Name: SAMIULLAH

ID: 17008

Submitted By: MUHAMMAD ABRAR KHAN

Q1(a) Differentiate 
$$\frac{2x^{2}-3x^{2}+5}{x^{2}+1}$$
 with respect to x.

(a) Soli.  $\frac{d}{dx} \left( 2x^{2}-3x^{2}+5 \right)$ 

=>  $(x^{2}+1) \frac{d}{dx} \left( 2x^{2}-3x^{2}+5 \right) - (2x^{2}-3x^{2}+5) \frac{d}{dx} (x^{2}+1)$ 

=>  $(x^{2}+1) \frac{d}{dx} \left( 2x^{2}-3x^{2}+5 \right) - (2x^{2}-3x^{2}+5) \frac{d}{dx} (x^{2}+1)$ 

=>  $(x^{2}+1) \frac{d}{dx} \left( 2x^{2}-1 \right) - (2x^{2}-3x^{2}+5) \left( 2x \right)$ 
 $(x^{2}+1)^{2}$ 

=>  $\frac{dx}{dx} \left( x^{2}+1 \right) \left( x^{2}-1 \right) - \left( 2x^{3}-3x^{2}+5 \right) \left( 2x \right)$ 
 $(x^{2}+1)^{2}$ 

=>  $\frac{dx}{dx} \left( x^{2}+1 \right) \left( x^{2}-1 \right) - \left( 2x^{3}-3x^{2}+5 \right) \left( 2x \right)$ 
 $x^{4}+2x^{2}+1$ 

(21(b) Differentiale 
$$(x^2+1)^2$$
 with respect to x

(b) Sol: 
$$y = (x^2 + 1)^2$$
  
 $x^2 - 1$ 

=> 
$$\frac{dy}{dx} = \frac{(x^2+1)^2}{x^2-1}$$

$$= \frac{(x^{1}-1)\frac{d}{dx}(x^{1}+1)^{1}-(x^{2}+1)^{1}\frac{d}{dx}(x^{1}+1)}{(x^{1}-1)^{2}}$$

=> 
$$\frac{(x^{2}-1)\lambda(x^{2}+1)\frac{d}{dx}(x^{2}+1)(x^{2}+1)^{2}(3x)}{(x^{2}-1)^{2}}$$

$$= \frac{(x^{2}-1) \left[\lambda (x^{2}+1)^{2}x\right] - (x^{2}+1)^{2}(2x)}{(x^{2}-1)^{2}}$$

$$= \frac{(x^{2}-1) \left[ (4x(x^{2}+1)-(x^{2}+1)^{2}(3x) - (x^{2}-1)^{2} \right]}{(x^{2}-1)^{2}}$$

$$= \frac{(x^2-1)^2}{(x^2-1)^2}$$

$$= \frac{(x^{2}-1)}{(2x)(x^{2}+1)[2x(x^{2}-1)-x^{2}+1]}$$

$$= \frac{(2x)(x^{2}+1)[2x(x^{2}-1)-x^{2}+1]}{x^{2}+2x^{2}+1}$$

$$Q_{\alpha}(\alpha)$$
 Find  $\frac{dy}{dx}$  if  $y=(1+2\sqrt{x})^{3}$ ,  $x^{2/3}$  using chain rule:

(a) Sol: 
$$\frac{dy}{dx} = (1+2\pi)^3 \cdot x^{2/3}$$
 (et x=4

=) 
$$\frac{dy}{dx} = (1+2 \pi)^{\frac{3}{2}} u^{-\frac{1}{3}} + u^{\frac{2}{3}} (3(1+2 \pi)^{\frac{3}{2}} \frac{1}{n})$$

=> 
$$\frac{dx}{du} = 1$$
 =>  $\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$ 

(b) Find 
$$\frac{dy}{dx}$$
 if  $y = \frac{V_{1-x}}{1+x}$  using chain rule:  
(b) Sol: Let  $\frac{1-x}{1+x} = u$ 

$$= \frac{\partial u}{\partial x} = \frac{(1+x)(-1) - (1-x)(1)}{(1+x)^2}$$

$$= \frac{-(1+x) - (1-x)}{(1+x)^2}$$

$$= \frac{-1-x-1+x}{(1+x)^2} = \frac{-2}{(1+x)^2}$$

$$= \frac{\partial y}{\partial u} = \frac{1}{u} = \frac{1}{2} \frac{1}{u} = \frac{1}{2} \frac{1}{u} \text{ using chain rule}$$

$$= \frac{\partial y}{\partial x} = \frac{1}{u} \times \frac{\partial y}{\partial u} \times \frac{\partial y}{\partial u}$$

$$= \frac{1}{2} \frac{1}{u} \times \frac{1}{u} \times \frac{1}{u} \times \frac{1}{u}$$

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$$= \frac{1}{u} \times \frac{1}{u} \times \frac{1}{u} \times \frac{1}{u} \times \frac{1}{u}$$

$$= \frac{1}{u} \times \frac{$$

(a) sol: 
$$\int \frac{1}{\sqrt{x^3}} dx$$

$$= \int \frac{1}{(x^3)^{1/2}} dx$$

$$= \int \int \frac{1}{(x^3)^{1/2}} dx$$

$$= \int \int \frac{1}{(x^3)^{1/2}} dx$$

$$= \int \frac{1}{x^{-3/2}} dx$$

$$= \frac{x^{-3/2+1}}{x^{-3/2}+1} + C$$

$$= \frac{x^{-3/2+1}}{x^{-1/2}} + C$$

$$= \frac{1}{\sqrt{x^3}} dx = \frac{-2}{\sqrt{x}} + C$$

(b) Sol: 
$$\int \frac{1}{(6x+7)^6} dx$$
  
=  $\int (6x+7)^6 dx$   
=  $\int (6x+7)^6 dx$   
((se again  $\int x^n dx = \frac{x^{n+1}}{n+1} + c$   
=  $\frac{1}{6} \int (6x+7)^6 (6) dx$  (1/4×6) = 1  
=  $\frac{1}{6} \int \frac{(6x+7)^{-6+1}}{(6x+7)^6} + c$