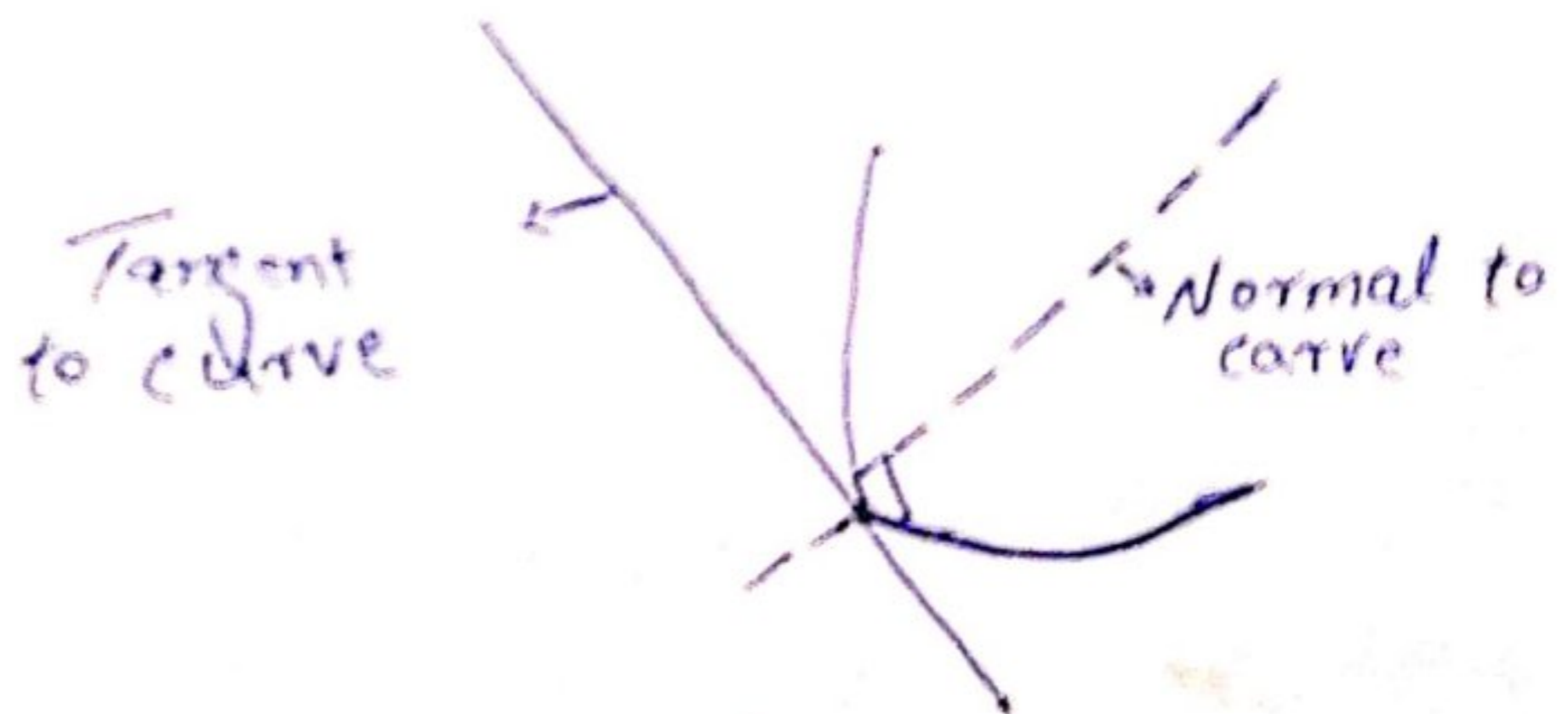


171
① We use the derivatives to determine the maximum and minimum values of particular functions (e.g., cost, strength, amount of material used in building, profit, loss etc.)

⇒ Derivatives are met in many engineering and science problems, especially when modeling the behavior of moving objects. Our discussion begins with some general application which we can then apply to specific problems.

Application of Derivatives.

- ① Tangents And Normals - A tangent to a curve is a line that touches the curve at one point and has the same slope as the curve at that point. A normal to a curve is a line perpendicular to a tangent of the curve.



notes- we can find the (2) Slope of a tangent at any point (x, y) using $\frac{dy}{dx}$

Tangents- If we are traveling in a car around a corner and we drive over some-thing slippery on the road like oil water and our car starts to skid it will continue in a direction tangent to the curve.

Normals- the spokes of a wheel etc placed normal to the circular shape of the wheel at each point where the spoke connects with the center.

① Newton method- the process involves making a guess at the true solution and then applying a formula to get a better guess and so on until we arrive at an acceptable approximation for the solution

If we wish to find x so that $f(x) = 0$ then we guess some initial value x_0 which is also to desired solution and then we get a better approximation using Newton Method

$$x_1 = x_0 - \frac{f(x_0)}{f'(x_0)}$$

③ Related Rates: - If ^{have a} two variables both vary with respect to time and relation between them we can express the rate of change of one in terms of one another that is we will be finding $\frac{dz}{dt}$ for some function $z(t)$

(4) Curvilinear Motion: - $v = \frac{ds}{dt}$, $a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$

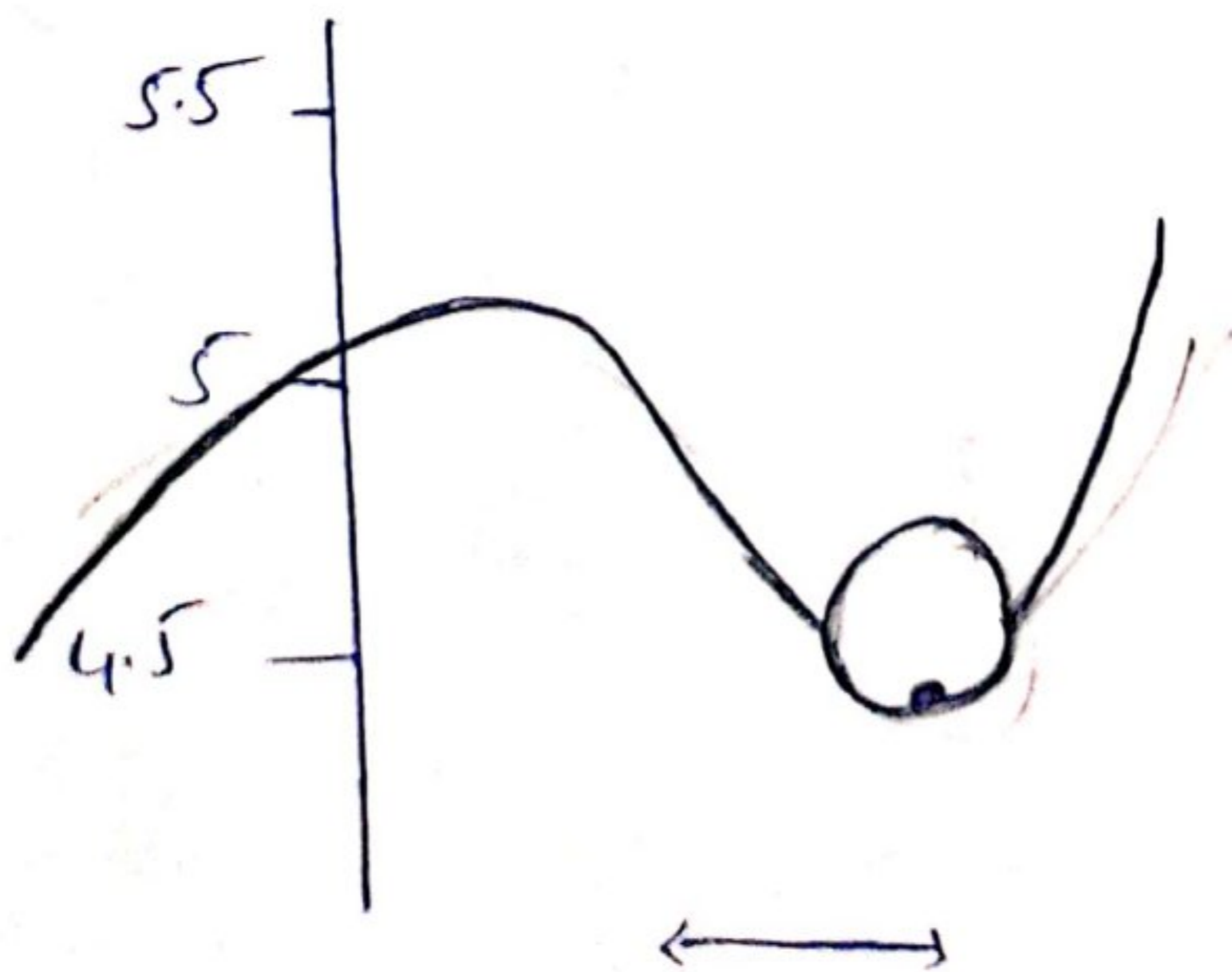
these formulae are only appropriate for rectilinear motion (velocity and acceleration in a straight line). this is inadequate for most real situations, so we introduce here the concept of curvilinear motion, where an object is moving in a plane along a specified curved path. we generally express the x and y components of the motion as function of time this form is called parametric form

(5) Radius of Curvature: (4)

$$\text{Radius of curvature} = \left[1 + \left(\frac{dy}{dx} \right)^2 \right]^{3/2}$$

The radius of curvature of the curve at a particular point is defined as the radius of the approximating circle. This radius changes as we move along the curve. The formula for the radius of curvature at any point

is for the curve $y = f(x)$



Application of Integration: ⑤

Integration: - The process of finding a function, given its derivative is called integration or anti

differentiation

1) If $F'(x)$ we say $F(x)$ is an anti-derivative of $f(x)$

2) It is usually used to find the area.

1) Shear Force and Bending Moment:

Shear force and Bending moment are one of the important parameters for structural design. These parameters affect a structure a lot.

2) Take example of a rod suspended between two horizontal supports and some load is applied at the centre. With applied load the beam will bend.

⇒ Some force will develop inside the rod which will try to break the rod.

in direction of force that force is called Shear force and produce of that force with distance from either end is bending moment.

(2) Length of curve:- Corrugated Iron Sheetings:-

2) Corrugated iron is used extensively throughout the world as a versatile building material. Bending the material into a regular sine wave pattern gives it greater strength than if a flat sheet is used.

⇒ so interation is used to find out how wide should ~~the flat sheet~~ be to given as a corrugated sheet to required width.

(3) Area under a curve by Integrations

In Civil engineering when we are dealing with curve or structure having curves then may need to find the area under the curve which

constructed so w(f) integration for this purpose

$$\text{Area } \int_a^b f(x) dx$$

4) Moment of Inertia by Integration:

moment of inertia is a geometrical property of a section of a structural member which is required to measure its resistance bending and buckling
 \Rightarrow a moment of inertia about x -axis

$$I_x = \int_A y^2 dA$$

where y is the y -coordinate of the different element of Area dA

\Rightarrow a moment of inertia about y -axis

$$I_y = \int_A x^2 dA$$

where x is the x -coordinate of element dA .

5) Centroid of an Area By (8)

25. In tilt-slab construction we have a concrete wall (with doors and windows cut out) which we need to raise into position we don't want the wall to crack as we raise it so we need to know the centre of mass of the wall we can find the centroid of an area with straight side, then we will extend the concept to area with curve side, where we will use integration

