

ASSIGNMENT :- 03

CONJUGATE BEAMS

NO :- 7965

SECTION :- "B"

SUBJECT :- STRUCTURAL ANALYSIS

SUBMITTED TO :- SIR AMTJAD ISLAM

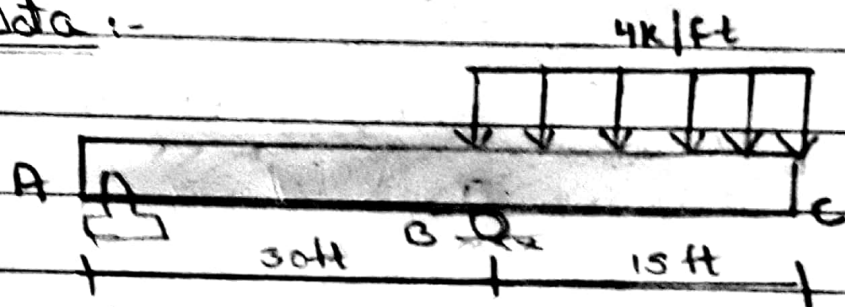
DEPARTMENT :- BE (CIVIL)

DATE :- 13 - JULY 2020

## QUESTION NO. 1

Determine the slope at point C --- use the moment Area theorem.

Given Data :-



Required Data :-

We have to find the slope

Solution :-

As we know that

$$\sum M_A = 0 \rightarrow$$

$$(F_B \times 30) - (4 \times 37.5) = 0$$

$$F_B = 75k$$

$$\text{Now } \sum F_y = 0 \uparrow$$

$$F_A + 75k - 60k = 0$$

$$F_A = -15k$$

$$\text{Now } \theta_{C/A} = \frac{1}{2} \left( \frac{-750k \cdot ft}{EI} \right) (45 ft)$$

$$= \frac{33750 k \cdot ft^2}{2 EI}$$

$$= \frac{16875}{EI} \text{ k}\cdot\text{ft}^2$$

$$(t_{B/A}) = \left[ \frac{1}{2} \left( \frac{750 \text{ k}\cdot\text{ft}}{EI} \right) (30 \text{ ft}) \right] \left[ \frac{1}{3} (30 \text{ ft}) \right]$$

$$= \frac{112500}{EI} \text{ k}\cdot\text{ft}^3$$

$$(t_{C/A}) = \left[ \frac{1}{2} \left( \frac{750 \text{ k}\cdot\text{ft}}{EI} \right) (30 \text{ ft}) \right] \left[ 15 \text{ ft} + \frac{1}{3} (30 \text{ ft}) \right]$$

$$+ \left[ \frac{1}{2} \left( \frac{750 \text{ k}\cdot\text{ft}}{EI} \right) (15 \text{ ft}) \right] \left[ \frac{2}{3} (15 \text{ ft}) \right]$$

$$= \frac{281250}{EI} \text{ k}\cdot\text{ft}^3 + \frac{56250}{EI} \text{ k}\cdot\text{ft}^3$$

$$= \frac{337500}{EI} \text{ k}\cdot\text{ft}^3$$

$$\text{Then, } \Delta' = \frac{45}{30} (t_{B/A})$$

$$= \frac{45}{30} \left( \frac{112500 \text{ k}\cdot\text{ft}^3}{EI} \right)$$

$$= \frac{168750}{EI} \text{ k}\cdot\text{ft}^3$$



$$Q_A = \frac{(H \tan B/A)}{t_{AB}} = \frac{112500}{30ft} EI$$

$$= \frac{3750 \text{ k}\cdot\text{ft}^3}{EI}$$

$$+ \downarrow Q_c = Q_A + Q_{c/A}$$

$$Q_c = \frac{-3750 \text{ k}\cdot\text{ft}^2}{EI} + \frac{16875 \text{ k}\cdot\text{ft}^2}{EI}$$

$$Q_c = \frac{13125 \text{ k}\cdot\text{ft}^2}{EI}$$

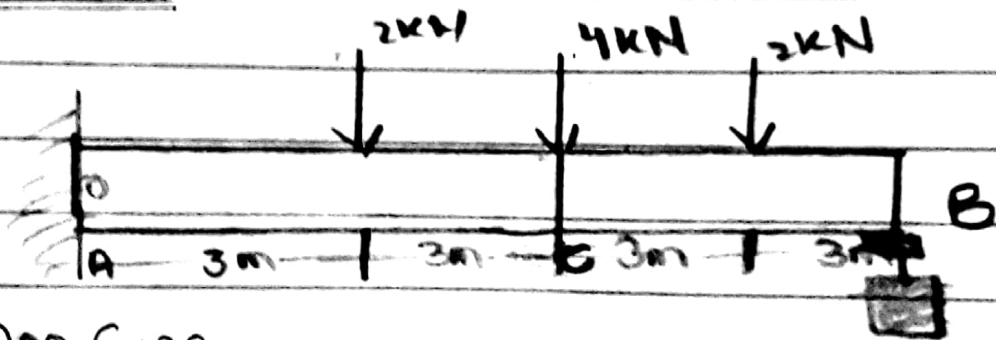
$$\Delta_c = H'_{c/A} - \Delta' = \frac{337500 \text{ k}\cdot\text{ft}^3}{EI} - \frac{168750 \text{ k}\cdot\text{ft}^3}{EI}$$

$$\Delta_c = \frac{168750 \text{ k}\cdot\text{ft}^3}{EI}$$

Question No :- 02

Determine the slope at point  $C$   
Taking  $E = 200 \text{ GPa}$ ,  $I = 6 \times 10^6 \text{ mm}^4$ .

Given Data :-



$$E = 200 \text{ GPa}$$
$$I = 6 \times 10^6 \text{ mm}^4$$

Solution :-

$$\theta_{A/C} = \frac{1}{2} \left( \frac{12}{EI} \times 3 \right) + \left( \frac{12}{EI} \times 3 \right) + \frac{1}{2} \left( \frac{6}{EI} \times 3 \right)$$

$$\theta_{A/C} = \frac{63}{EI}$$

$$\theta_{A/C} = \frac{63}{(200 \times 10^9)(6 \times 10^6)(1/1000)^4}$$

$$\theta_{A/C} = 0.0525 \text{ radian}$$

$$\tan A/c = \frac{1}{2} \left( \frac{12}{EI} \times 3 \right) \left( \frac{2 \times 3}{3} \right) + \left( \frac{12}{EI} \times 3 \right) \left( 3 + \frac{1}{2} \times 3 \right) \\ + \frac{1}{2} \left( \frac{6}{EI} \times 3 \right) \left( 3 + \frac{2}{3} \times 3 \right)$$

$$\tan A/c = 0.202 \text{ m}$$

$$\Delta_c = \tan A/c = 0.202 \text{ m}$$

$$\Delta_c = 202 \text{ mm}$$

Result :-

$$\Delta_c = 202 \text{ mm}$$