

**Department of Electrical Engineering
Assignment**

**Date:
13/04/2020**

Course Details

Course Title: Linear Circuit Analysis
Instructor: Dr. Sohailmaran

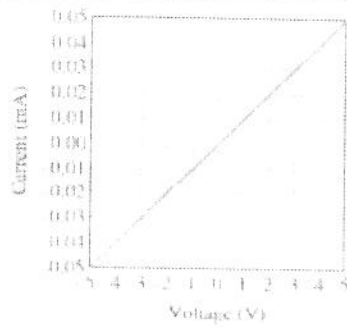
Module: 2
Total Marks: 30

**Student
Details**

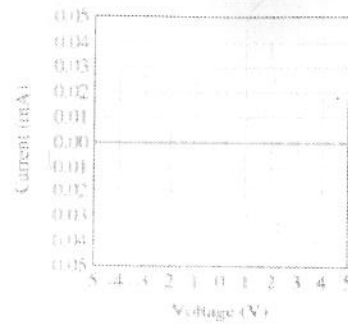
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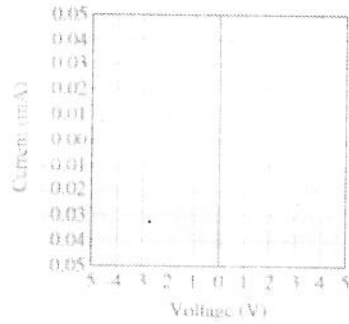
Q1	(a)	<p>For each of the circuits in figure, find the current I and compute the power absorbed by the resistor</p> <div style="text-align: center;"> </div>	<p>Marks 3</p>
			<p>PLO1</p>
	(b)	<p>Determine the power supplied by the leftmost element in the circuit of following figure</p> <div style="text-align: center;"> </div>	<p>Marks 4</p>
		<p>PLO1</p>	
	(c)	<p>Following figure depicts the current-voltage characteristic of three different resistive elements. Determine the resistance of each, assuming the voltage and current are defined in accordance with the passive sign convention.</p>	<p>Marks 3</p>
			<p>PLO1</p>



(a)

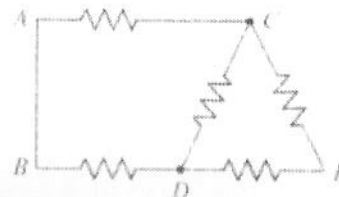
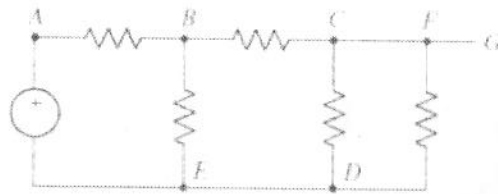


(b)



(c)

- Q2 (a) Refer to the circuits of following figures, and answer the following:
1. How many distinct nodes are contained in the circuit?
 2. How many elements are contained in the circuit?
 3. How many branches does the circuit have?
 4. Determine if each of the following represents a path, a loop, both, or neither:
 - i. A to B
 - ii. B to D to C to E
 - iii. C to E to D to B to A to C
 - iv. C to D to B to A to C to E



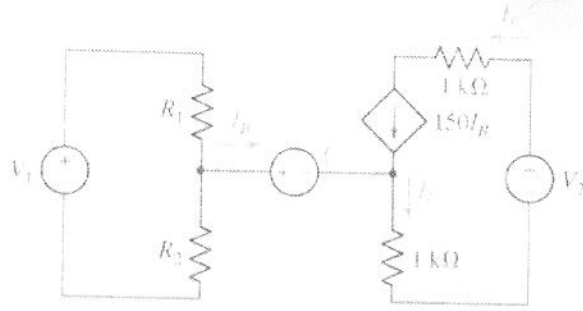
- (b) For the circuit of following figure (which is a model for the dc operation of a bipolar junction transistor biased in forward active region), I_B is measured to be $100 \mu\text{A}$. Determine I_C and I_E .

Marks
4

PLO2

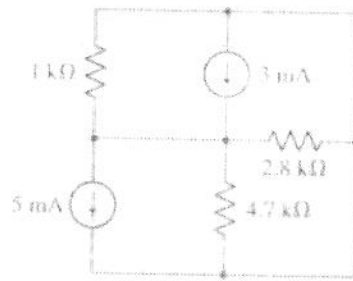
Marks
6

PLO2

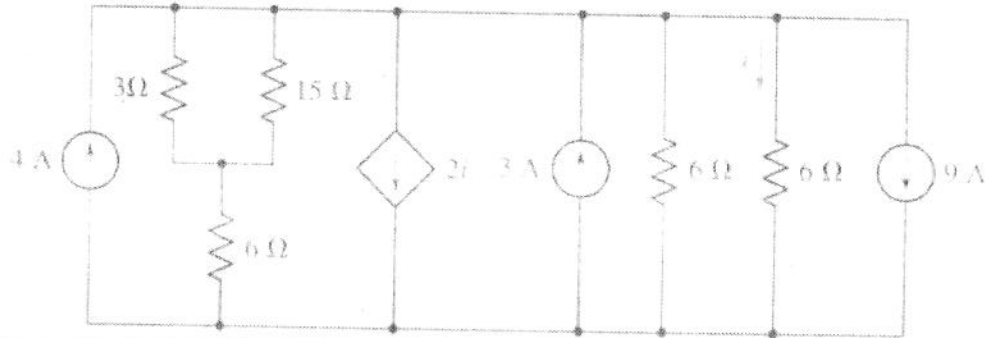


Q3 (a) Although drawn so that it may not appear obvious at first glance, the circuit of following figure is in fact a single-node-pair circuit.

- Determine the power absorbed by each resistor.
- Determine the power supplied by each current source.
- Show that the sum of the absorbed power calculated in (a) is equal to the sum of the supplied power calculated in (b).



(b) Determine the power absorbed by the 15Ω resistor in the circuit of following figure



Marks
5

PLO1

Marks
5

PLO1

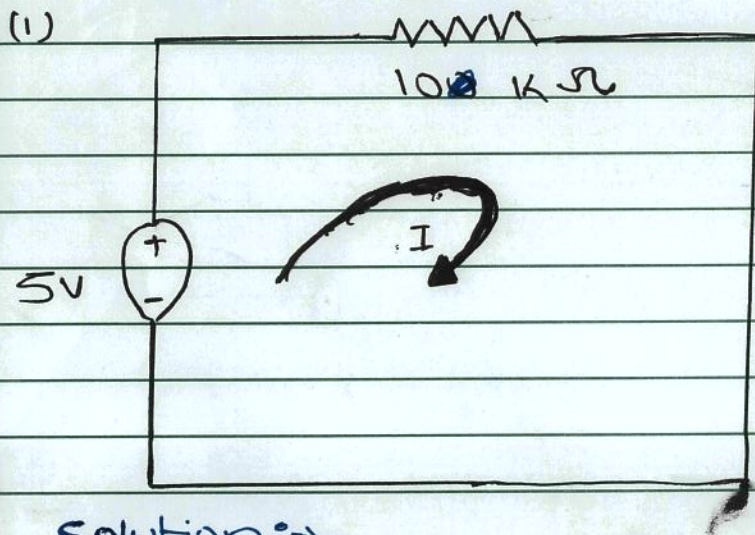
Date: _____

(1)

Question no 1:-

Part (a)

FOR each of the circuit
Following circuit.
Find current (I)
and Power (P) absorbed
by the resistor (R).



Solution:->

In order to find Power
we ~~have~~ need voltage and
current.

$$P = I \cdot V \rightarrow (1)$$

In Given Fig:-
voltage $V = 5V$

but current is not given.

So first we have to calculate
current (I) through circuit.

Date: _____

(2)

From Ohm Law:-

$$V = IR$$

$$\Rightarrow I = V/R \quad \text{--- (ii)}$$

WE HAVE

$$V = 5 \text{ volt}$$

$$R = 100 \text{ k}\Omega$$

$$R = 100 \times 10^3 \text{ Ohm}$$

$$I = 5 / 100 \times 10^3$$

$$I = 0.0005 \text{ A}$$

OR

$$I = 0.5 \text{ mA}$$

Put value of (i) I & v in (i)

$$(i) \Rightarrow P = I \cdot V$$

$$P = 0.0005 \text{ A} \times 5 \text{ volt}$$

$$P = 0.0025 \text{ watt}$$

~~OR~~

$$P = 0.0025 \text{ watt} \rightarrow \text{ANS}$$

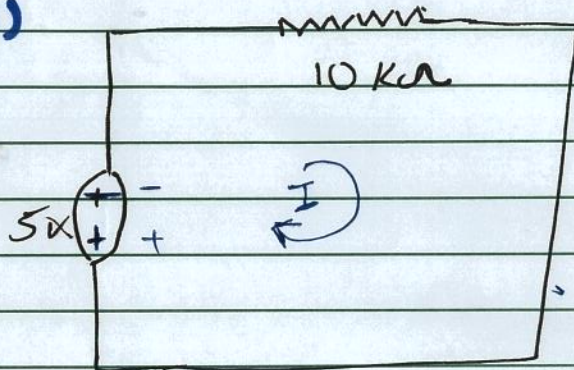
OR

$$P = 2.5 \text{ mwatt}$$

Date: _____

(3)

(iii)



Solution:

In this circuit the ~~polarity~~ polarity of voltage source is changed hence we take V as $(-V)$
 $\Rightarrow V = 5 \text{ volt} \Rightarrow -5 \text{ volt.}$

From Ohm law

$$V = IR$$

$$I = V/R$$

$$= -5/10 \times 10^3$$

$$I = -0.0005 \text{ A}$$

OR

$$I = -0.5 \text{ mA}$$

Hence power consumed by resistor

$$P = I \cdot V \Rightarrow -0.0005 \times -5$$

$$P = 0.0025 \text{ W}$$

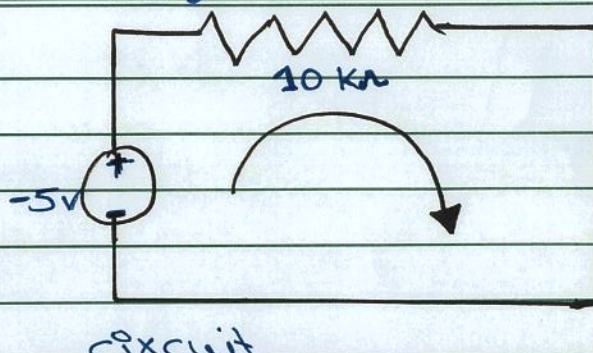
OR

$$P = 2.5 \text{ W}$$

Date: _____

(4)

(11)



In above circuit

$$V = -5 \text{ volt}$$

$$I = ?$$

$$P = ?$$

$$R = 10 \text{ K ohm} \Rightarrow 10 \times 10^3 \text{ ohm}$$

Solution:-

From ohm Law

$$V = IR$$

$$I = V/R$$

$$I = -5/10 \times 10^3$$

$$I = -0.0005 \text{ A}$$

OR

$$I = -0.5 \text{ mA}$$

Power consumed

$$P = V \cdot I$$

$$P = -5 \times -0.0005$$

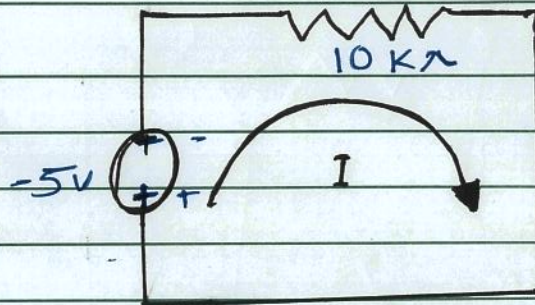
$$P = 0.0025 \text{ W}$$

$$P = 2.5 \text{ mW}$$

Date: _____

(5)

(iv)



In above The direction / polarity
polarity of voltage source changed
hence we take

$$V = -(-5) \Rightarrow -5V = -(-5)$$

$$V = 5V$$

From ohm law

$$V = IR$$

$$I = V/R$$

$$= -(-5) / 10 \times 10^3 \text{ ohm}$$

$$\Rightarrow I = 5 / 10 \times 10^3$$

$$I = 0.0005A$$

OR

$$I = 0.5mA$$

Hence power

$$P = I \cdot V$$

$$P = 0.0005 \times 5$$

$$P = 0.0025W$$

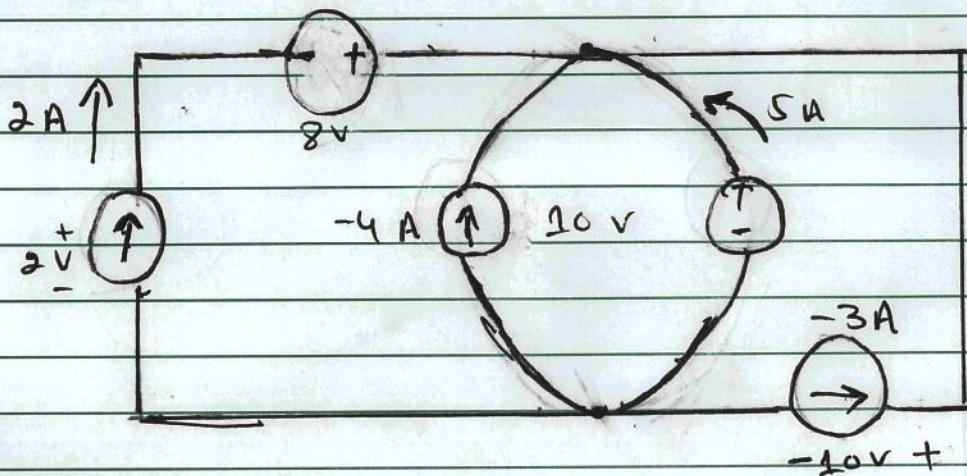
$$P = 2.5mW$$

Q#1

Date: B

(6)

B) Determine the Power supplied by the left most element in the circuit of following figure.



Solution:-

The left most element of the circuit is the 2V voltage source. Here we have to calculate power supplied by left most element i.e. 2V source.

We know that:-

$$P = I \cdot V$$

Given $V = 2V$

$$I = 2A$$

$$\Rightarrow P = 2V \times 2A$$

$$P = 4W$$

$$P = 4W$$

This 4 watt power is supplied power.

Q# 1

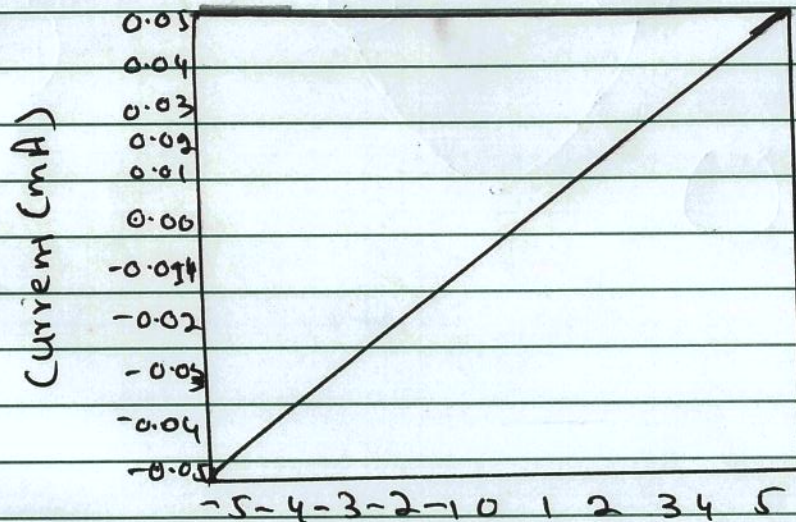
Date: C

(07)

C :- following figure depicts the current-voltage characteristic of three different resistive element. Determine the resistance of each. assuming the voltage and current are defined in accordance with the passive sign convention.

(A)

(B)



Solution:

We can find Resistance
From Ohm Law
 $V = IR$

$$\Rightarrow R = V/I \quad \text{---(1)}$$

above graph is linear/constant
we can take any point
from the graph -

Date: _____

(08)

let

$$I = 0.04 \text{ mA} = 0.04 \times 10^{-3}$$

$$V = 4 \text{ V}$$

Put in ①

$$\begin{aligned} \text{①} \Rightarrow R &= V/I \\ &= 4 / 0.04 \times 10^{-3} \\ &= \frac{4}{0.00004} \\ R &= 100000 \end{aligned}$$

$$R = 100 \times 10^3 \text{ ohm}$$

$$R = 100 \text{ K ohm}$$

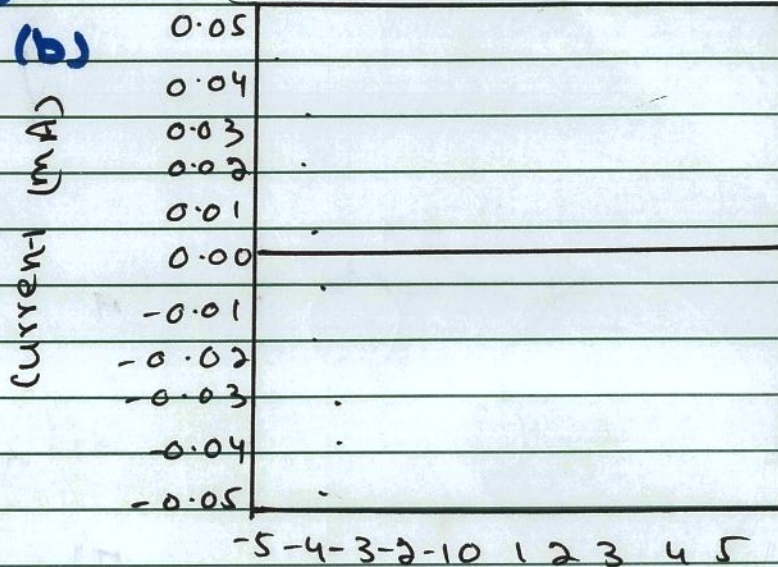
~~in Fig (i)~~
in Fig (i)

The resistor is 100 K ohm.

Date: _____

(09)

(b)



In above graph current (I) is zero.

We can take voltage from any point of graph
Let

$$V = 5 \text{ volt}$$

$$I = 0 \text{ mA} \Rightarrow 0 \text{ A}$$

From Ohm law

$$R = \frac{V}{I}$$

$$R = \frac{5}{0}$$

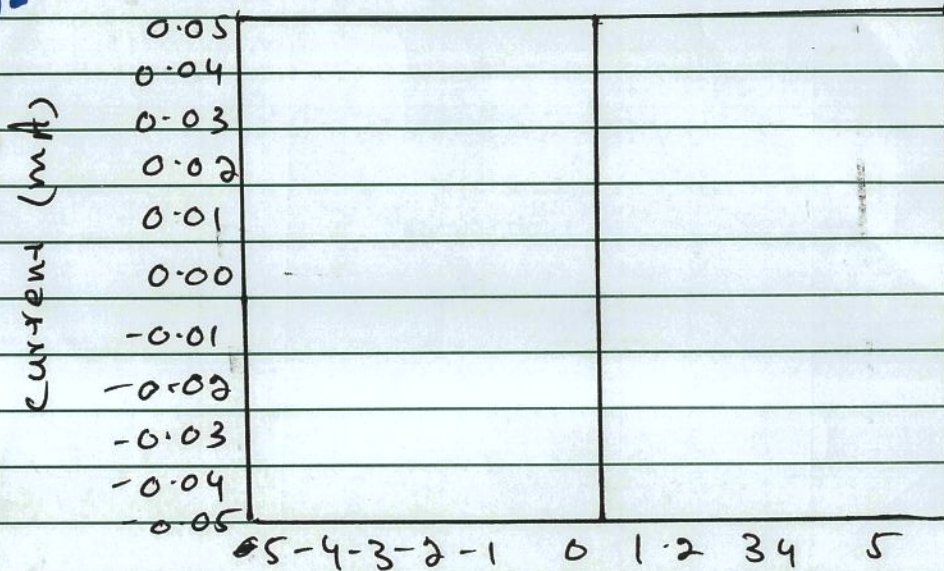
$R = \infty$ ohm in above graph

The current is zero and show infinite resistance.

Date: _____

(10)

(C)-



Voltage (V)
(C)

In above graph voltage is zero $V=0$ we can take current ~~from~~ from any point.

$$V = IR$$

$$R = V/I$$

$$R = 0/0.05 \text{ mA}$$

$$R = 0$$

above graph show zero resistor-

(11)

Date: Question #2

Part (A)

(A)

2) a- Refer to the circuits of following figure and answer the following.

- 1) How many distinct nodes are contained in the circuits?
- 2) How many elements are contained in the circuits?
- 3) How many branched does the circuit have?
- 4) Determine if each of the following represents a loop, a path, or neither!

(i) A to B

(ii) B to D to C to E

(iii) C to E to D to B to A to C

(iv) C to D to B to A to C to E

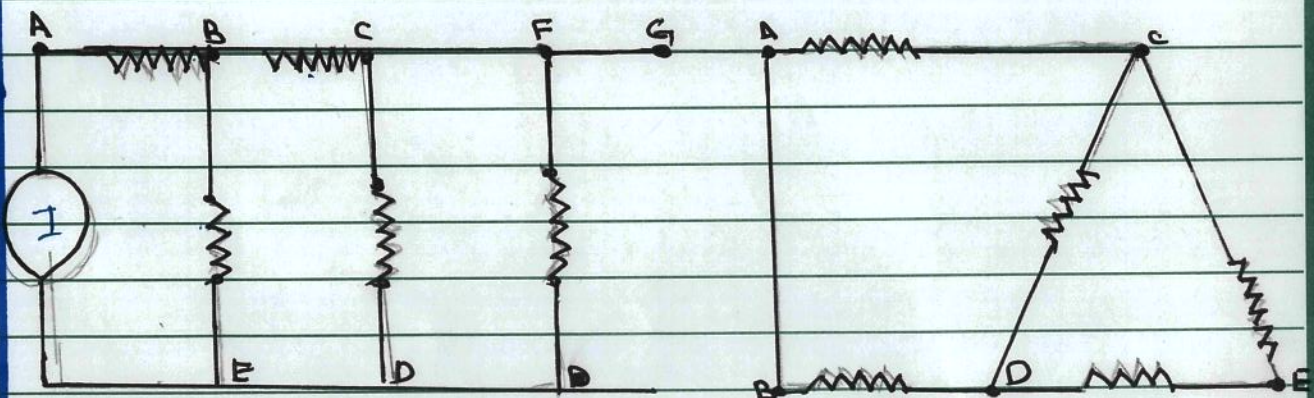


figure (a)

figure (b)

(12)

Date: _____

(1) By counting, ~~we~~ we get that the number of nodes in the circuit is 4.

(2) Number of elements
= 5 (5 resistor.)

(3) Number of branches in circuit is 5.

(4)

(i) Nither, we are on same node.

(ii) Only path:

we ~~have~~ ^{are} moved by 3 nodes & visit each once.

(iii) path & loop:

we moved by 7 nodes & the loop closed on "c".

(iv) Nither:

we visit node c ~~twice~~ twice but not finish in it.

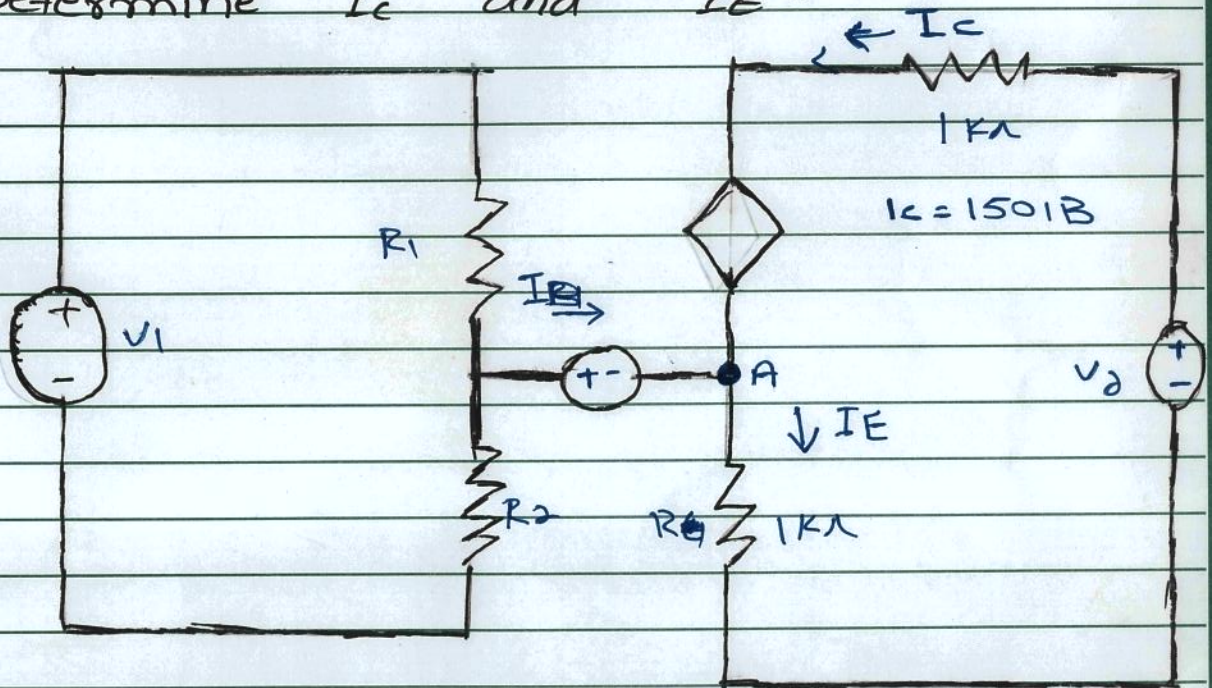
(13)

Date: Q 2

B

part : B:

for the circuit of the following (which is the model of the (DC) operation of a bipolar junction transistor biased in the forward active region). I_B is measured to be $100 \mu A$. Determine I_C and I_E .



Solution:

We have to find I_C & I_E

In order to find these current we use Kirchoff current law (KCL).

Date: _____

(14)

From KCL we know that

(1) Sum of all current in a node is equal to zero.

$$\sum_{i=1}^n I_n = 0$$

(a) OR

current entering node equal to current leaving node.

Now

From above fig:-

~~At~~

⊙ Node A:-

I_B and I_C entering node
but I_E leaving node.

~~I~~

$$I_B + I_C = I_E$$

OR

$$I_B + I_C - I_E = 0 \rightarrow (i)$$

Given That

$$I_B = 100 \text{ mA} = 100 \times 10^{-3} \text{ A} = 0.1 \text{ A}$$

$$I_C = 150 I_B$$

$$= 150 \times 100 \times 10^{-3} \text{ A}$$

$$I_C = 0.015 \text{ A}$$

Date: _____

(15)

TO Find I_E p.w. value
 I_B & I_C on eq ①

$$\text{①} \Rightarrow I_B + I_C - I_E = 0$$
$$I_E = I_B + I_C$$

$$I_E = 0.0001A + 0.015A$$

$$I_E = 0.0151A$$

RESULT

I_C	$I_C = 0.015A$
OR	$I_C = 15mA$
&	
	$I_E = 0.015A$
OR	$I_E = 15.1mA$

→ANS.

Date: _____

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Q 3:

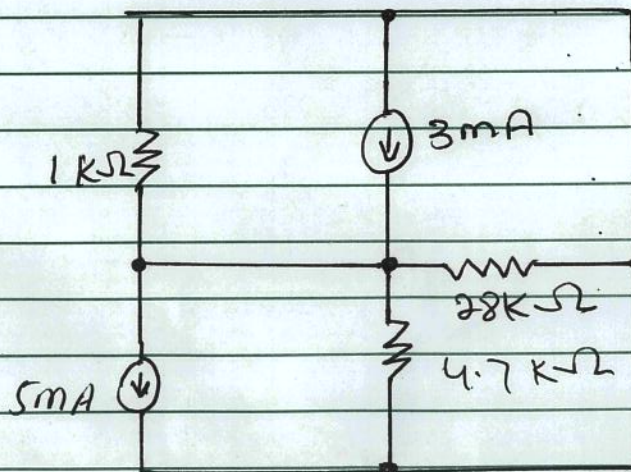
Part (a) :-

Although drawn so that it may not appear obvious at first glance, the circuit of following figure is in fact a Single-node-Pair Circuit.

a:- determine the Power absorbed by each resistor.

b:- determine the Power supplied by each current source.

c:- Show that the sum of the absorbed Power calculated in (a) is equal to the sum of the supplied Power calculation in (b).

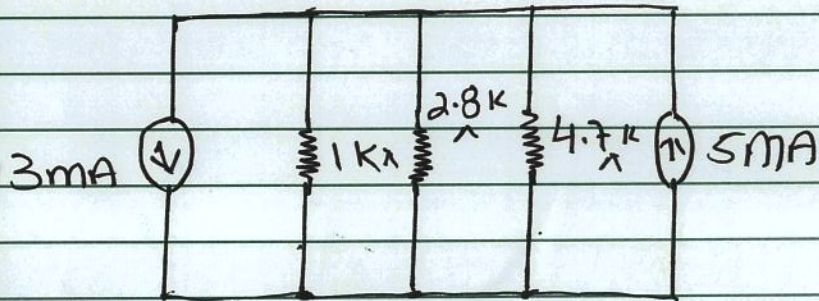


(17)

Date: _____

Solution!

by ~~b~~ Re-construct Fig



The current sources & resistors are parallel to each other.

$$I = -3 + 5$$

$$I = 2 \text{ mA}$$

$$I = 2 \times 10^{-3} = 0.002 \text{ A}$$

Now

$$\frac{1}{R_{eq}} = \frac{1}{1} + \frac{1}{2.8} + \frac{1}{4.7}$$
$$= \frac{658 + 235 + 140}{658}$$

$$\frac{1}{R_{eq}} = \frac{1033}{658}$$

$$R = 658 / 1033$$

$$R = 0.637 \text{ K Ohm}$$

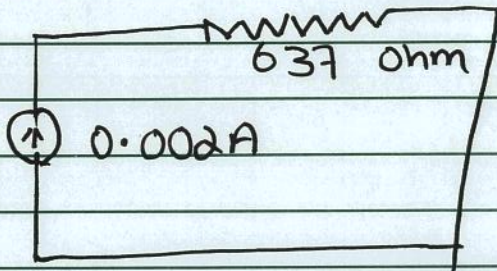
$$R = 0.637 \times 10^3 \text{ Ohm}$$

$$R = 637 \text{ Ohm}$$

(18)

Date: _____

The circuit be come



by Ohm law

$$V = IR$$
$$= 0.002 \times 637$$

$$V = 1.27 \text{ Volt}$$

Now

power observed by ~~1K~~ 1K resistor

$$P_{1K} = I_{1K} \times V \quad \text{--- (1)}$$

Now

$$I_{1K} = \frac{V}{R_{1K}} = \frac{1.27}{1000}$$

$$I_{1K} = 0.00127 \text{ A}$$

$$P_{1K} = 0.00127 \text{ A} \times 1.27 \text{ V}$$

$$P_{1K} = 0.00161 \text{ W}$$

OR \rightarrow

$$P_{1K} = 1.6 \text{ mW}$$

(19)

Date: _____

Power observed by 2.8 k ~~ohm~~ resistor

$$I(2.8k) = \frac{V}{R}$$
$$= \frac{1.27}{2.8}$$

$$I(2.8k) = 0.45 \text{ mA}$$
$$\Rightarrow I(2.8k) = 0.00045 \text{ A}$$

NOW

$$P(2.8k) = 0.00045 \times 1.27$$

OR

$$P(2.8k) = 0.00057 \text{ W}$$
$$P(2.8k) = 0.57 \text{ mW}$$

Power by 4.7 k resistor

$$I(4.7k) = \frac{V}{R} = \frac{1.27}{4.7}$$

$$I(4.7k) = 0.27 \text{ mA}$$

$$I(4.7k) = 0.00027 \text{ A}$$

NOW

$$P(4.7k) = 0.00027 \times 1.27$$

OR

$$P(4.7k) = 0.000343 \text{ W}$$
$$P(4.7k) = 0.343 \text{ mW}$$

(20)

Date: _____

Now

Power ~~supplied~~ supplied
by 5mA source

$$P(5mA) = I \cdot V$$

$$= 5 \times 10^{-3} \times 1.27$$

$$= 0.005 \times 1.27$$

OR

$P(5mA) = 0.00635 W$
$P(5mA) = 6.35 mW$
$P(5mA)$

Power supplied by 3mA source.

$$P(3mA) = 3 \times 10^{-3} \times 1.27$$

$$= 0.00381 W$$

OR

$P(3mA) = 0.00381 W$
$P(3mA) = 3.81 mW$

Now

Power observed by 'R' = power supplied

$$1.6 mW + 0.57 mW + 0.343 mW = 2.513 mW$$
$$= 6.3 mW + 3.8 mW$$

$2.5 = 2.5 \rightarrow \text{proved}$

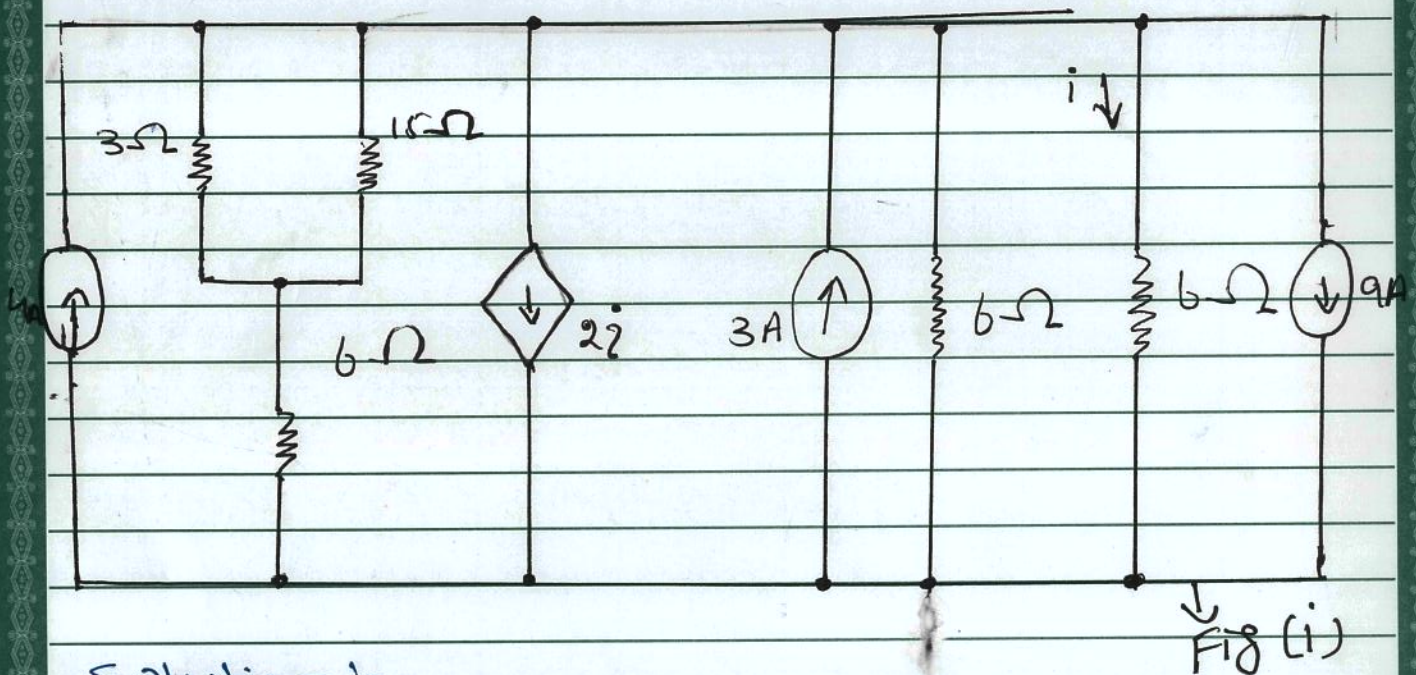
power observed = power supplied.

Q 3 (B) (21)

Part (B)

Date: _____

(B) Determine the Power absorbed by the 15Ω resistor in the ~~circuit~~ circuit of the following figure.



Solution:-

In order to find power observed by 15Ω resistor we ~~have to find~~ we need voltage & current
As

$$P = I \cdot V$$

or

$$P = V^2 / R$$

(22)

Date: _____

In above fig all current source are parallel to each other, so we can add them

$$I_{\text{total}} = 4 - 2i + 3 - 9$$

$$I_{\text{total}} = (-4 - 2i)$$

and also,

3 Ω & 15 Ω resistors are parallel to each other but in series to 6 Ω

Now

The equivalent resistor of these three resistors given by

$$R = \left(\frac{3 \times 15}{3 + 15} \right) + 6$$

$$R = \frac{45}{18} + 6$$

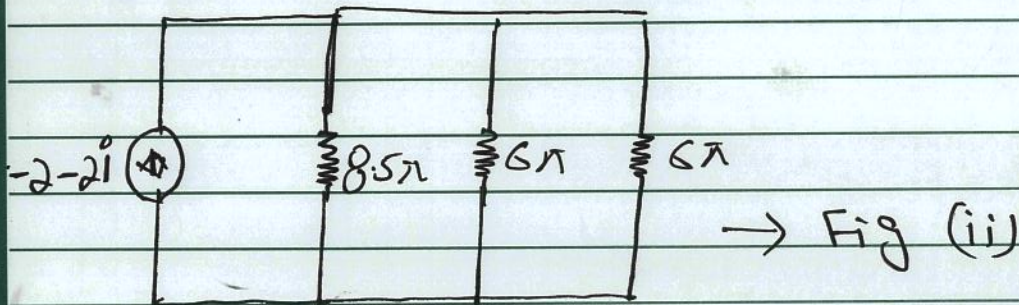
$$2.5 + 6$$

$$R = 8.5 \text{ ohm}$$

(23)

Date: _____

Now The Fig become



In Fig (ii) all resistor are parallel to each other.

$$\text{Now } \frac{1}{R(\text{eq})} = \frac{1}{8.5} + \frac{1}{6} + \frac{1}{6}$$

$$= \frac{12+17+17}{102}$$

$$\frac{1}{R(\text{eq})} = \frac{46}{102}$$

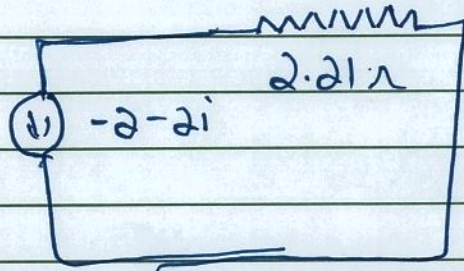
$$R(\text{eq}) = \frac{102}{46}$$

$$R(\text{eq}) = 2.21 \text{ ohm}$$

Date: _____

(24)

now we can draw Fig (ii) as:



now ~~by~~ from ohm law

$$V = IR$$

$$V = (-2 - 2i) \times (2.21 \Omega) \rightarrow *$$

now the voltage across 6Ω resistor, ~~is~~

$$V = IR \Rightarrow V = i \times 6$$

$$V = 6i \rightarrow (i)$$

The voltage across 6Ω resistor & total ~~across~~ across circuit will be same because it's parallel circuit so ~~we~~ its mean that

$$-2 - 2i \times (2.21) = 6i$$

$$-4.42 - 4.42i = 6i$$

$$-4.42 = 6i + 4.42i$$

$$10.42i = -4.42$$

$$-4.42$$

$$I = \frac{-4.42}{10.42}$$

(25)

Date: _____

$$I = 0.42 \text{ A}$$

This (0.42 A) current through 6 ohm resistor

$$\Rightarrow V = 6I$$
$$V = 6 \times (0.42)$$
$$V = -2.5 \text{ V}$$

Now

To calculate power observed by 15 ohm resistor we have to find voltage across it. This (-2.5) is not used for this resistor b/c there is 6 ohm resistor in series with 15 ohm resistor.

$$V_{(15\Omega)} = \frac{15}{6+15} \times V$$

$$= 0.714 \times 2.5$$
$$V_{(15\Omega)} = 1.78 \text{ V}$$

$$P_{(15\Omega)} = (1.78)^2 / 15$$
$$= 3.18 / 15$$

$$P_{(15\Omega)} = 0.212 \text{ W} \rightarrow \text{ANS.}$$

THE END