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NAME

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AD NO

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Dep

B.S. (DT)

Bio Statistic

①

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Q No 1

(A)

~~$x \quad y \quad x^2 \quad y^2$~~

$x$	$y$	$x^2$	$y^2$	$xy$
3	25	9	625	75
4	24	16	576	96
5	20	25	400	100
6	20	36	400	120
7	19	49	361	133
8	17	64	289	136
9	16	81	256	144
10	13	100	169	130
11	10	121	100	110
<u>12</u>	<u>8</u>	<u>144</u>	<u>64</u>	<u>96</u>
75	172	645	3246	1140

$n = 10, \quad \sum x = 75, \quad \sum y = 172, \quad \sum x^2 = 645$

$\sum y^2 = 3246, \quad \sum xy = 1140$

Substituting in to the computing formulae for  $r$  gives

$$r = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{\sqrt{\left[ \sum x^2 - \frac{(\sum x)^2}{n} \right] \left[ \sum y^2 - \frac{(\sum y)^2}{n} \right]}}$$



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$$x = 1140 \left[ \frac{(75)(172)}{10} \right]$$

$$\sqrt{645 - (75)^2 / 10} \cdot \sqrt{3246 - (172)^2 / 10}$$

$$x = 1140 - 1290$$

$$\left[ \frac{645 - 5625}{10} \right] \left[ \frac{3246 - 2958.4}{10} \right]$$

$$= \frac{150}{(22.5)(2876)}$$

$$= \frac{150}{23727}$$

$$= -0.01$$

ANS.

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Q No 1 (B)

Determine the equation of the least square regression line of  $y$  on  $x$  and  $x$  on  $y$ .

$x$	$y$	$x^2$	$y^2$	$xy$
20	5	400	25	100
11	15	121	225	165
15	14	225	196	210
10	17	100	289	170
17	8	289	64	136
18	9	324	81	162
21	12	441	144	252
25	16	625	256	400
28	18	784	324	504
total	165	3309	1604	2099

Regression line  $y$  on  $x$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$n \sum x^2 - (\sum x)^2$$

$$b = \frac{9(2099) - (165)(124)}{9(3309) - (165)^2}$$



(4)

$$b = \frac{18891 - 20460}{29781 - 27225}$$

$$b = \frac{-1569}{2556}$$

$$b = -0.6$$

$$a = \frac{\sum y - b \sum x}{n}$$

$$a = \frac{124 - (-0.6)(165)}{9}$$

$$= \frac{124 - (-99)}{9}$$

$$a = 24.7$$

Regression line  $x$  on  $y$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum y^2 - (\sum y)^2}$$

$$b = \frac{9(2099) - (165)(124)}{9(1604) - (124)^2}$$

$$= \frac{18891 - 20460}{14436 - 15376}$$

$$b = \frac{-1569}{-940}$$

$$b = \frac{1569}{940}$$

$$b = 1.7$$

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$$a = \frac{\sum x - b \sum y}{n} = \frac{165 - (1.7)(194)}{9}$$

$$a = \frac{165 - 310.8}{9}$$

$$a = \frac{-45.8}{9}$$

$$a = -5.1$$

Hence the required regression line is give by

$$\hat{x} = a + by$$

~~$$\hat{x} = -5.1$$~~

$$\hat{x} = -5.1 + 1.7y$$



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~~Part~~

Q No 1 part B

Find the predicted value  
of  $y$  for  $x = 20, 11, 15, 25, 28,$   
and  $x$  for  $y = 5, 15, 9, 12,$   
 $16, 18.$

$$\hat{y} = 24.7 - 0.6x$$

$$\hat{x} = 5.1 + 1.7y$$

$$x \quad y \quad \hat{y} = 24.7 - 0.6x \quad \hat{x} = 5.1 + 1.7y$$

$$20 \quad 5 \quad 12.7 \quad 3.4$$

$$11 \quad 15 \quad 18.1 \quad 20.4$$

$$25 \quad 12 \quad 9.7 \quad 15.3$$

$$28 \quad 16 \quad 7.9 \quad 22.1$$

$$18 \quad 25.5$$

This is the required  
predicted value.



Q No 2

(A) find the following  
A fair coin is  
tossed 5 times.

find the probabilities  
of obtaining various number  
of heads.

⇒ Let us regard the tossing  
of a coin as experiment.  
then we observe that

(i) each toss of a coin  
(i.e. each trial) has two  
possible outcomes, head  
(success) and tails (failure).

(ii) The probability of a  
head (success) is  $p = \frac{1}{2}$   
and remains the same for  
for

Successive tosses:

(iii) The successive tosses of  
the coin are independent;  
and

(iv) The coin is tossed 5 times.



Therefore the r.v.  $X$  which denotes the number of head (success) has a binomial probability distribution with  $p = 1/2$  and  $n = 5$ . The possible value of  $X$  are 0, 1, 2, 3, 4 and 5, Hence

$$P(\text{no head}) = P(X=0) = \binom{5}{0}$$

$$\left(\frac{1}{2}\right)^0 \left(\frac{1}{2}\right)^5$$

$$= 1 \times \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$

$$P(1 \text{ heads}) = P(X=1) = \binom{5}{1} \left(\frac{1}{2}\right)^1 \left(\frac{1}{2}\right)^{5-1}$$

$$= 5 \times \left(\frac{1}{2}\right)^5 = \frac{5}{32}$$

$$P(2 \text{ heads}) = P(X=2) = \binom{5}{2} \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^{5-2}$$

$$P(3 \text{ heads}) = P(X=3) = \binom{5}{3} \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^{5-3}$$



$$= 10 \times \left(\frac{1}{2}\right)^5 = \frac{10}{32}$$

$$P(4 \text{ heads}) = P(X=4) = \binom{5}{4} \left(\frac{1}{2}\right)^4 \left(\frac{1}{2}\right)^{5-4}$$

$$= 5 \times \left(\frac{1}{2}\right)^5 = \frac{5}{32}, \text{ and}$$

$$P(5 \text{ heads}) = P(X=5) = \binom{5}{5} \left(\frac{1}{2}\right)^5 \left(\frac{1}{2}\right)^{5-5}$$

$$= 5 \times \left(\frac{1}{2}\right)^5 = \frac{5}{32}, \text{ and}$$

$$P(5 \text{ heads}) = P(X=5) = \binom{5}{5} \left(\frac{1}{2}\right)^5 \left(\frac{1}{2}\right)^0$$

These probabilities can also be obtained by expanding the binomial  $\left(\frac{1}{2} + \frac{1}{2}\right)^5$ . The binomial

probability distribution for the number of heads obtained in 5 tosses of a coin is a ~~poisson~~ ~~coin~~ is.



$x$	0	1	2	3	4	5
$f(x)$	$\frac{1}{32}$	$\frac{5}{32}$	$\frac{10}{32}$	$\frac{10}{32}$	$\frac{5}{32}$	$\frac{1}{32}$

(B)

A and B play a game in which A's probability of winning is  $\frac{2}{3}$  in a series of 10 games. What is the probability that A will win (i) at least 4 games.

(ii) Exactly equal to 4/10 games

(iii) Exactly equals to 10 games

(iv) 6 or more games.



Q No 2 part (B)

$$① P(X=4) =$$

$$= 1 - P(X=0)$$

$$= 1 - \sum_{x=0}^4 \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$\left[ \binom{10}{0} \left(\frac{2}{3}\right)^0 \left(\frac{1}{3}\right)^{10-0} + \binom{10}{1} \left(\frac{2}{3}\right)^1 \left(\frac{1}{3}\right)^{10-1} +$$

$$\binom{10}{2} \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^{10-2}$$

$$+ \binom{10}{3} \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^{10-3} \Big]$$

$$= 1 - \left[ 10 \left(\frac{1}{3}\right)^{10} + 10 \left(\frac{2}{3}\right) \left(\frac{1}{3}\right)^9 + 45 \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^8 \right.$$

$$\left. + 120 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^7 \right]$$

$$= 1 - \left[ 0.0009 + 0.0003 + 45(0.44)(0.0009) \right.$$

$$\left. + 120 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^7 \right]$$

$$= 1 - \left[ 0.0009 + 0.0003 + 45(0.44)(0.0009) \right.$$

$$\left. + 120(0.296)(0.0005) \right]$$



$$= 1 - [0.0002 + 0.0003 + 0.0004 + 0.017]$$

$$= 1 - [0.0215]$$

$$P(X \geq 4) = 0.978$$

$$(ii) P(X = 4/10) = ?$$

$$P(X = 4/10) = f(4/10) = 0 \text{ because a}$$

$X = n$ .  $X$  with a binomial distribution takes only one of the values  $0, 1, 2, \dots, n$ .

Value  $0, 1, 2, \dots, n$ .

$$(iii) P(X = 11) = ?$$

$$P(X = 11) = f(6) = 0 \text{ because } X \text{ can take only value } 0, 1, 2, \dots, 10$$

$$(iv) P(X \geq 6) = ?$$

$$= \sum_{x=6}^{10} \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= \binom{10}{6} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^{10-6} + \binom{10}{7} \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^{10-7}$$



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$$\left( \frac{10}{8} \right) \left( \frac{2}{3} \right) \left( \frac{1}{3} \right)^{10} \cdot 2$$

$$\left[ 910 (0.007) (0.017) + 80 (0.008) (0.017) \right. \\ \left. + 45 (0.039) (0.11) + 10 (0.026) (0.31) \right. \\ \left. + 1 (0.017) \right]$$

$$\left[ 0.91994 + 0.17168 + 0.195 + 0.08658 \right. \\ \left. + 0.017 \right]$$

$$P(x \leq 716) = 0.6725$$

This is the reversed solution of the probability.



Q No 3 (a)

Construct the ungrouped frequency distribution of these data.

Number	Frequency	Tally
0	1	
1	4	
2	8	
3	11	
4	8	
5	5	
6	4	
7	3	
8	2	
9	1	
10	3	



(3)

Construct the grouped frequency distribution of these data.

Number of groups	Frequency
0 - 2	13
3 - 5	24
6 - 8	9
9 - 11	4

