

Submitted To : Engr. ADEED

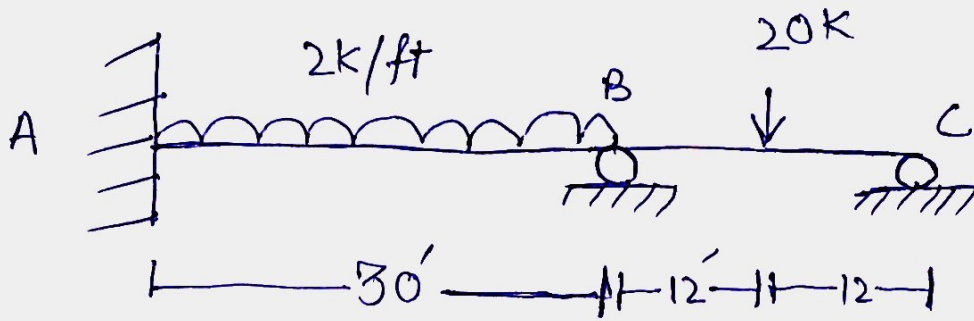
Submitted by : Mudasir

Subject : Structure Analysis. II

ID-NO : 7755

Date : 21 Aug 2020

Question No # 01



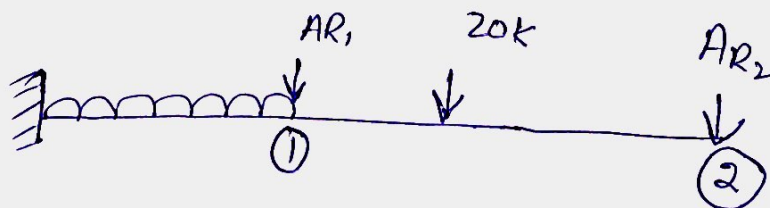
$$EI = \text{Constant}$$

Solution:

Structural Indeterminacy = ?

Step # 01

Select Redundant Actions

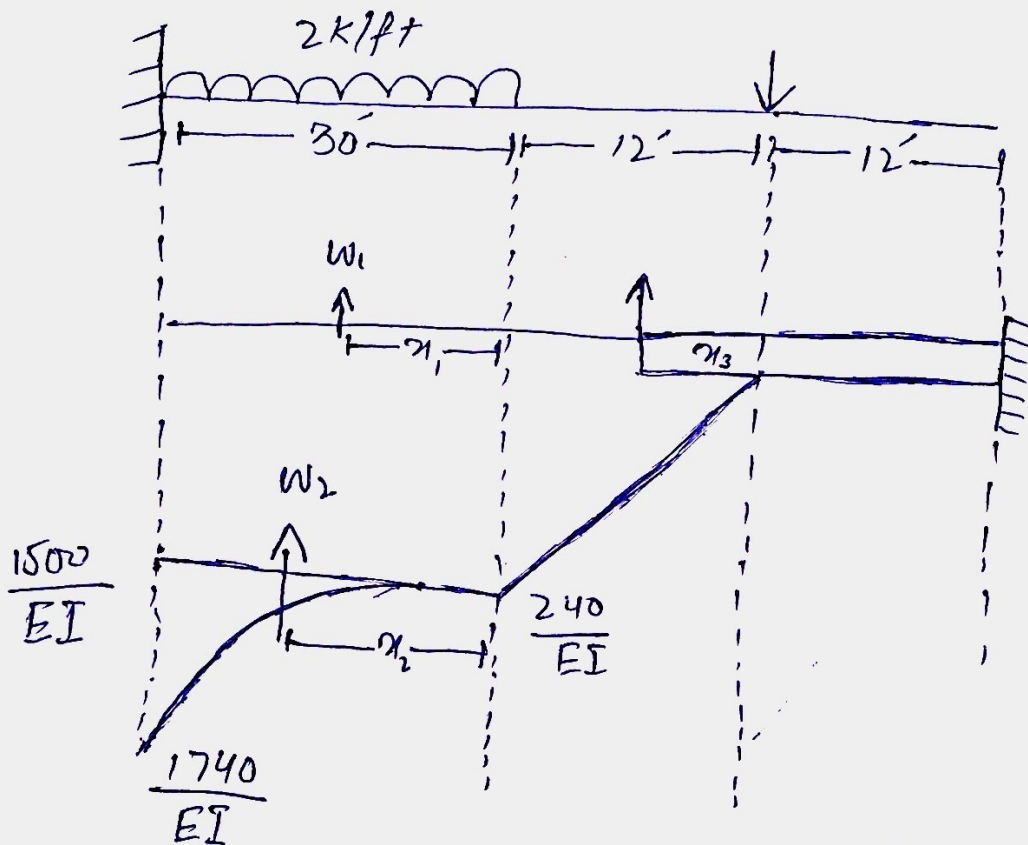


$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$[DRS] = [DRL] + [F] \times [AR]$$

Step # 02

Compute the values of [DRL]



$$20 \times 12 = 240$$

$$20 \times (12 + 30) + 2 \times 30 \times 15 = 1740$$

$$w_1 = 1500 \times 30 = 45000$$

$$w_2 = \frac{1}{3} \times 30 \times 240 = 2400$$

$$w_3 = \frac{1}{2} \times 12 \times 240 = 1440$$

$$\alpha_1 = \frac{b}{2} = \frac{30}{2} = 15'$$

$$\alpha_2 = \frac{3}{n+2} \times L = \frac{3}{2+2} \times 30 = 22.5'$$

$$\alpha_3 = \frac{2}{3} \times L = \frac{2}{3} \times 12 = 8'$$

Now Finding DRL

$$DRL_1 = w_1 (r_1) + w_2 (r_2)$$

$$DRL_1 = 45000(15) + (2400)(22.5)$$

~~or applying~~ ~~the~~ ~~same~~ ~~method~~ ~~as~~ ~~before~~

$$DRL_1 = 729000 \text{ EI}$$

$$DRL_2 = w_1 (r_1 + 24) + w_2 (r_2 + 24) + w_3 (r_3 + 12)$$

$$= 45000(15+24) + 2400(22.5+24) + 1440(8+12)$$

$$= 1755000 + 111600 + 28800$$

$$DRL_2 = 1895400 \text{ EI}$$

So

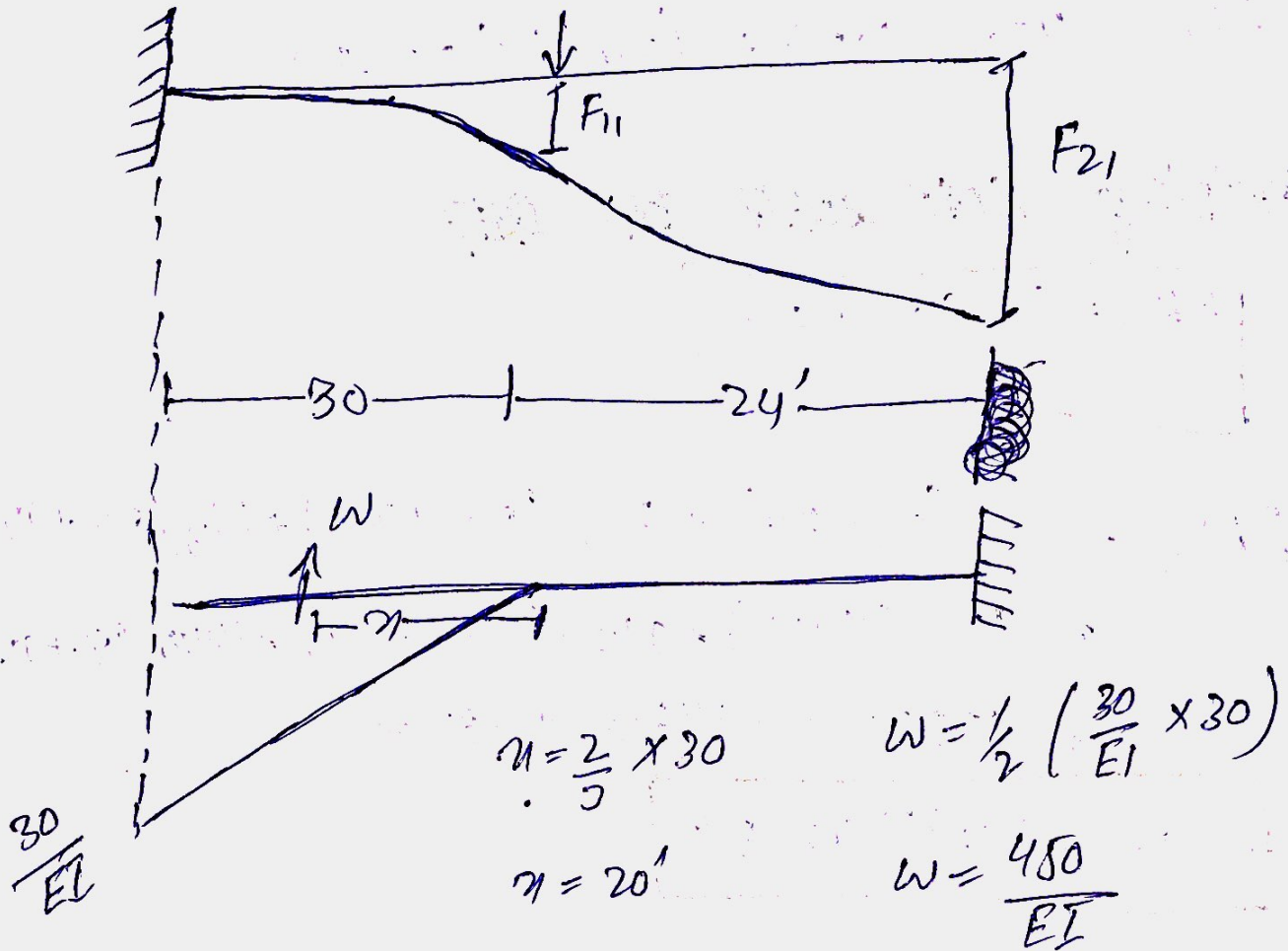
$$DRL = \frac{I}{EI} \begin{bmatrix} 729000 \\ 1895400 \end{bmatrix}$$

Step # 03

flexibility matrix

$$[F]_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

a) Applying unit load on AR,

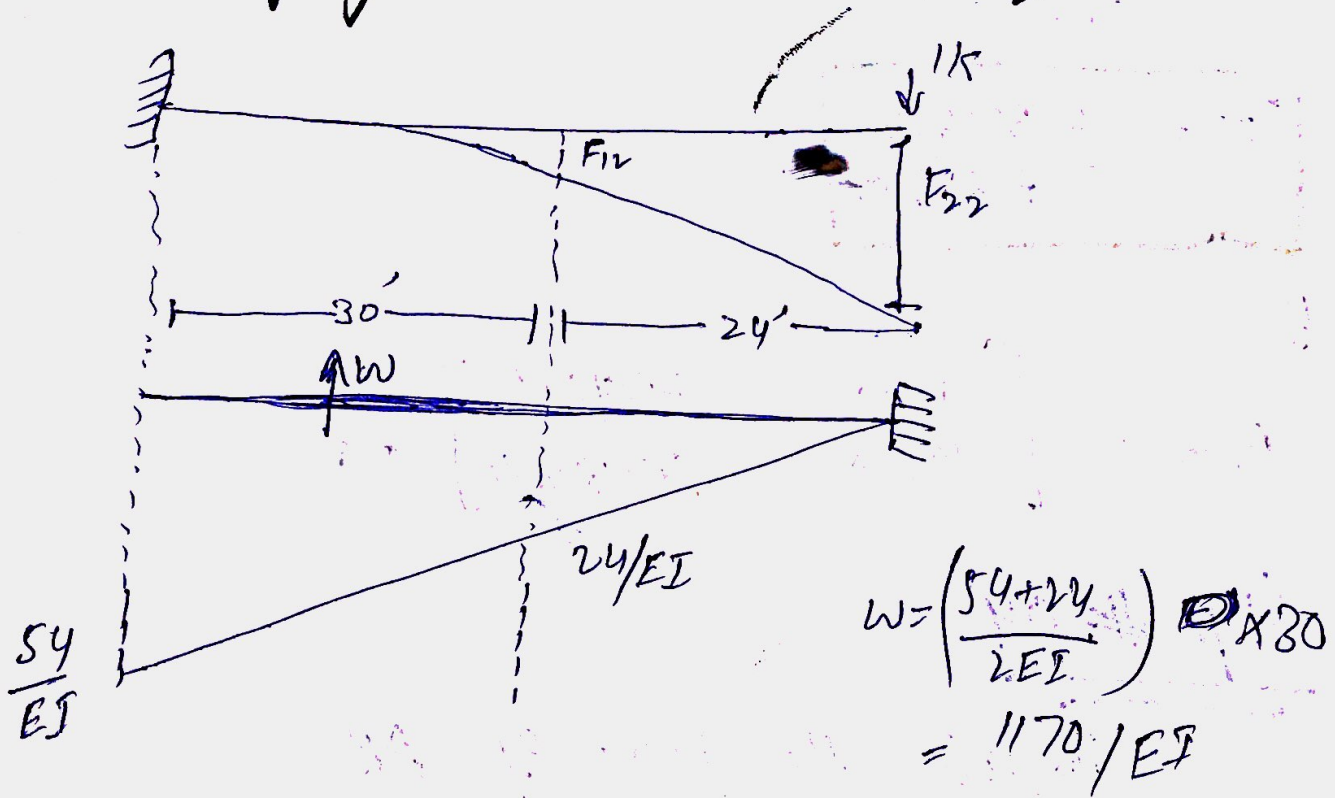


~~30~~ 30,

$$F_{11} = \frac{450}{EI} (20) = 9000/EI$$

$$F_{21} = \frac{450}{EI} (20+24) = 19800/EI$$

(B) Applying Unit load on AR_2



$$W = \left(\frac{54+24}{2EI} \right) \times 80 = 1170/EI$$

Now the distance

$$m = \frac{2}{3} \left[\frac{b + 2(a)}{a+b} \right]$$

$$= \frac{30}{3} \left[\frac{24 + 2(54)}{54 + 24} \right] = 16.92$$

$$\rightarrow F_{12} = \frac{1170}{EI} \times 16.92$$

$$F_{12} = \frac{19796.4}{EI}$$

$$F_{22} = \frac{1170}{EI} \times (16.92 + 24)$$

$$F_{22} = \frac{47876.4}{EI}$$

Hence

$$F_{2 \times 2} = \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix} \frac{1}{EI}$$

Step # 04

Compute the value of AR

$$[DRS] = [DRL] + [F] \times [AR]$$

$$AR = [DRS - DRL] \times [F]^{-1}$$

$$[F]^{-1} = \frac{1}{|F|} \text{Adj } F$$

$$= \frac{1}{\begin{vmatrix} 9000 & 19796.4 \\ 19800 & 47896.4 \end{vmatrix}} \times \text{Adj} \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix}$$

$$|F| = (9000 \times 47876.4 - 19796.4 \times 19800)$$

$$|F| = (430987600 - 391968720)$$

$$|F| = 38918880$$

$$\text{Adj } A = \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 0 - 729000 \\ 0 - 1895400 \end{bmatrix} \frac{1}{EI} \times \frac{1}{38918880} \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$= \begin{bmatrix} -729000 \\ -1895400 \end{bmatrix} \frac{1}{EI} \times \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 66.193 \\ -67.505 \end{bmatrix}$$

QNO # 02

FORCE METHOD

* It is also known as flexibility matrix method or compatibility method

* In force method the unknowns are taken as force or reaction

* In this the number of redundants = D_s

* In this the ~~number~~ forces are found by compatibility equations of displacements.

* In this the type of indeterminacy is static indeterminacy

* It is suitable when $D_s < D_k$

Displacement Method

* It is also called as equilibrium method or stiffness method matrix.

* In displacement method the unknowns are taken as joint displacements (θ, Δ)

* In this the number of Redundants = D_k

* In this the displacements are found by equilibrium equations of forces

* In this the type of indeterminacy is kinematic indeterminacy

* It is suitable when $D_s > D_k$

Suitable Method

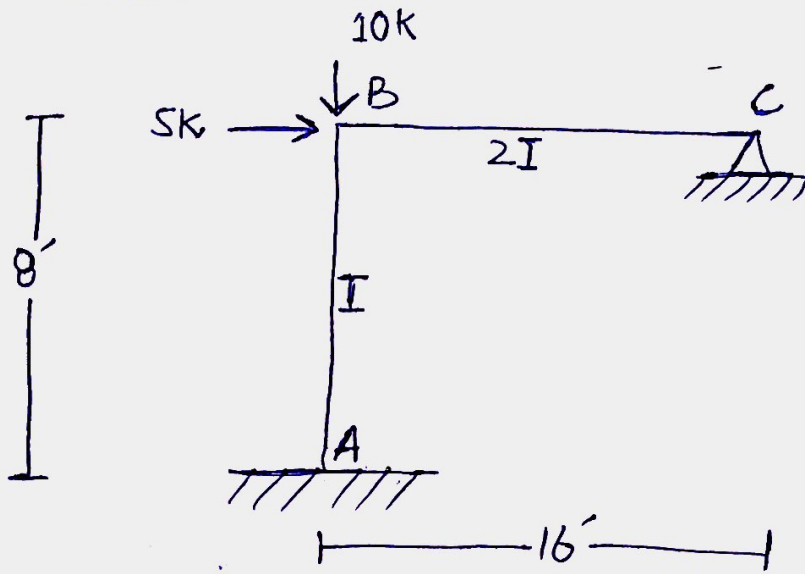
⇒ For analysis of structure of matrix approach both the force method or displacement method can be used depend upon situations

★ When the degree of Static Indeterminacy (D_s) is less than the degree of Kinematic Indeterminacy (D_k) i.e. $D_s < D_k$ than it is suggested to use force method of analysis.

★ When the degree of Static Indeterminacy (D_s) is more than the degree of Kinematic Indeterminacy (D_k), $D_k < D_s$

than it is suggested to use "Displacement method of Analysis".

Question # 03



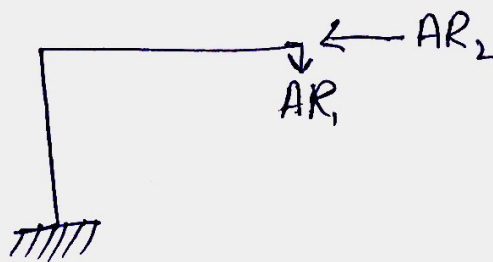
$E = \text{Constant}$

Solution:

Total Statical Indeterminacy
 $R - 3 = 5 - 3 = 2^{\circ}$

Step # 01

Identifying Redundant actions



$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Step # 02

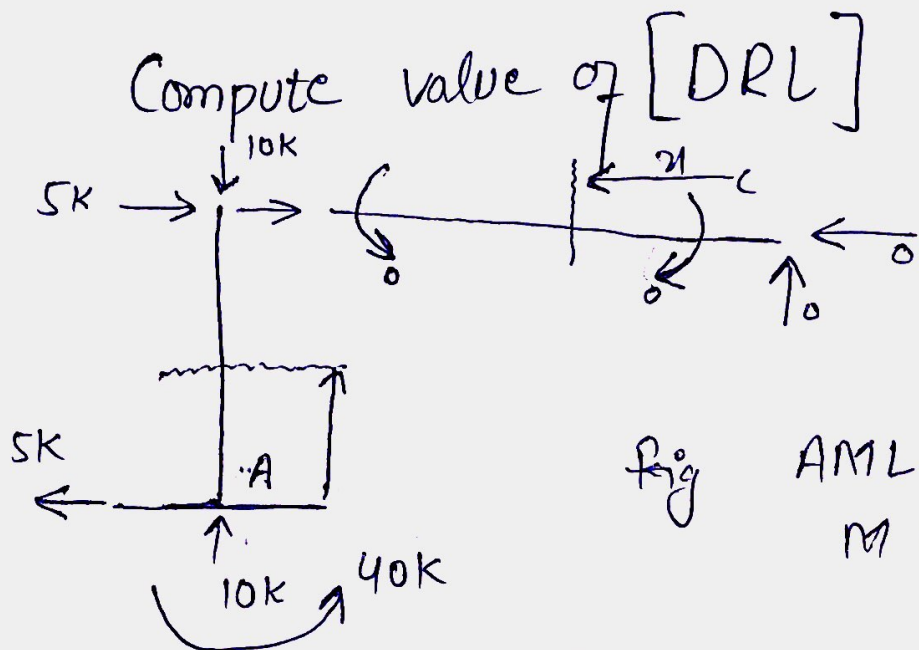


Fig AML value
M value

Step # 03

(a)

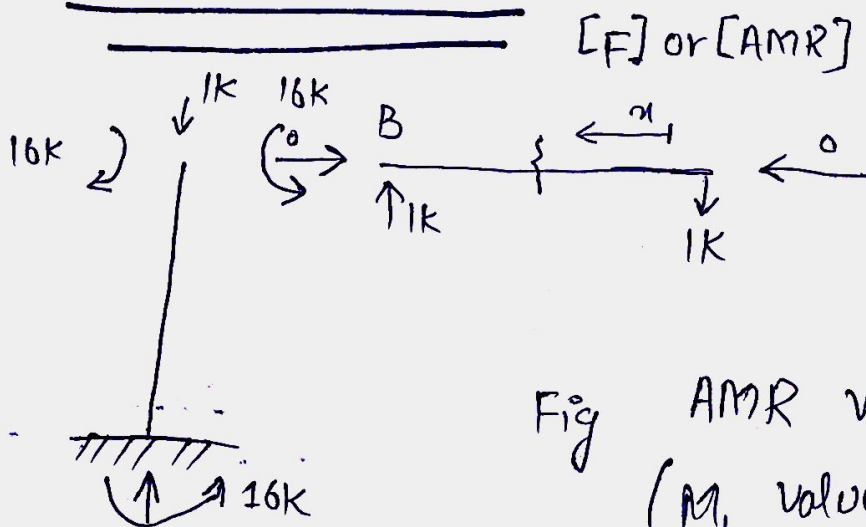


Fig AMR value
(M, values)

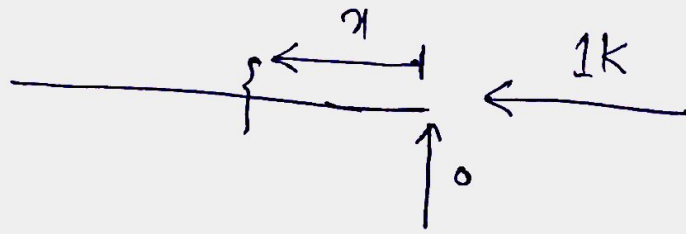
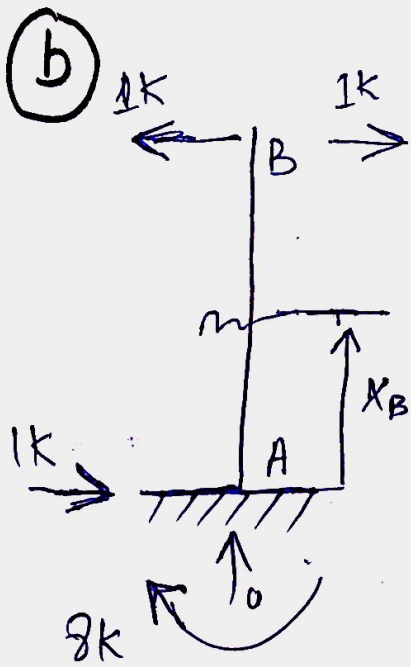


Fig AMR value
[M_2 value]

| | | |
|--------|---------|------|
| MEMBER | AB | BC |
| Origin | A | C |
| Limits | 0-8 | 0-16 |
| I | I | 2I |
| M | $5x-40$ | 0 |
| M_1 | -16 | -x |
| M_2 | $8-x$ | 0 |

→ Finding values of DRL

$$DRL_1 = \int_0^8 \frac{M_{AB} \cdot M_1(AB)}{EI} + \int_0^{16} \frac{M_{BC} \cdot M_2(BC)}{EI}$$

$$= \int_0^8 \frac{(5x-40)(-16) dx}{EI} + \int_0^{16} \frac{0.2x}{E(2I)} dx$$

$$DRL_1 = \frac{2560}{EI}$$

$$DRL_2 = \int_0^8 \frac{(5x-40)(8-x) dx}{EI} + \int_0^{16} \frac{0.2x}{E(2I)} dx$$

$$DRL_2 = -\frac{853.33}{EI}$$

→ Compute Flexibility Matrix

$$F_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

$$\Rightarrow F_{11} = \int_0^8 m_1^2(AB) + \int_0^{16} \frac{m_1^2(BC)}{EI}$$

$$= \int_0^8 \frac{(-16)^2 d\eta}{EI} + \int_0^{16} \frac{\eta^2 d\eta}{E(2I)}$$

$$F_{11} = \frac{2730 \cdot 67}{EI}$$

$$\begin{aligned} \rightarrow F_{12} = F_{21} &= \int_0^8 m_1(AB) \cdot m_2(AB) + \int_0^{16} m_1(BC) \cdot m_2(BC) \\ &= \int_0^8 \frac{(-16)(8-\eta)}{EI} d\eta + \int_0^{16} \frac{(\eta)(0)}{E(2I)} d\eta \end{aligned}$$

$$F_{12} = F_{21} = -\frac{512}{EI}$$

$$\begin{aligned} \Rightarrow F_{22} &= \int_0^8 (m_1)^2 AB d\eta + \int_0^{16} (m_2)^2 BC d\eta \\ &= \int_0^8 \frac{(8-\eta)^2}{EI} d\eta + \int_0^{16} \frac{0^2}{E(2I)} d\eta \end{aligned}$$

$$F_{22} = 170 \cdot 67$$

As we know that

$$[DRS] = [DRL] + [AR] \times [F]$$

$$[AR] = \frac{[DRS] - [DRL]}{[F]}$$

$$[AR] = [F]^{-1} \times [DRS - DRL]$$

$$= EI \begin{bmatrix} 2730.67 & -512 \\ -512 & 170.67 \end{bmatrix} \times \begin{bmatrix} 0 - 2560 \\ 0 + 853.33 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} -0.00028 \\ 4.97 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$