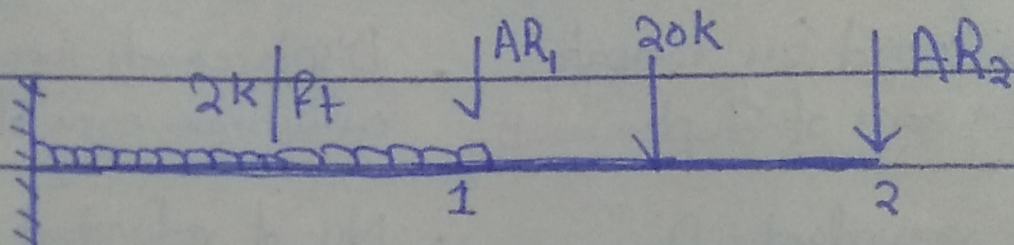
12th (Summer)

Q1



Sol Structural Indeterminacy = 2°

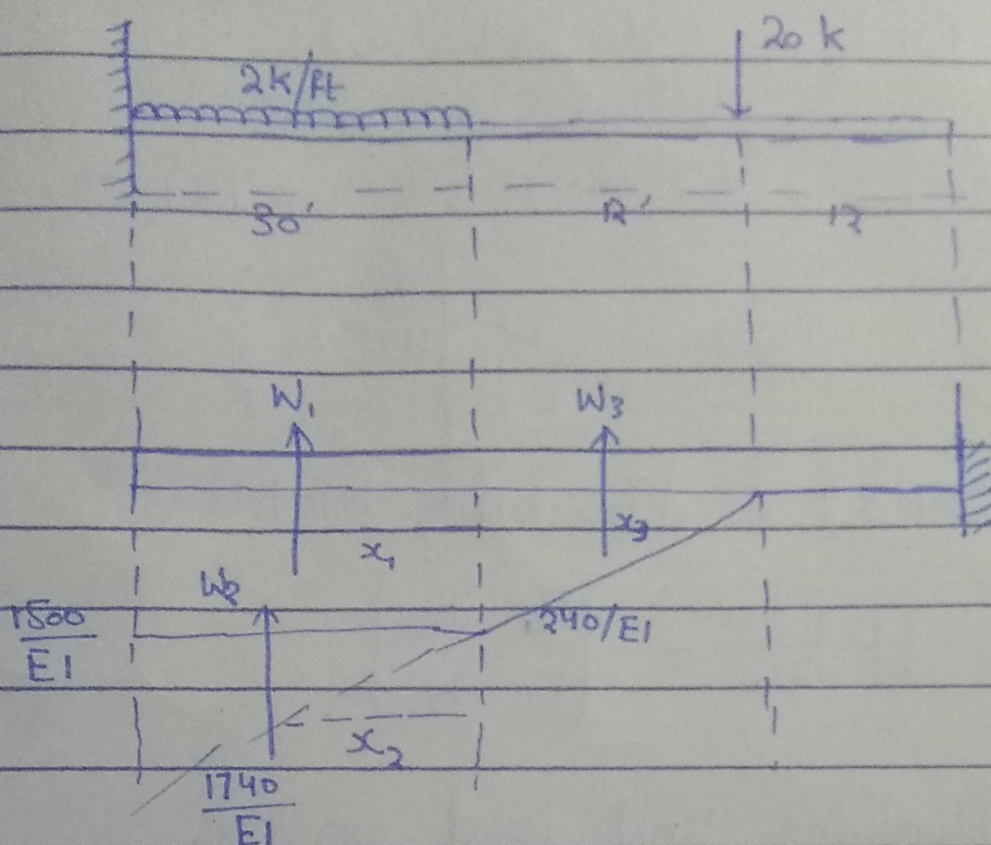
Step 1 # Select Redundant Actions



$$\begin{bmatrix} DR_{s_1} \\ DR_{s_2} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \quad \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$[DR_s] = [DRL] + [F] \times [AR]$$

Step #2 Compute the value of [DRL]



$$W_1 = 1500 \times 30 = 45000$$

$$20 \times 12 = 240$$

$$W_2 = \frac{1}{3} \times 30 \times 240 = 2400$$

$$20 \times (2 \times 30) + (2 \times 30) \times 15 = 1740$$

$$W_3 = \frac{1}{2} \times 12 \times 240 = 1440$$

$$x_1 = \frac{l}{2} = \frac{30}{2} = 15'$$

$$x_2 = \frac{3 \times l}{n+2} = \frac{3 \times 30}{2+2} = 22.5', \quad x_3 = \frac{2}{3} \times l = 8'$$

Now finding DRL :-

$$\begin{aligned} DRL_2 &= W_1 \times (x_1 + 24) + W_2 \times (x_2 + 24) + \\ & \quad W_3 \times (x_3 + 12) \\ &= 45000(15 + 24) + 2400(22.5 + 24.5) + \\ & \quad + 1440(8 + 12) \end{aligned}$$

$$DRL_2 = 175000 + 111600 + 28800 = 1895400/EI$$

$$\begin{aligned}
 DRL_1 &= W_1(x_1) + W_2(x_2) \\
 &= 45000(15) + 24000(22.5) \\
 &= 675000 + 540000 = 1215000
 \end{aligned}$$

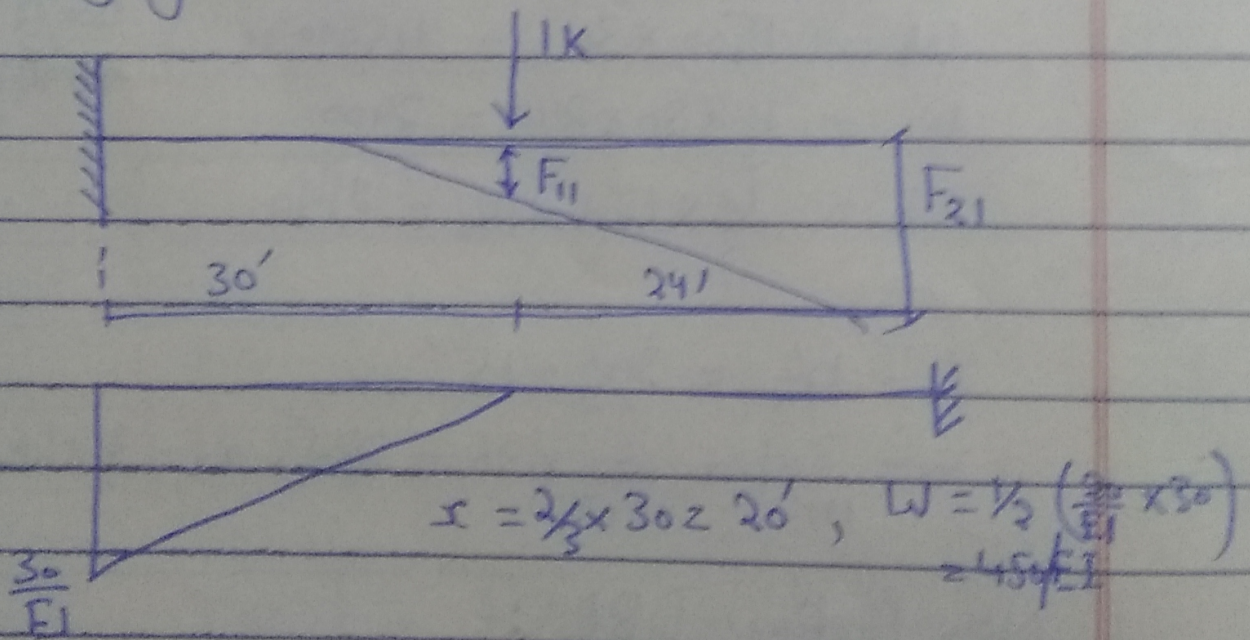
So,

$$DRL = \frac{1}{EI} \begin{bmatrix} 729000 \\ 1875400 \end{bmatrix}$$

Step 3; Flexibility Matrix

$$[F]_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

Applying unit load on AR,

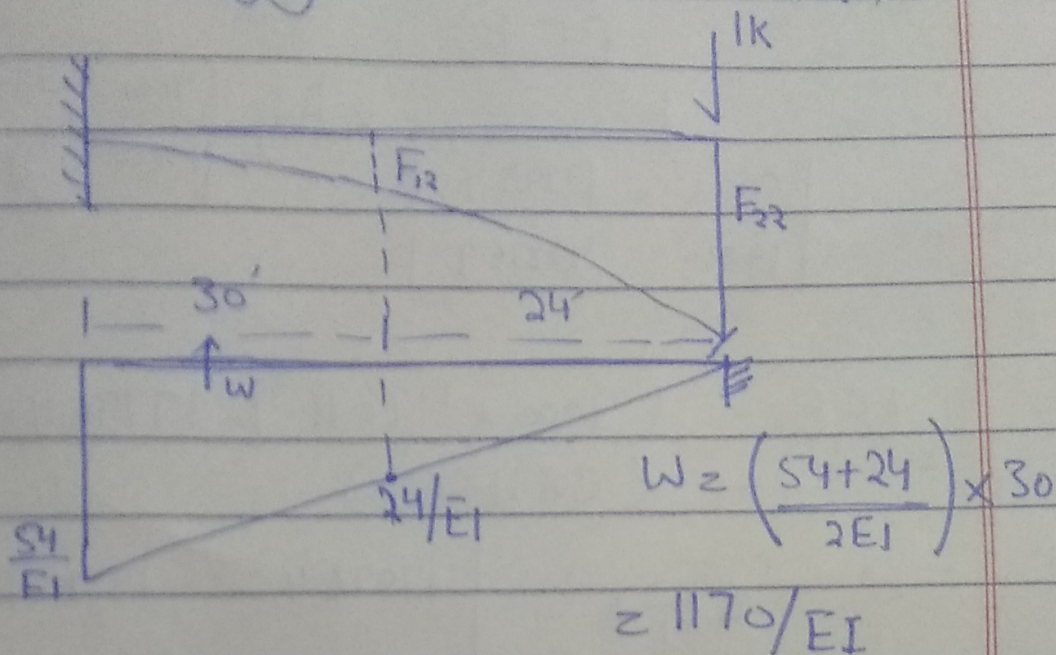


So,

$$F_{11} = \frac{450}{EI} (20) = \frac{9000}{EI}$$

$$F_{21} = \frac{450}{EI} (20 + 24) = \frac{19800}{EI}$$

Now Applying unit load on AR₂;



Now

$$x = \frac{L}{3} \left[\frac{b + 2a}{a + b} \right]$$

$$= \frac{30}{3} \left[\frac{24 + 2(54)}{54 + 24} \right] = 16.92$$

$$F_{12} = \frac{1170}{EI} \times 16.92 = \frac{19796.4}{EI}$$

Hence

$$F_{2 \times 2} = \begin{vmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{vmatrix} \frac{1}{EI}$$

Step # 4; Compute the values AR

$$[DR_s] = [DRL] + [F] \times [AR]$$

$$[AR] = [DR_s - DRL] \times [F]^{-1}$$

$$[F]^{-1} = \frac{1}{[F]} \times \text{Adj } F$$

$$Z = \begin{vmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{vmatrix} \times \text{Adj} \begin{pmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{pmatrix}$$

$$|F| = (9000 \times 47876.4 - 19796.4 \times 19800)$$

$$= (38918880)$$

$$\Rightarrow \text{Adj } A = \begin{pmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{pmatrix}$$

$$\begin{pmatrix} AR_1 \\ AR_2 \end{pmatrix} = \begin{pmatrix} 0 & -729000 \\ 0 & -1895400 \end{pmatrix} \times \frac{1}{EI} \times \frac{1}{38918880}$$

$$= \begin{pmatrix} -729000 \\ -1895400 \end{pmatrix} \times \frac{1}{EI} \times \begin{pmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{pmatrix}$$

$$\begin{pmatrix} AR_1 \\ AR_2 \end{pmatrix} = \begin{pmatrix} 66.193 \\ 67.505 \end{pmatrix}$$

Q2

D/f b/w force method and displacement method and suggest which method is more suitable for structure analysis in matrix approach?

Ans)

→

Force Method

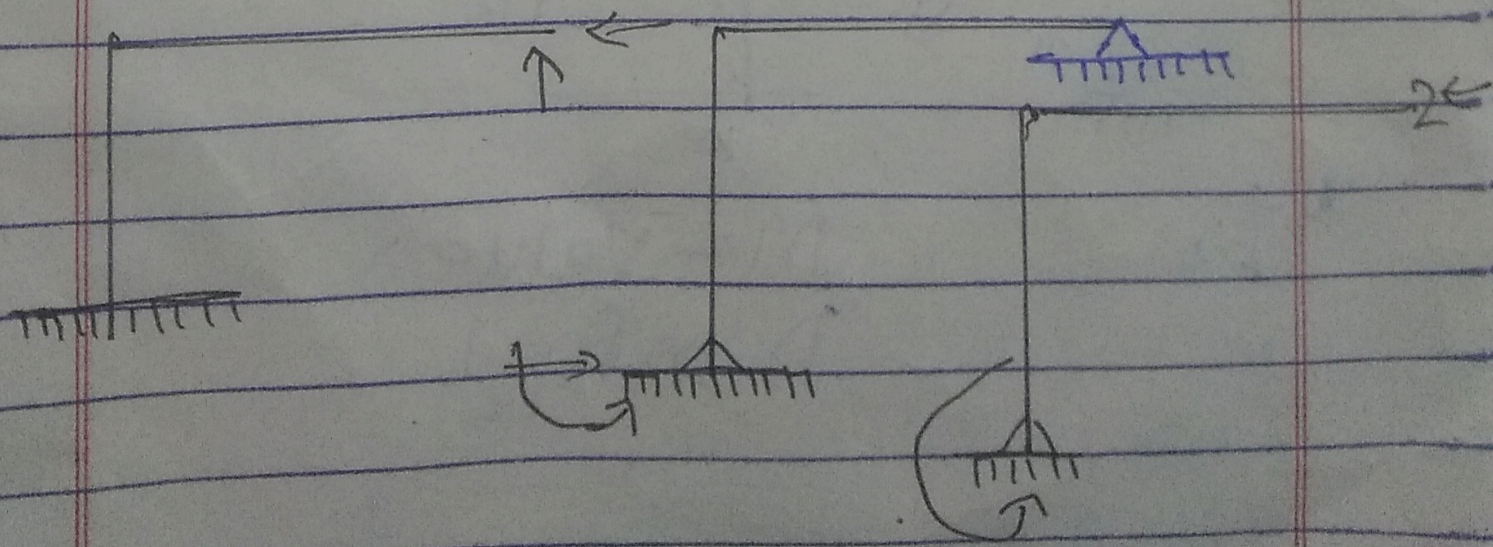
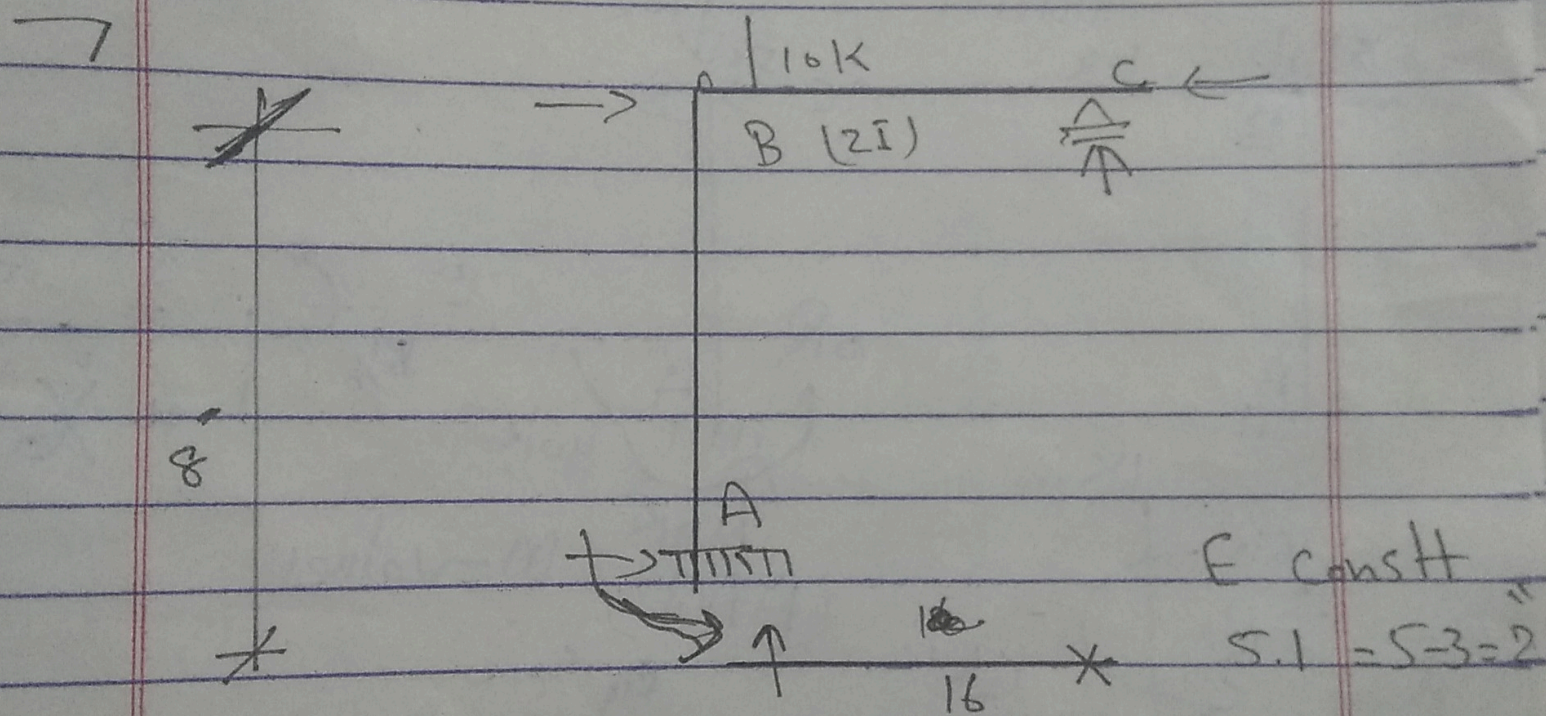
Displacement Method

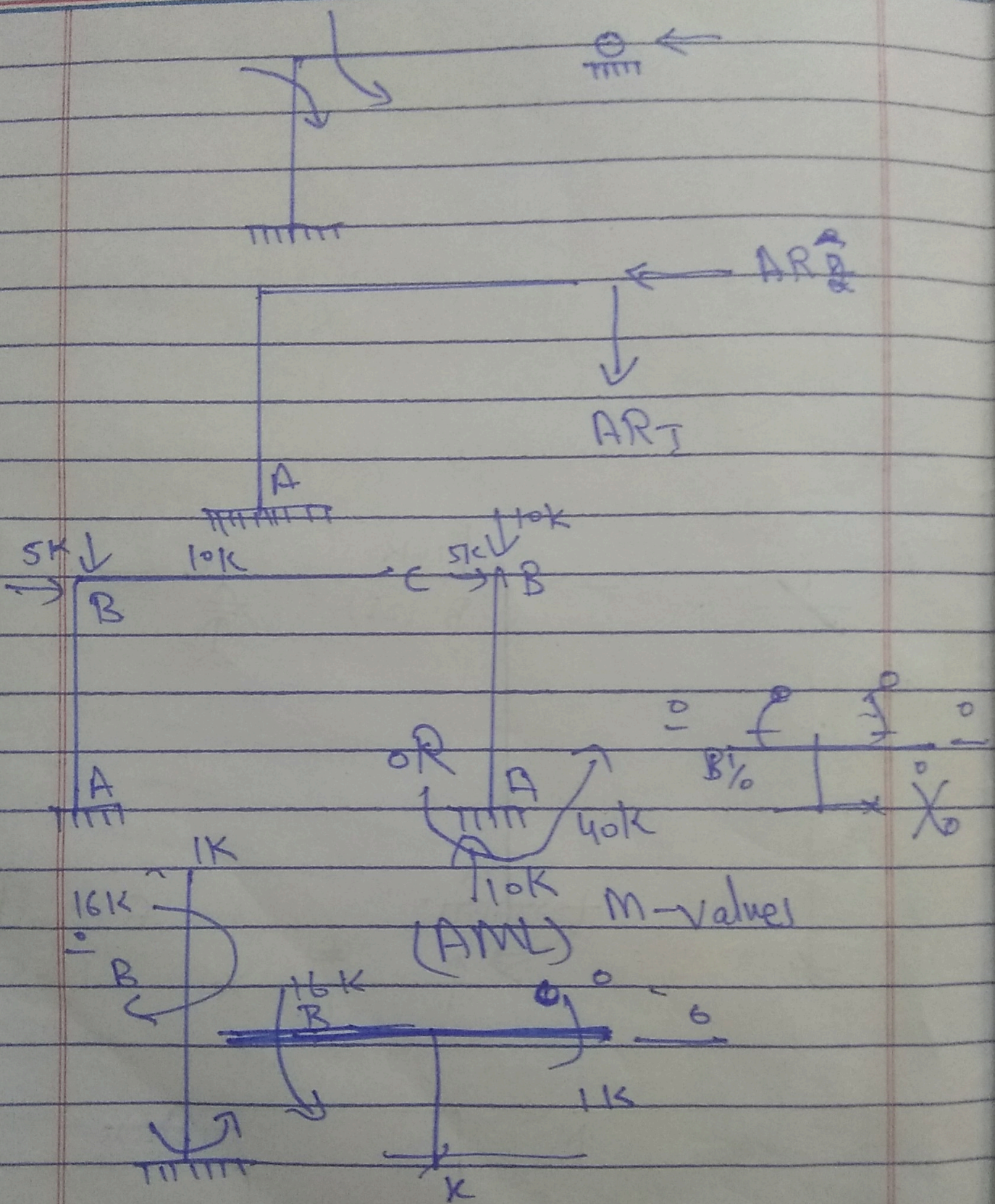
- | | |
|--|--|
| • $D_s < D_k$ | • $D_s > D_k$ |
| • Forces are redundant or unknowns. | • Displacements are unknown. |
| • Starts with equilibrium of forces. | • Starts with compatible deformation. |
| • Forces found by compatibility eqns of displacements. | • Displacements found by equilibrium eqns of forces. |
| • No of redundant = D_c | • No of redundant = D_k |
| • not suitable for computer. | • not suitable for trusses. |

→ Stiffness method also called displacement method is more suitable for structure analysis matrix approach, as it is a primary method used in matrix analysis. The main advantage of this method over flexibility method is that is conducive to computer programming. Once the analytical model of the structure has been

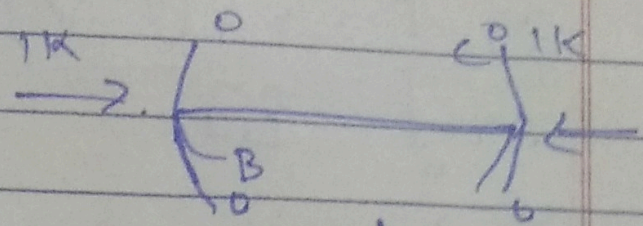
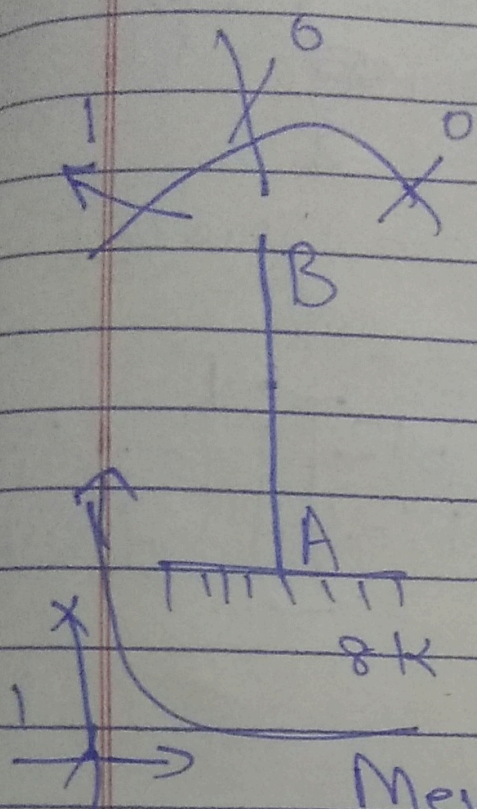
Q3)

Solve the following Problem through flexibility method;





M-values
 A MR-1



M_2 - values
AMR₂

$$\begin{aligned} & \int_0^8 \frac{1}{EI} (-5x + 10) (-16) dx + \int_0^6 \frac{1}{2EI} (-x)(-x) dx \\ & \int_0^8 \frac{1}{EI} (-80x + 160) dx + \int_0^6 \frac{1}{2EI} (-x)(-x) dx \end{aligned}$$

Member	AB	BC
origin	A	C
limits	0 → 8	0 → 6
I	I	2I
mm	-16	-x
mmI	8-x	0

$$DR_4 = \int_0^8 \frac{(5x - 10)(-16)}{EI} dx + \int_0^6 \frac{(0)(-x)}{2EI} dx$$

$$= 2560 EI$$

$$DAI \int_B^A \frac{(5x - 10)(8 - x)}{EI} dx = -853.33 / EI$$

$$F_{11} \int_0^8 \frac{(-16)(8 - x)}{EI} dx + \int_0^6 \frac{(-x)(-x)}{2EI} dx$$

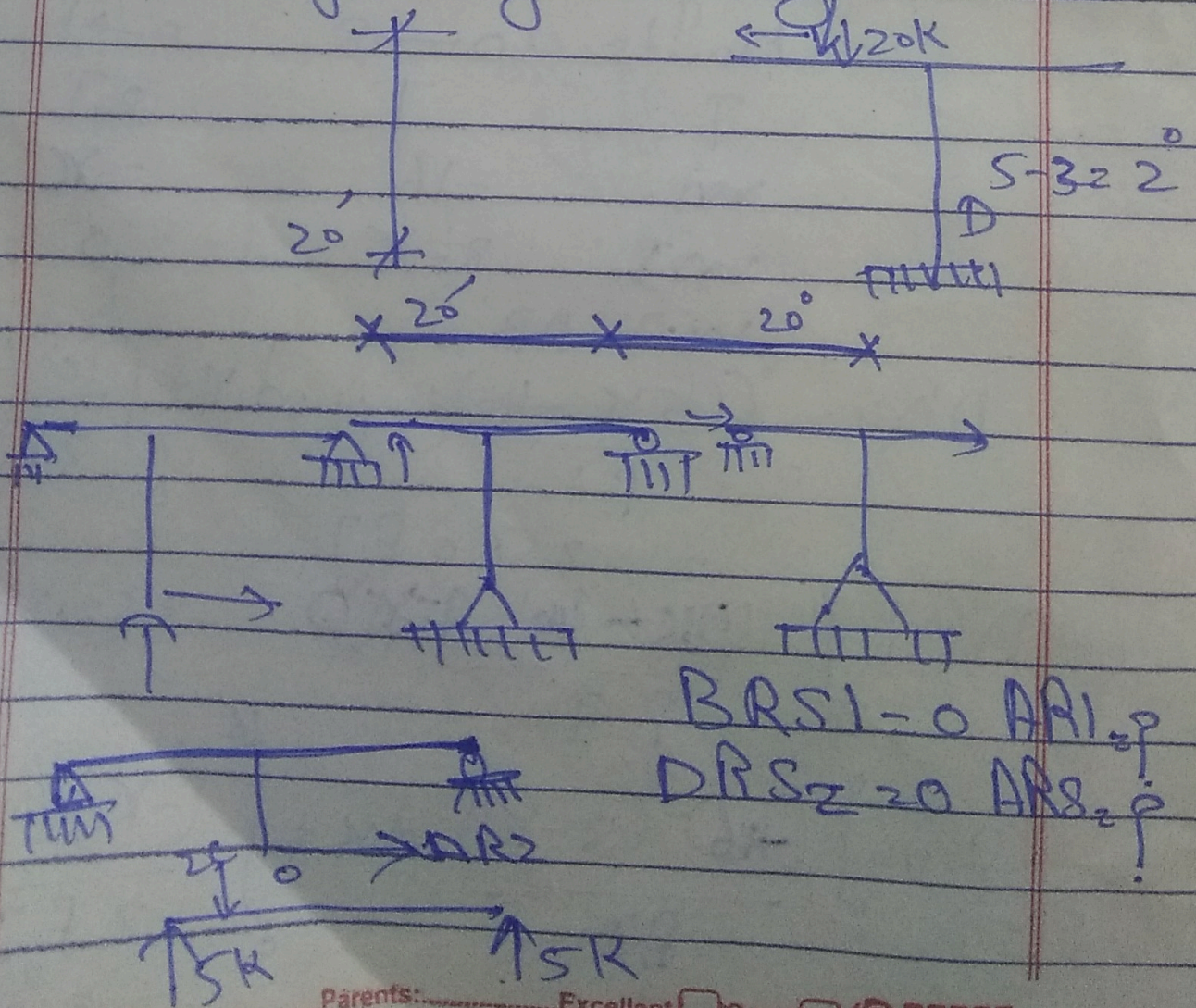
$$f_{21} \int_0^8 \frac{(8-x)(8-x)}{EI} dx + 0 = -512/EI$$

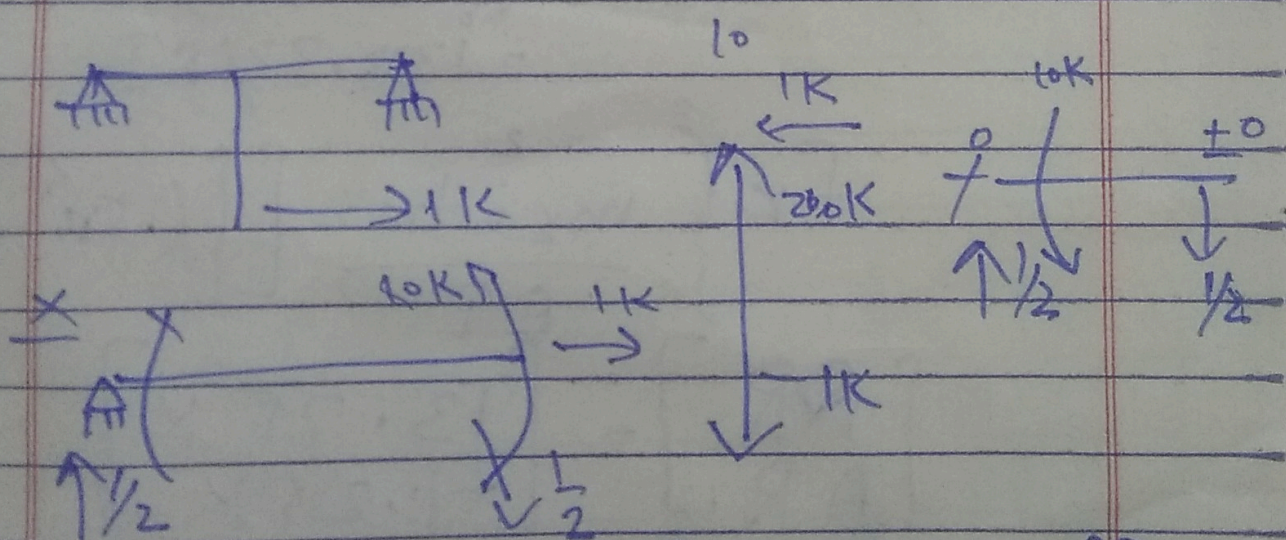
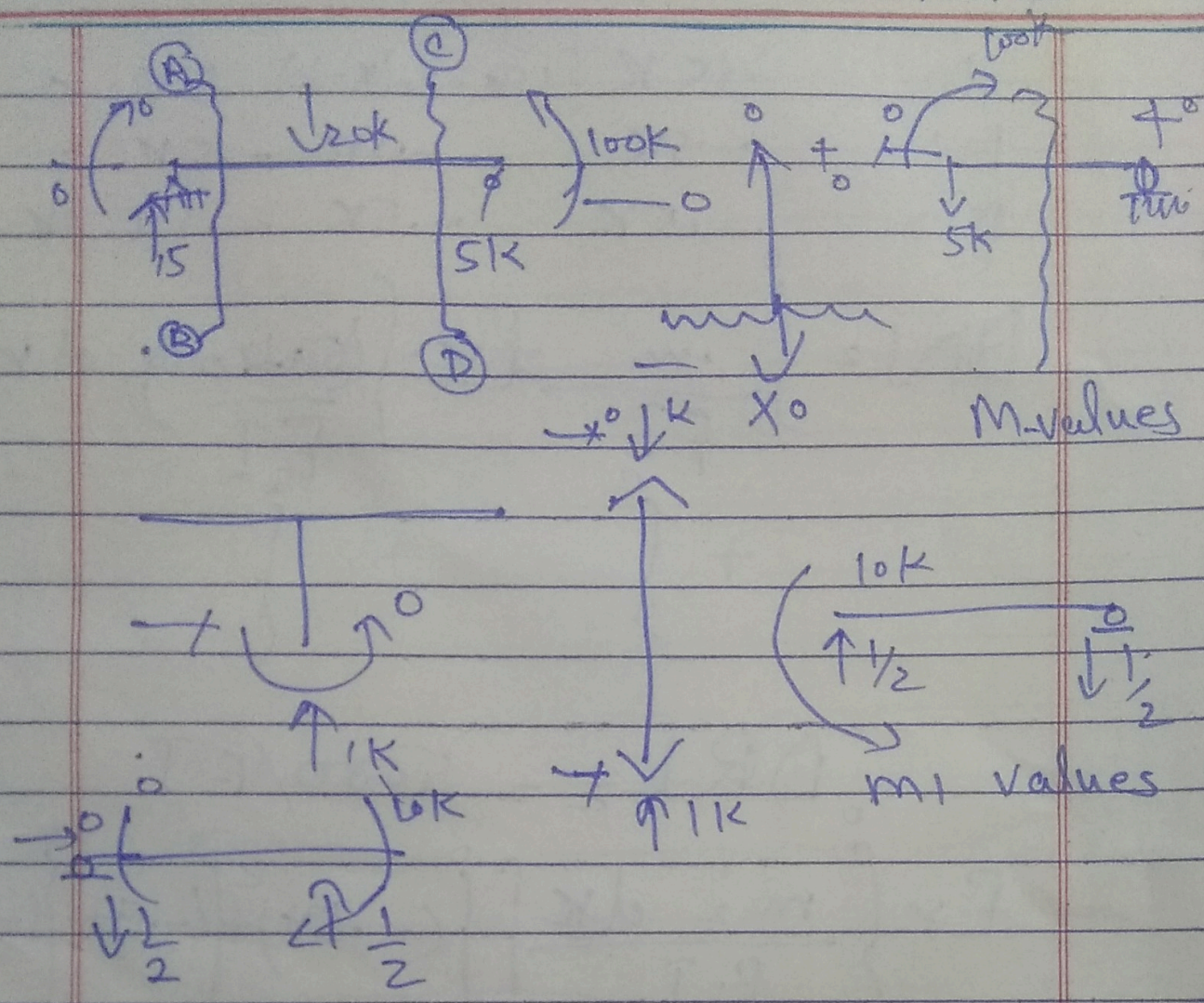
$$f_{22} \int_0^8 \frac{(8-x)(8-x)}{EI} dx + 0 = 170.67/EI$$

$$\begin{bmatrix} ARL \\ ARL \end{bmatrix} = \begin{bmatrix} 2730.67 & -512 \\ -512 & 170.67 \end{bmatrix} \begin{bmatrix} 0.2860 \\ 0.1853 \end{bmatrix} \times \frac{1}{EI}$$

$$= \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$

Analyse by flexibility Methods





members	AB	BC	CD
origin	A	A	C
Limit	→ 10	10 → 20	0 → 20
T	I	I	I

M	15K	15K - 20(K-10)	5K	0
M1	-0.5K	-0.5K	-0.5K	0
M2	-0.5K	-0.5K	-0.5K	1K

$$[DR] = \int_0^L \frac{m}{EI} dx + \int_0^L \frac{(5x + 2000)}{EI} dx$$

$$+ \int_0^L \dots + \int_0^L \dots$$

$$DRL_2 = 5000/EI$$

$$F_x \int_0^L \frac{m_2}{EI} dx = \int_0^L (-0.5x) + \int_0^L (-0.5) + \int_0^L (-0.5x)$$

$$= 1333.33/EI$$

$$F_x \int_0^L \frac{m_2}{EI} dx = \left[(-0.5x)^2 + \dots \right]$$

$$\begin{bmatrix} RR \\ AR \end{bmatrix} = \begin{bmatrix} 13.75 K \\ -1.25 K \end{bmatrix}$$