

Date \_\_\_\_\_

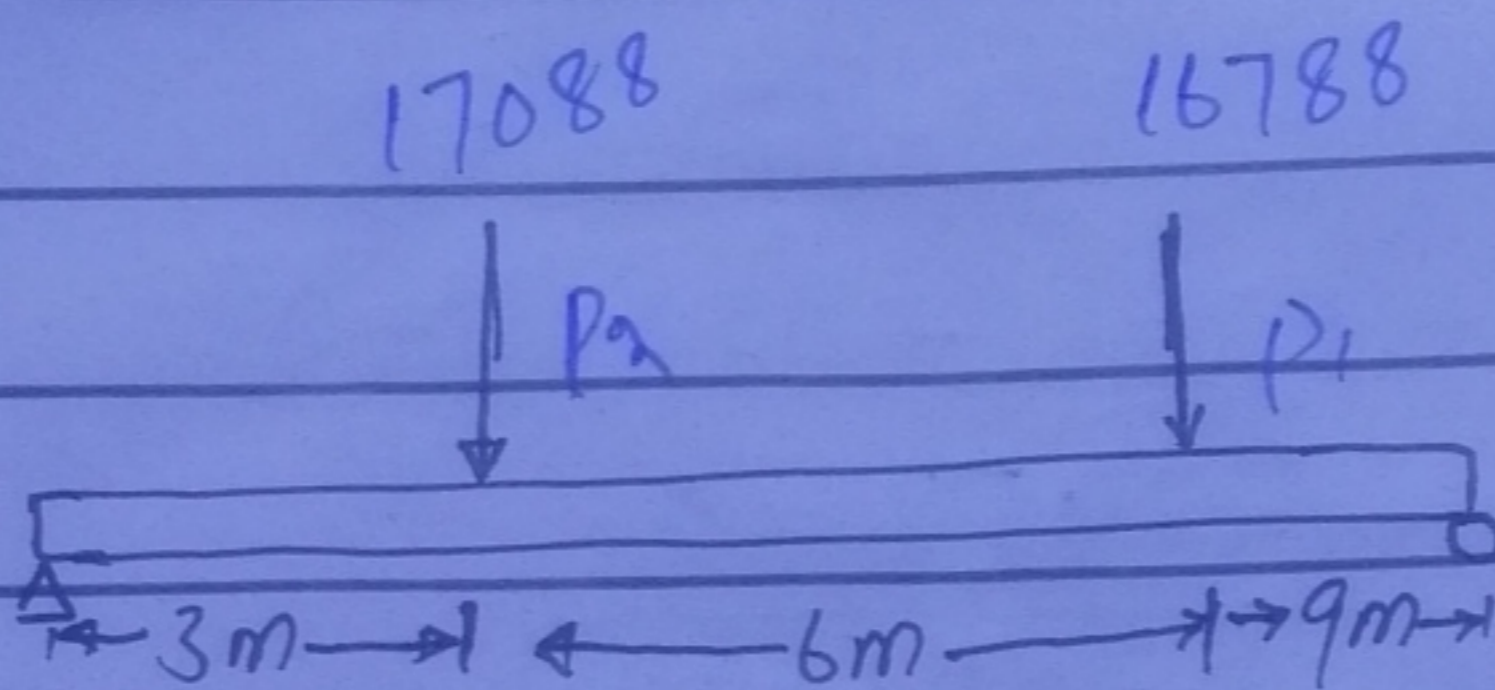
①

Day  M  T  W  T  F  SName: ~~1588~~ Ziaullah ID: 16588.

Section: B Dept: Civil Engineering.

Paper: Engineering mechanics.

Q No 4

Sol

$$P_1 = 200 + \text{Student ID}$$

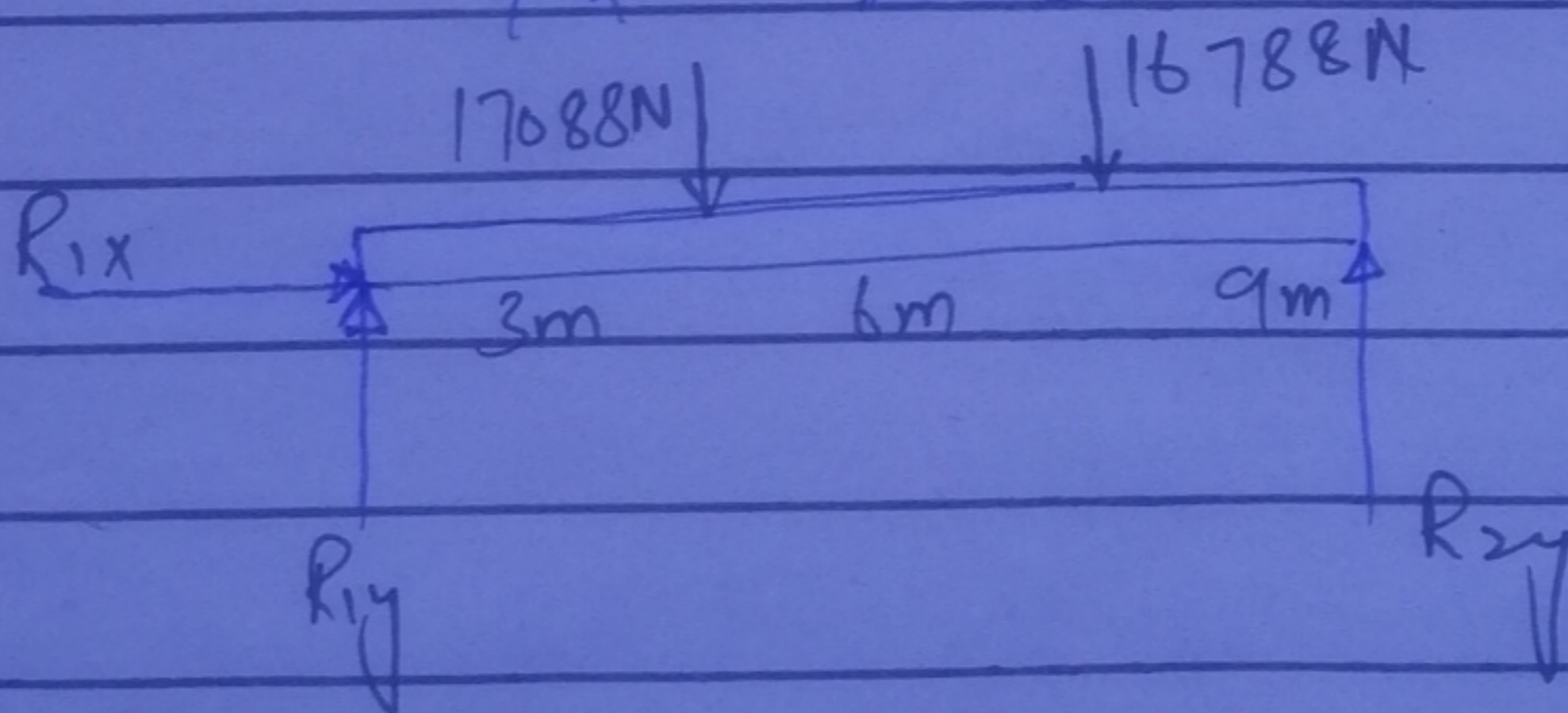
$$P_1 = 200 + 16588$$

$$P_1 = 16788 \text{ N}$$

$$P_2 = 500 + \text{Student ID}$$

$$P_2 = 500 + 16588$$

$$P_2 = 17088 \text{ N}$$



$$R_{1x} = 0$$

$$R_{1y} + R_{2y} - 16788 - 17088 = 0 \quad \text{--- (i)}$$

$$(R_{2y} \times 18) - (16788 \times 9) - (17088 \times 3) = 0$$

$$18R_{2y} - 151092 - 51264 = 0$$

$$18R_{2y} - 202356 = 0$$

$$R_{2y} = \frac{202356}{18}$$

18

$$R_{2y} = 11242 - N$$

put the value of  $R_{2y}$  in equation we get.

$$R_{1y} + R_{2y} - 16788 - 17088 = 0$$

$$R_{1y} + 11242 - 33876 = 0$$

$$R_{1y} - 22454 = 0$$

$$R_{1y} = 22454 \text{ N}$$

So

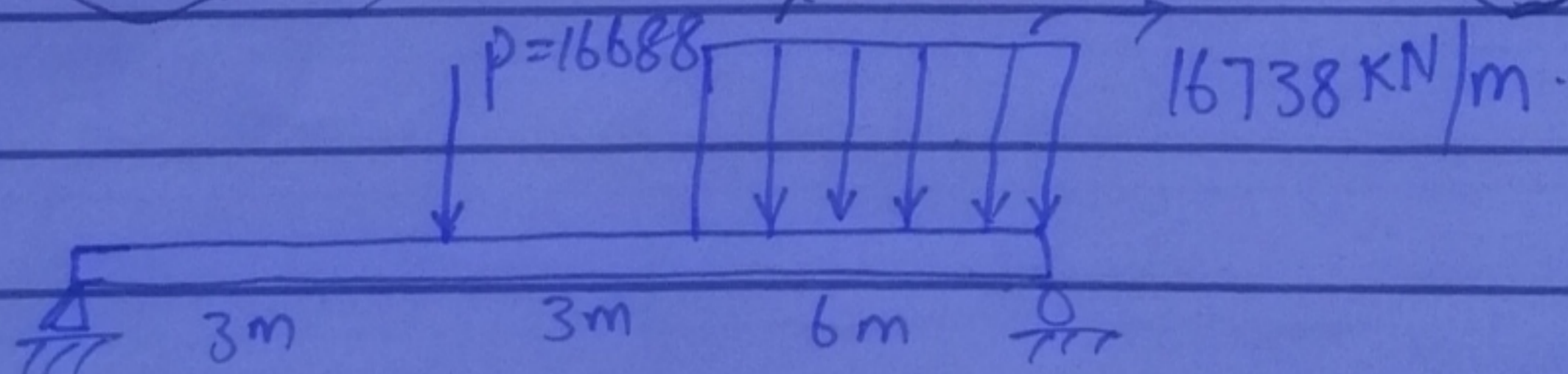
$$R_{1x} = 0 \text{ N}$$

$$R_{1y} = 22454 \text{ N}$$

$$R_{2y} = 11242 - N$$

Q No 2.

Sol.



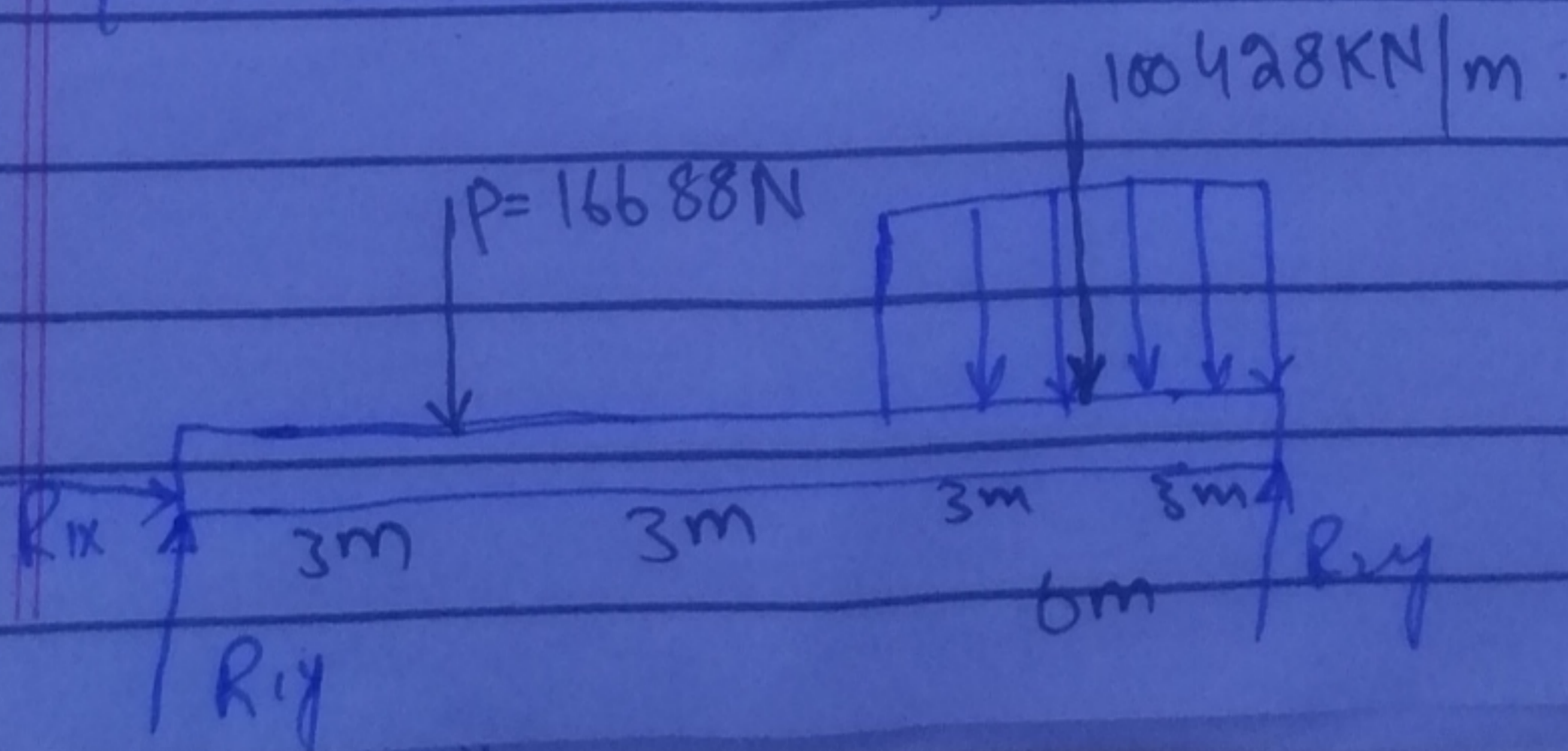
$$p = 100 + \text{Student ID}$$

$$p = 100 + 16588 = 16688 \text{ N}$$

$$\text{UDL} = 150 + \text{Student ID}$$

$$= 150 + 16588 = 16738 \text{ N}$$

$$P_1 = \text{Resultant of UDL} = 16738 \times 6 = 100428 \text{ kN/m}$$



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$$R_{1x} = 0 - N$$

$$R_{1y} + R_{2y} - 16688 - 100428 = 0 \quad \text{--- (i)}$$

$$\Sigma M = 0$$

$$(R_{2y} \times 12) - (16688 \times 3) - (100428 \times 9) = 0$$

$$12 R_{2y} - 50064 - 903852 = 0$$

$$12 R_{2y} - 953916 = 0$$

$$R_{2y} = \frac{953916}{12}$$

$$R_{2y} = 79493 - N$$

put the value of  $R_{2y}$  in equation (i) we get.

$$R_{1y} + R_{2y} - 16688 - 100428 = 0$$

$$R_{1y} + 79493 - 117116 = 0$$

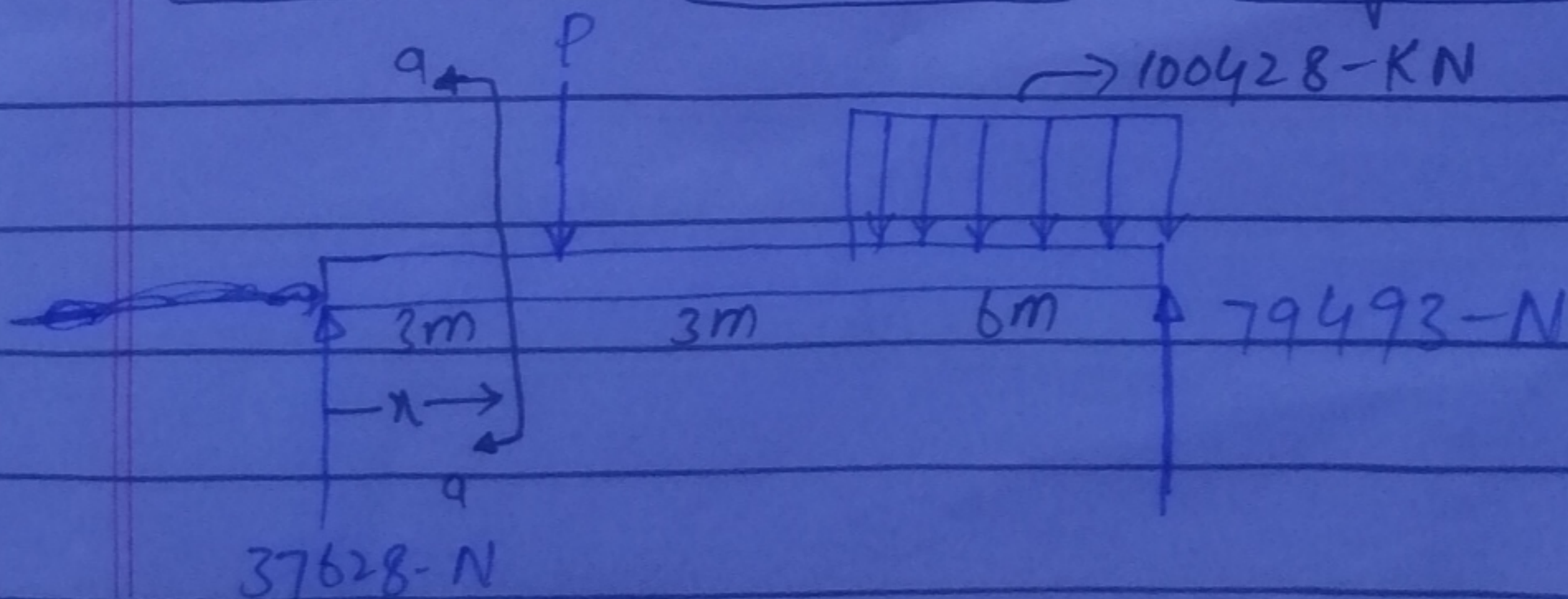
$$R_{1y} - 37623 = 0$$

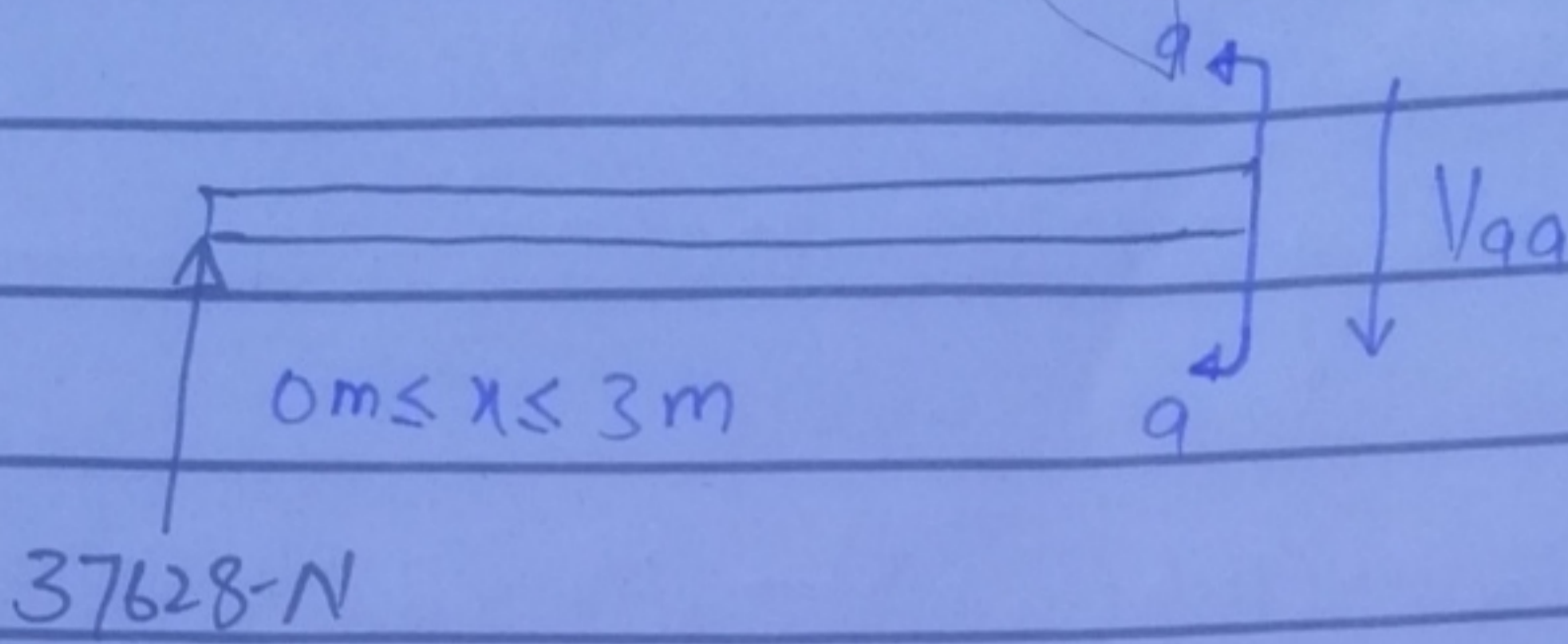
$$R_{1y} = 37623 - N$$

$$R_{1x} = 0 - N$$

$$R_{1y} = 37628 - N$$

$$R_{2y} = 79493 - N$$





$$\text{Summation } \leftarrow f \quad F_y = 0$$

$$-V_{qa} + 37628 = 0$$

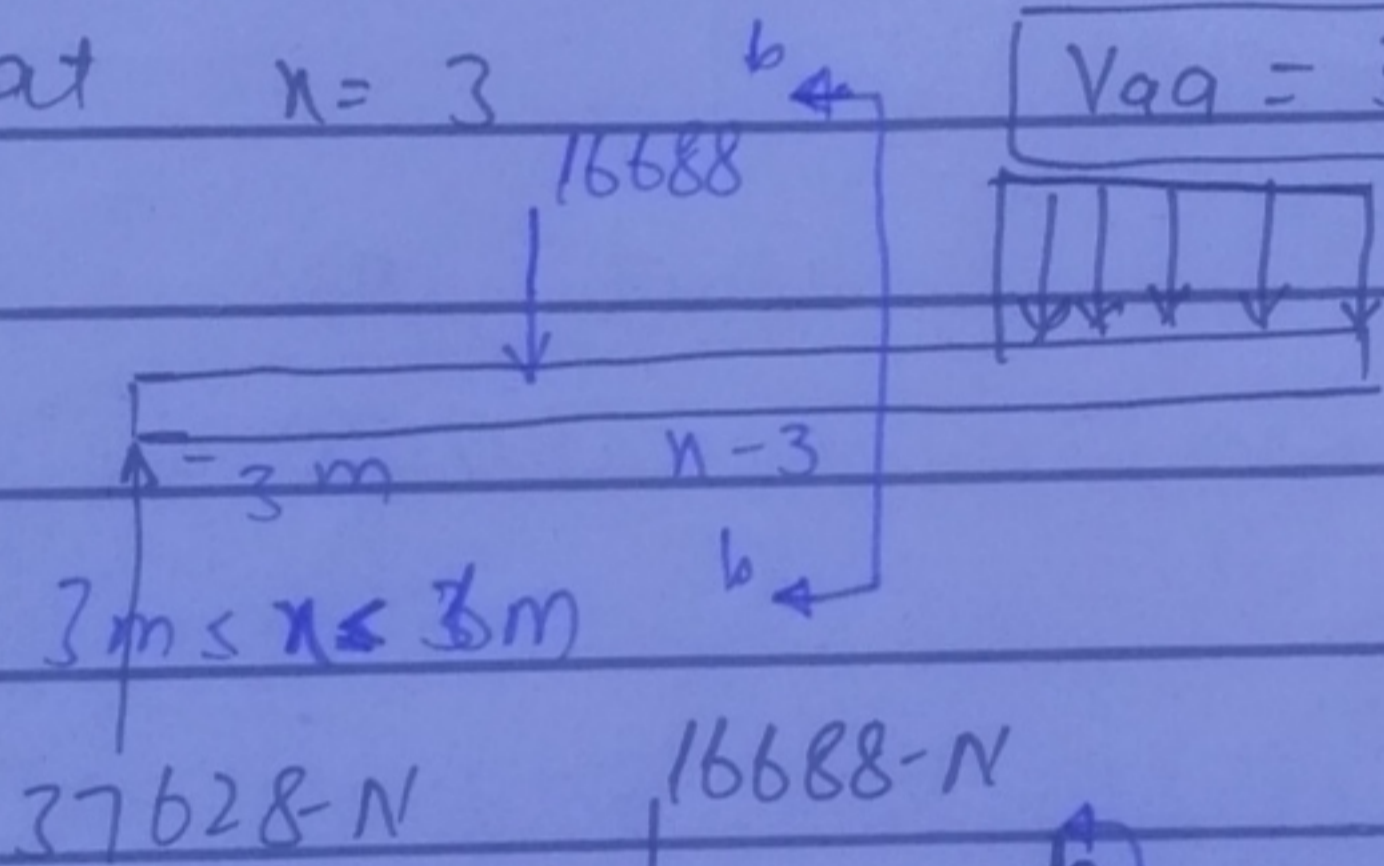
$$V_{qa} = 37628$$

at  $x=0$

$$V_{qa} = 37628-N$$

at  $x=3$

$$V_{qa} = 37628-N$$



37628-N

16688-N

$V_{bb}$

37628-N

$$-V_{bb} - P + 37628 = 0$$

$$-V_{bb} - 16688 + 37628$$

$$V_{bb} = 37628 - 16688$$

$$V_{bb} = 20940$$

at  $x=3$

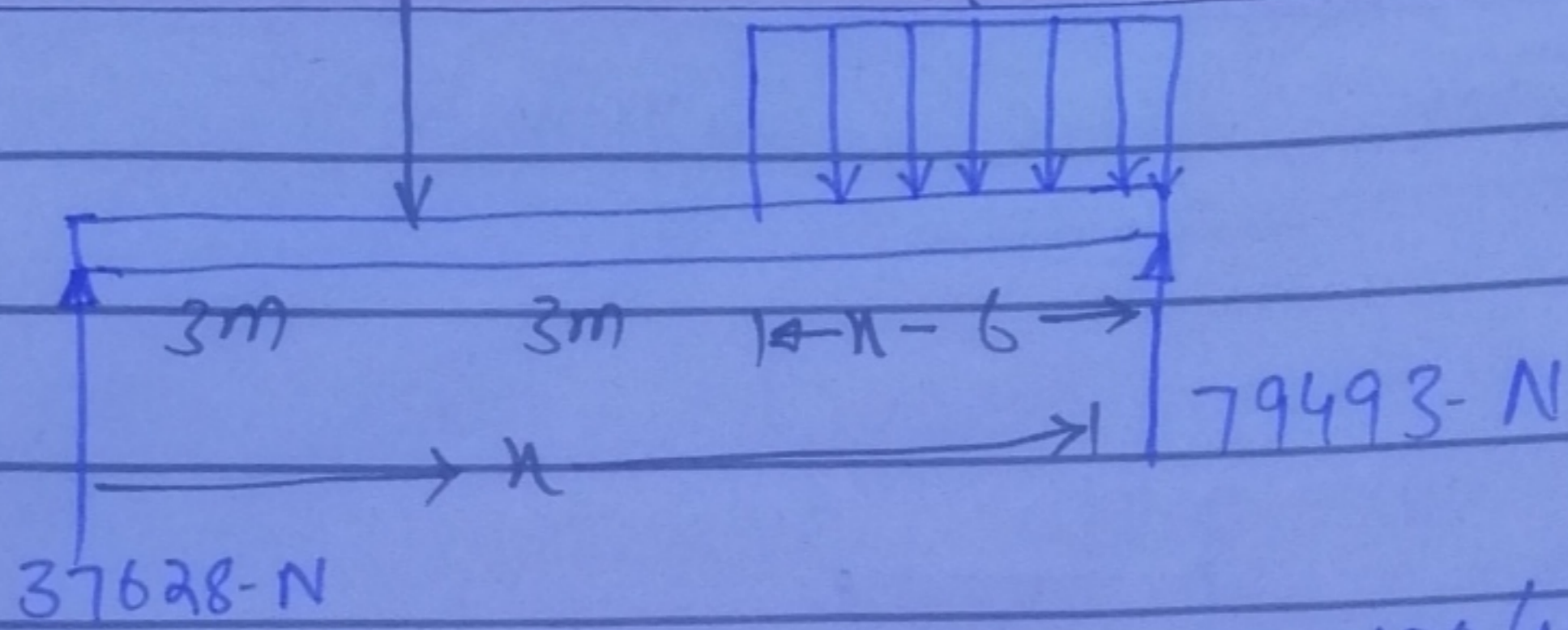
$$V_{bb} = 20940N$$

at  $x=6$

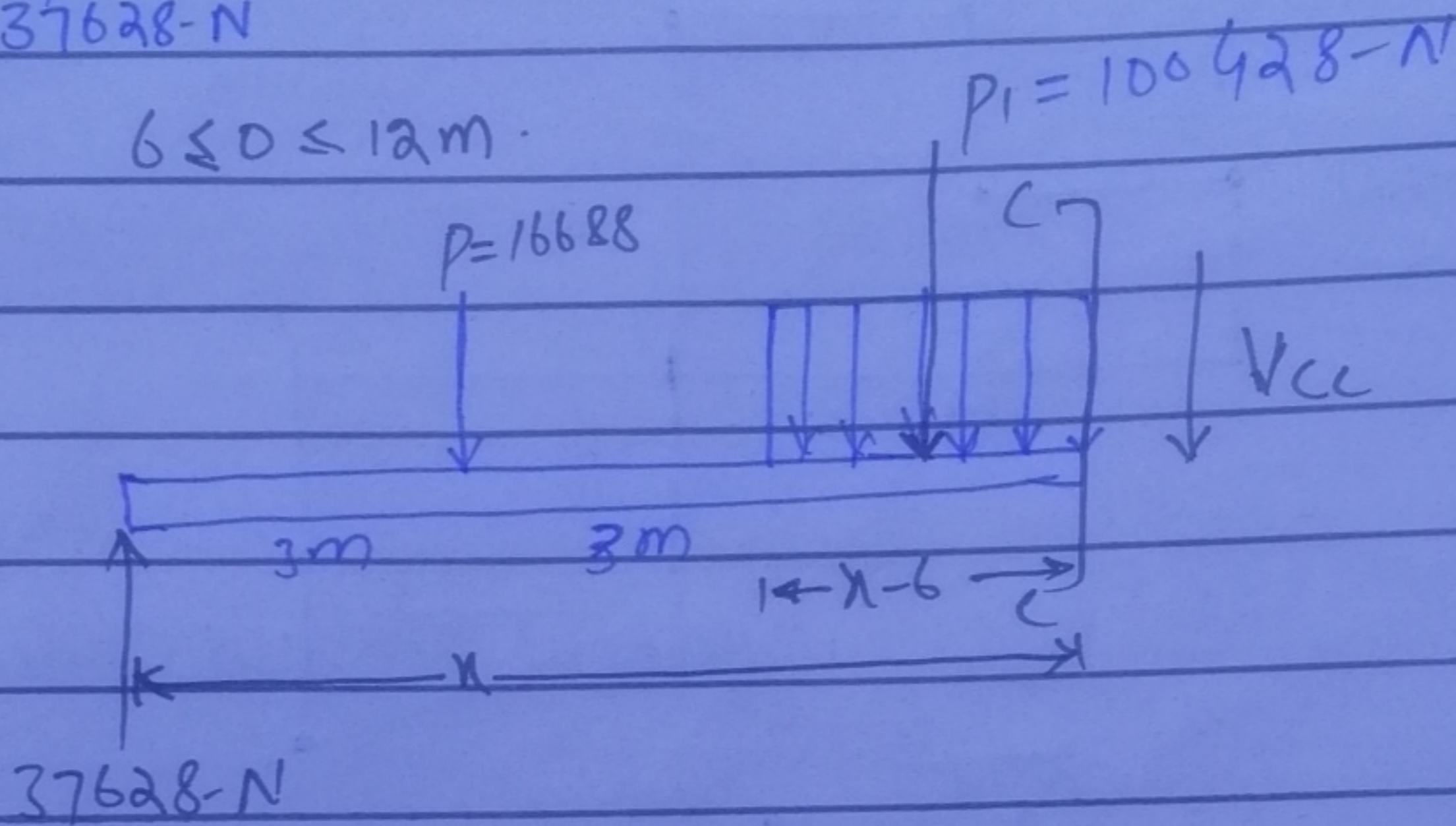
$$V_{bb} = 20940-N$$

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$$P = 16688 - N$$

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$$6 \leq x \leq 12m$$



$$P_1 = 100428 \times (x - 6)$$

$$P = 100428x - 602568$$

$$-V_{cc} - P_1 - P + 37628 = 0$$

$$-V_{cc} - 100428x - 602568 - 16688 + 37628 = 0$$

$$V_{cc} = 37628 - 16688 - 602568 - 100428x$$

$$V_{cc} = 37628 - 619256 - 100428x$$

$$V_{cc} = -100428x - 581628$$

$$\text{at } x = 6$$

$$V_{cc} = -1184196 - N$$

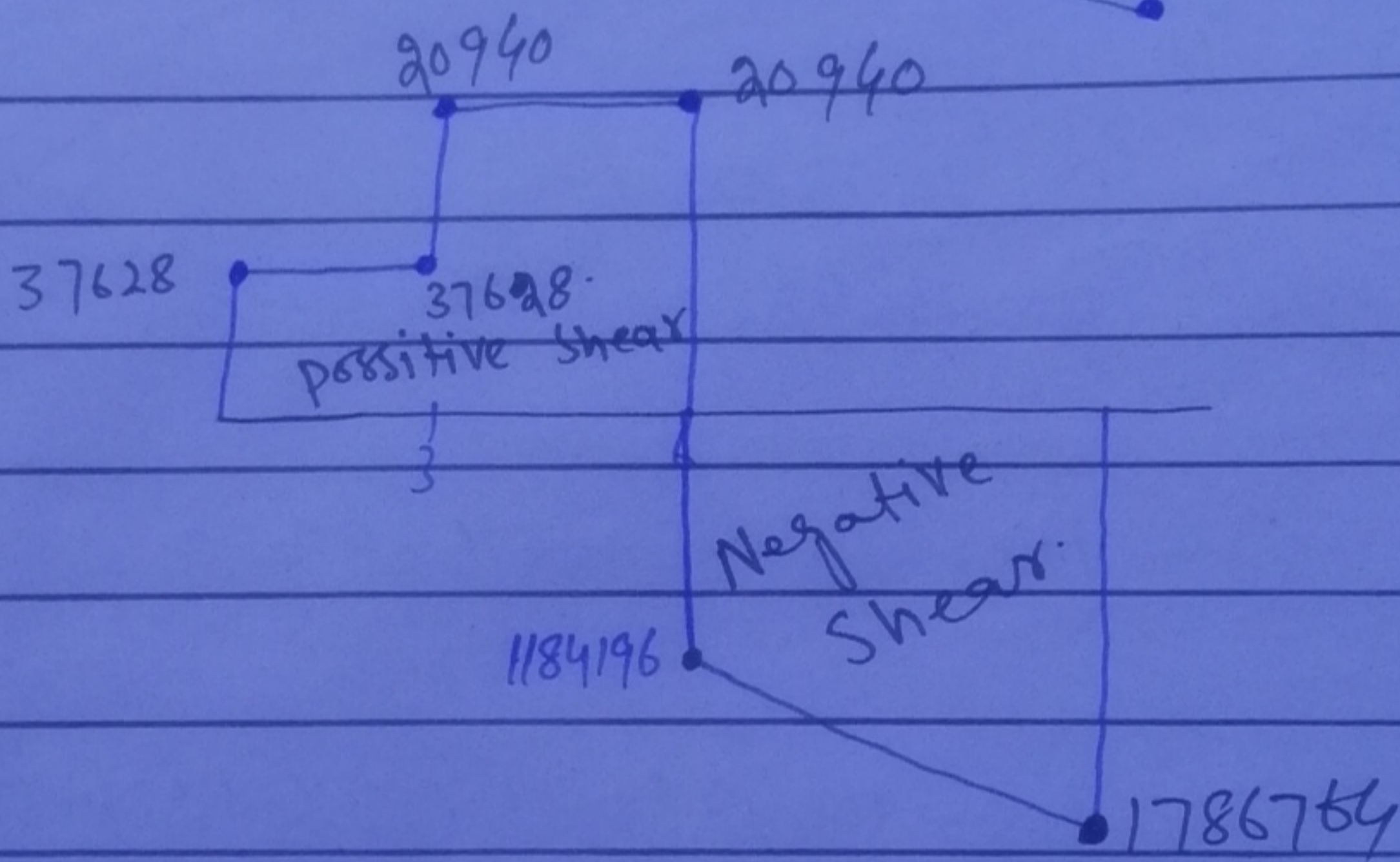
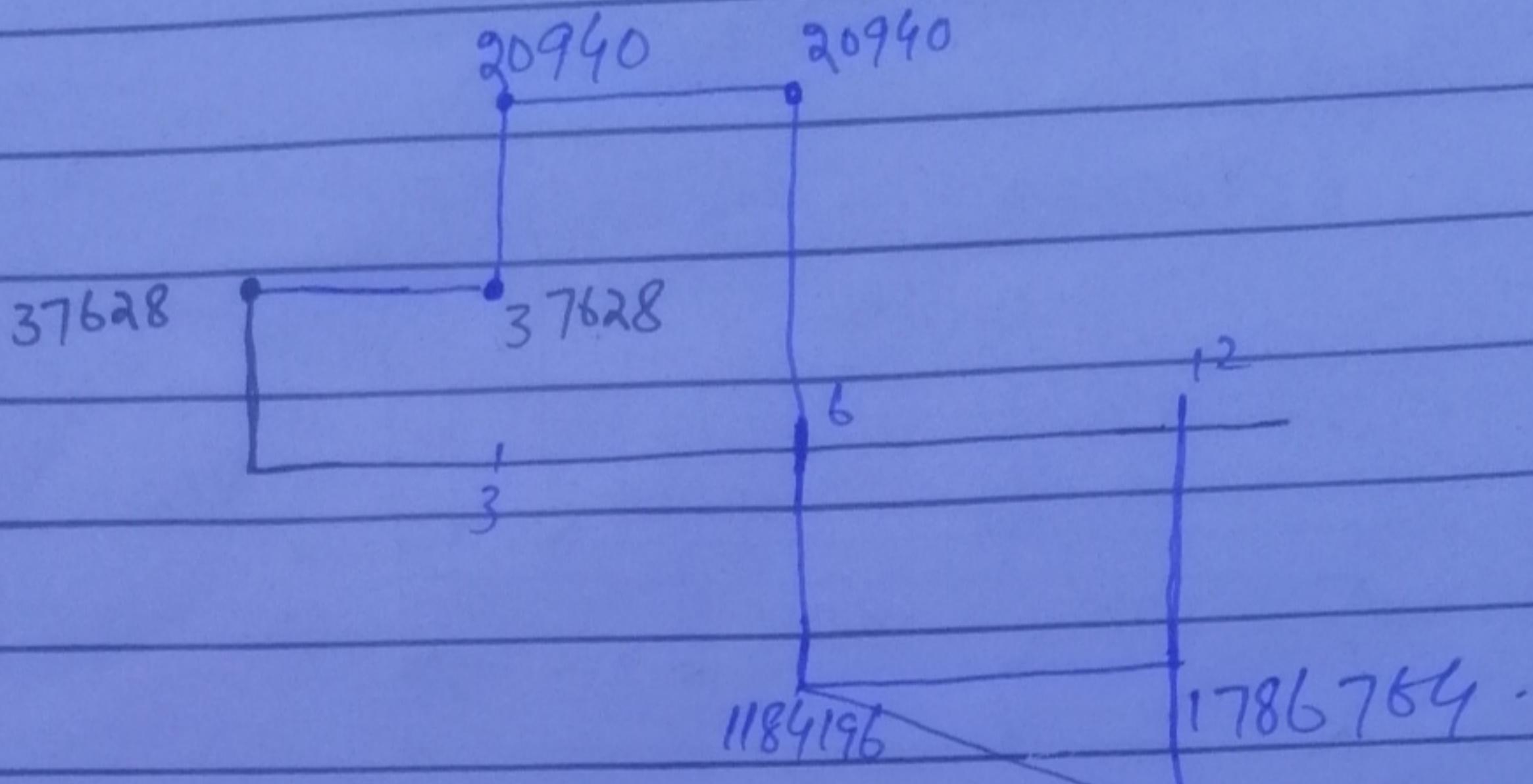
$$\text{at } x = 12$$

$$V_{cc} = -1786764 - N$$

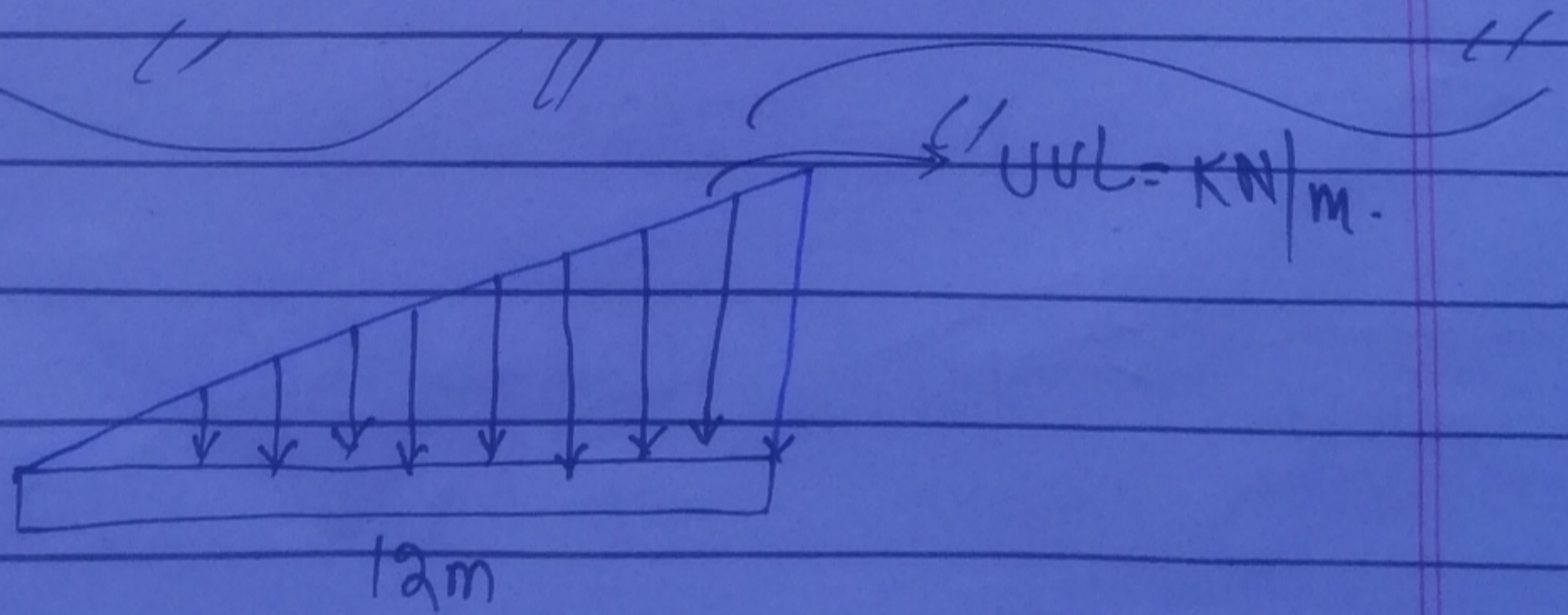
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# Shear force diagrams →



QNo3



$$UUL = \text{Student ID} / 1000$$

$$UUL = 16588 / 1000$$

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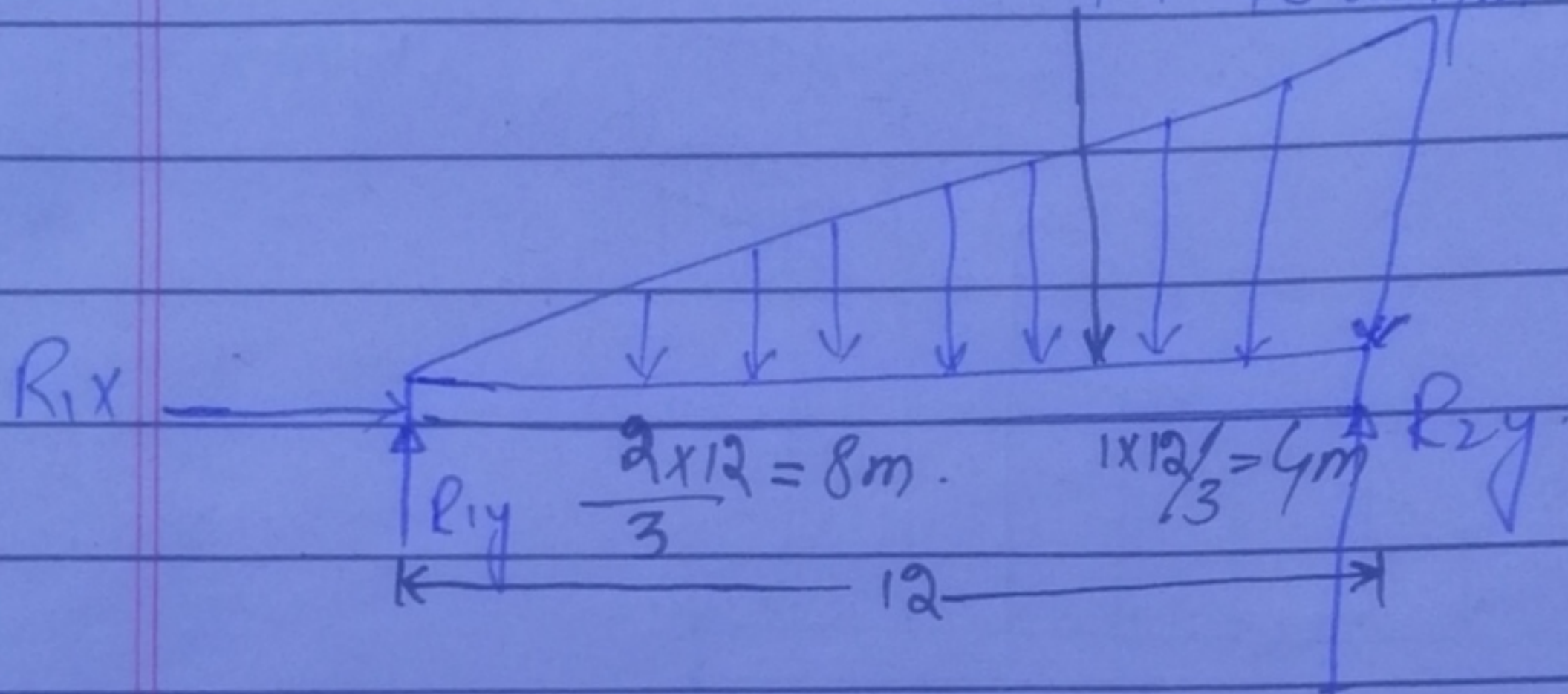
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$$UVL = 16.58 \text{ KN/m}$$

$$P = \text{Resultant of } UVL = \frac{16.58 \times 12}{2}$$

$$= 99.48 \text{ KN/m}$$



$$R_{1x} = 0$$

$$R_{1y} + R_{2y} - 99.48 = 0 \quad \text{--- (i)}$$

$$\sum M = 0$$

$$(R_{2y} \times 12) - (99.48 \times 8) = 0$$

$$12 R_{2y} = 795.84$$

$$R_{2y} = \frac{795.84}{12}$$

$$\boxed{R_{2y} = 66.32 \text{ N}}$$
 put the value of

$R_{2y}$  in eq (i) we get.

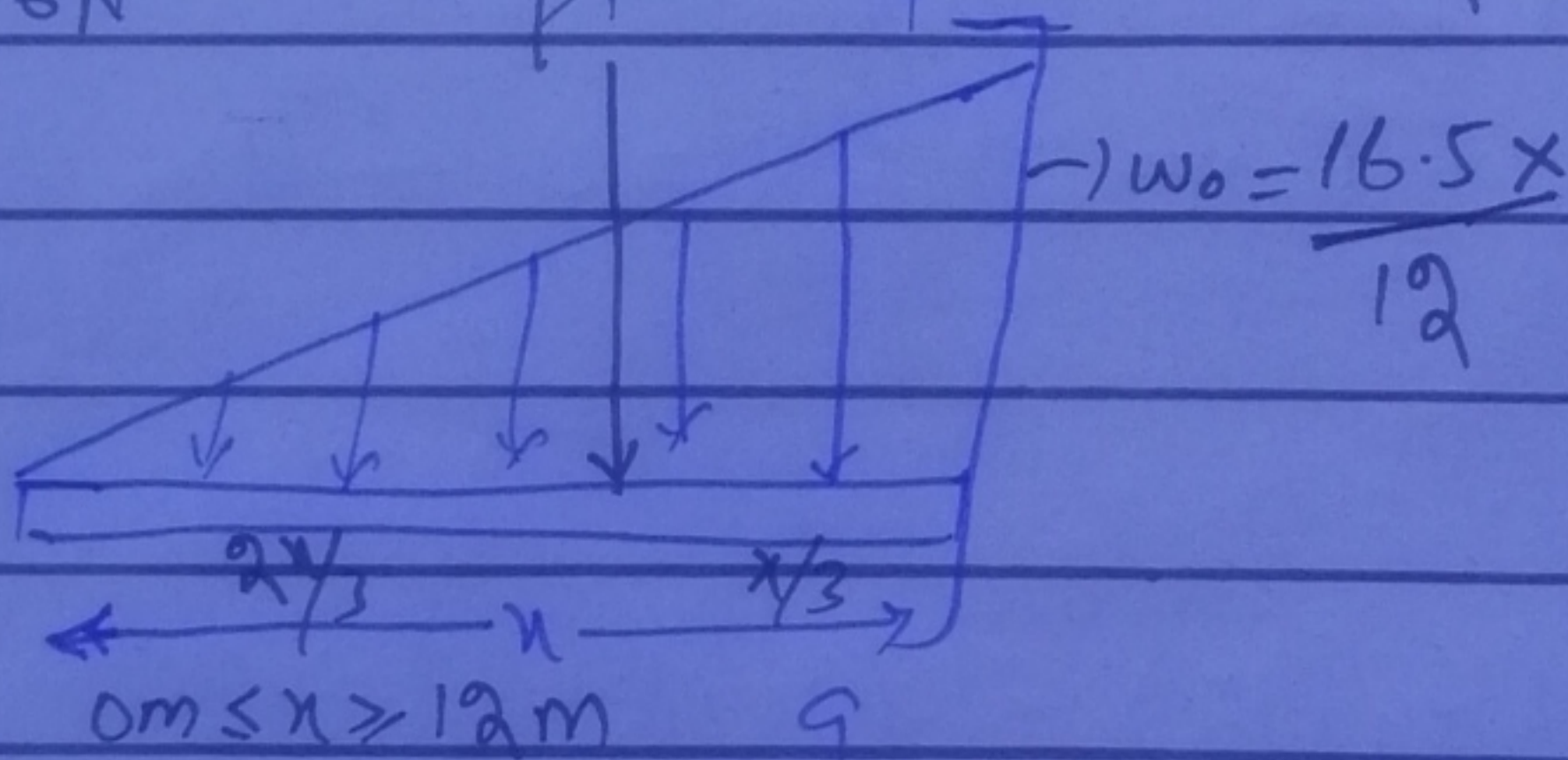
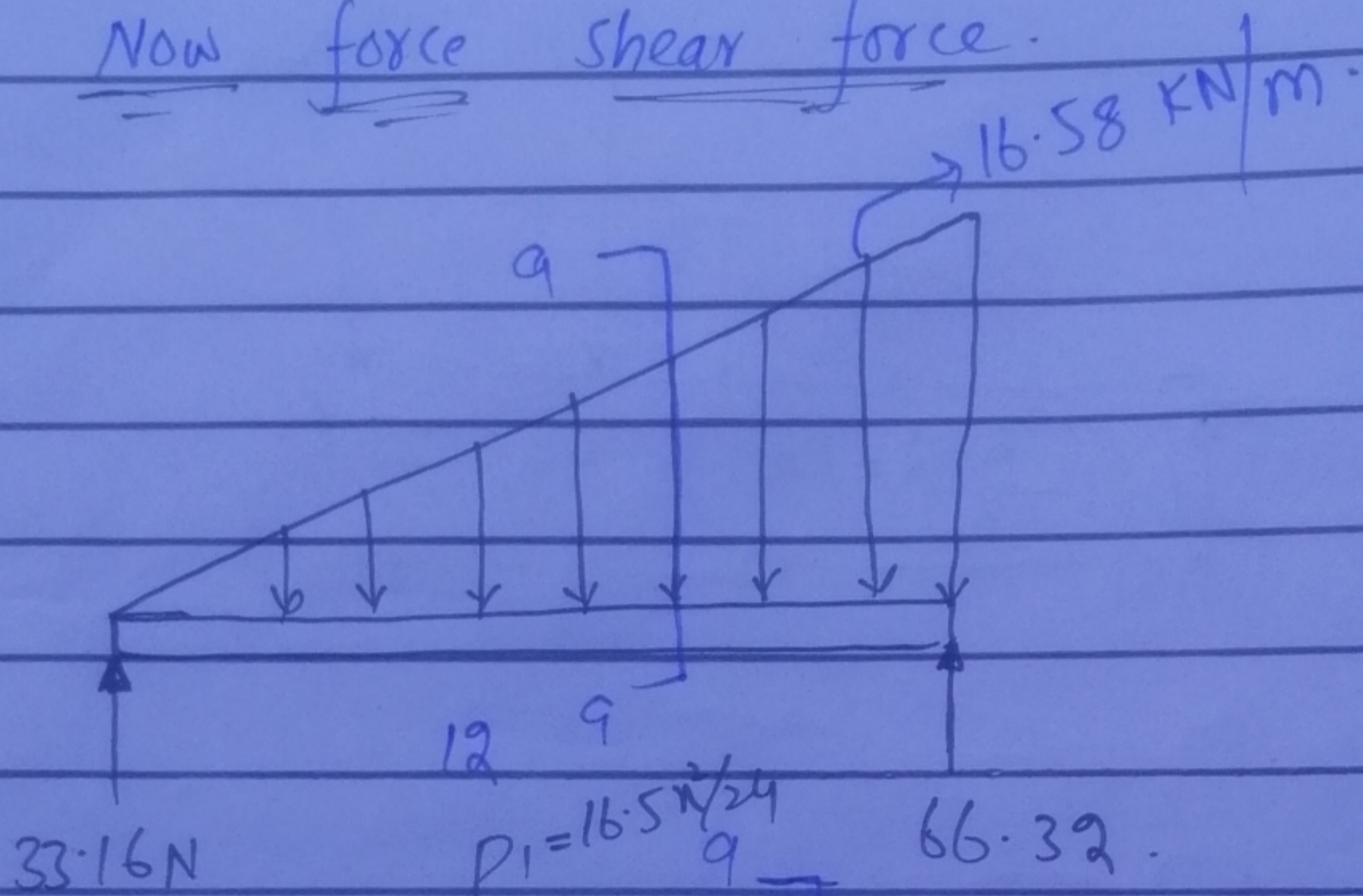
$$R_{1y} + R_{2y} - 99.48 = 0$$

$$R_{1y} + 66.32 - 99.48 = 0$$

$$R_{iy} - 33.16 = 0$$

$$R_{iy} = 33.16 \text{ N}$$

Now force shear force.



From Similar triangle.

$$\frac{w_0 \text{ KN/m}}{x - m} = \frac{16.58 \text{ KN/m}}{12}$$

$$w_0 \text{ KN/m} = \left[ \frac{16.5x}{12} \right] \text{ KN/m}$$

$$P_1 = w_0 \times \frac{x}{2}$$

$$P_1 = \left[ \frac{16.5x \times x}{12} \right] \div 2$$



$$p_1 = \frac{16.5x^2}{24} - \text{KN}$$

$$\text{Sumation } F_y = 0$$

$$-V_{aq} - p + 33.16 = 0$$

$$-V_{aq} - \frac{16.5x^2}{24} + 33.16 = 0$$

$$V_{aq} = \frac{-16.5x^2 + 33.16}{24}$$

$$\text{at } x=0 \quad V_{aq} = 33.16 - N$$

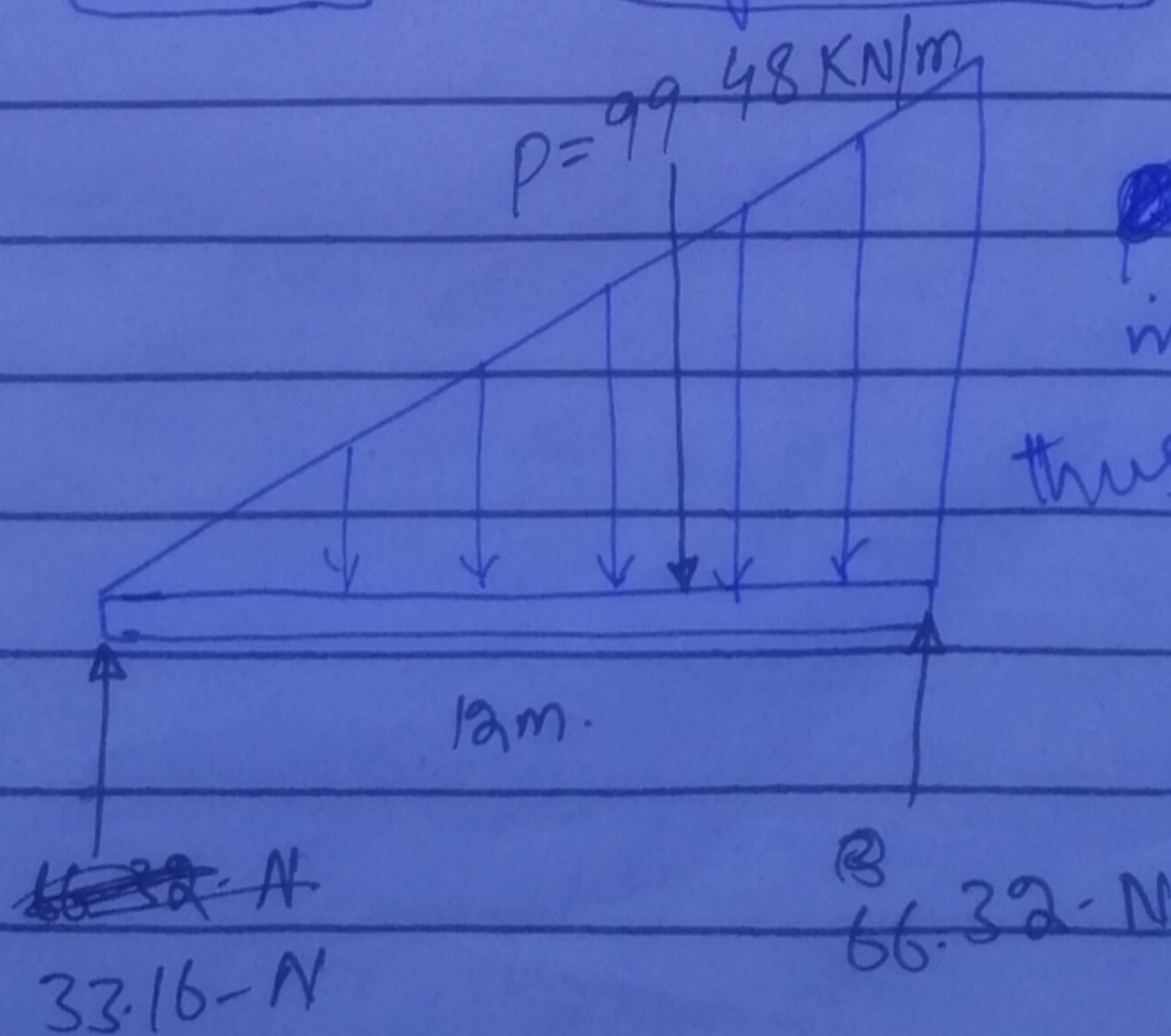
$$\text{at } x=12 \quad V_{aq} = -65.84 - N$$

Now for Bending moment  $\rightarrow$

$$R_{ix} = 0$$

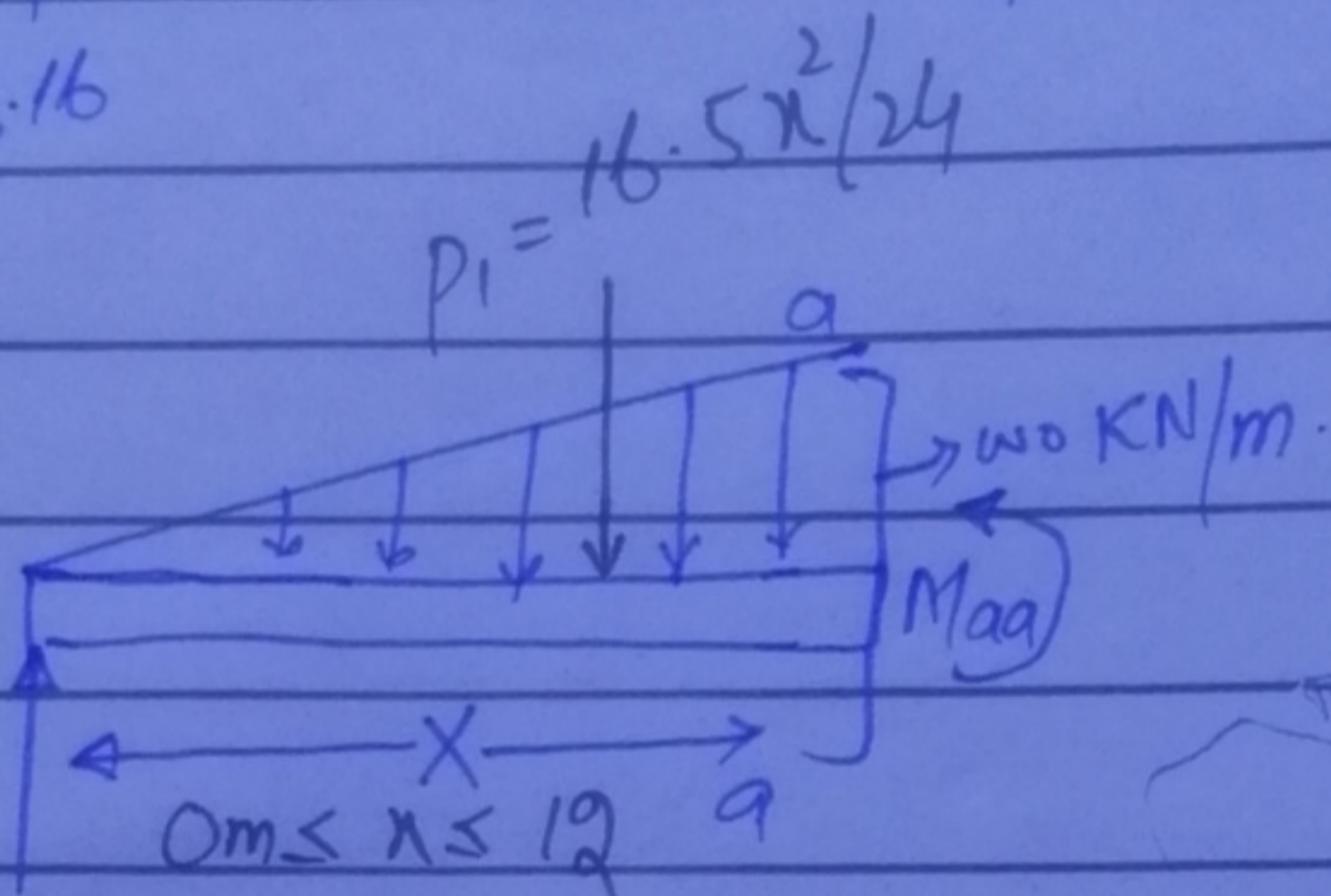
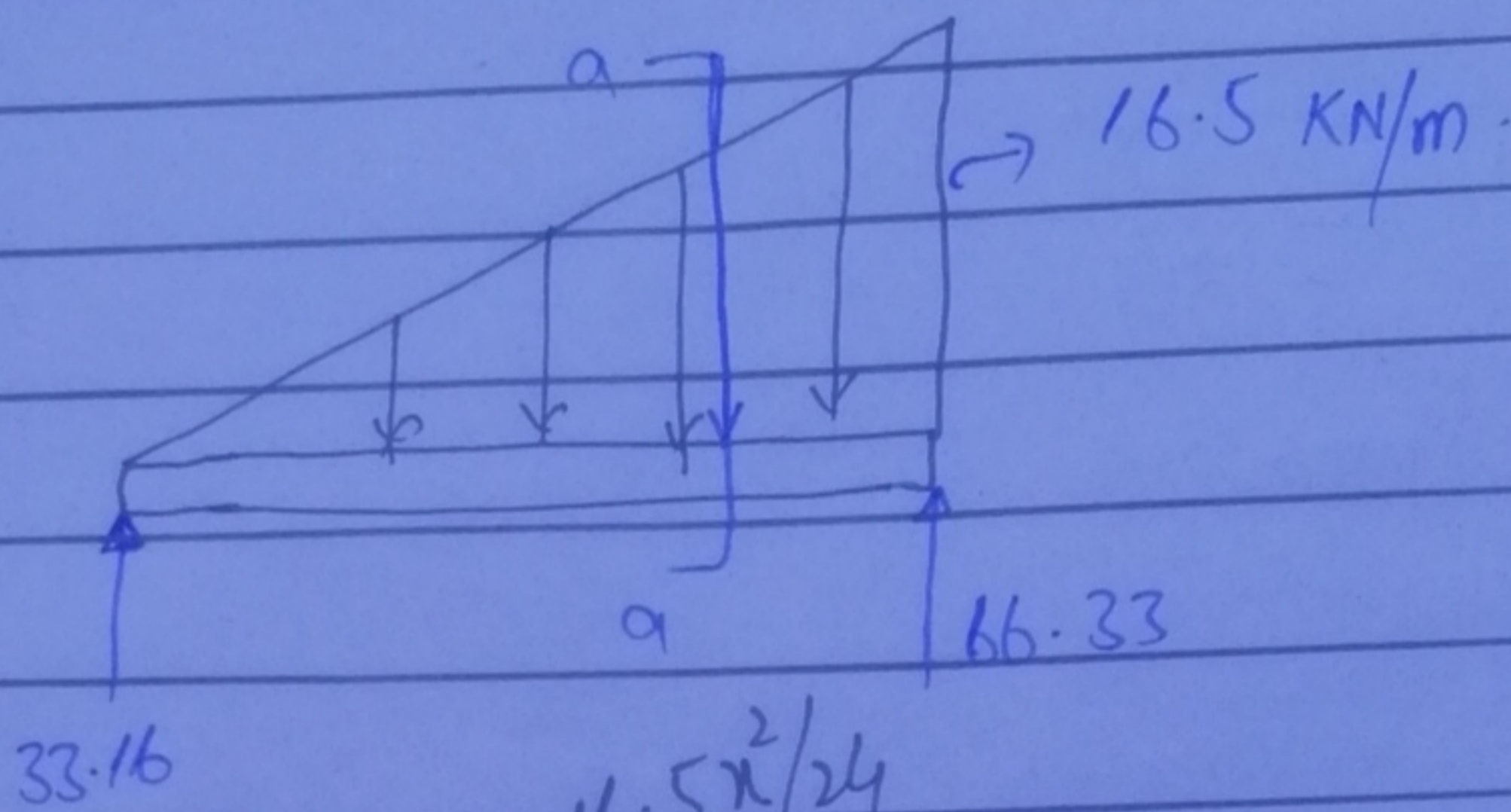
$$R_{ay} = 66.32 - N$$

$$R_{iy} = 33.16 - N$$



we find  $p$   
in shear force  
thus  $p = 99.48 \text{ kN/m}$ .

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33.16 N

From similar triangle.

$$\frac{w_0 \text{ KN/m}}{x \text{ m}} = \frac{16.58 \text{ KN/m}}{12}$$

$$w_0 \text{ KN/m} = \frac{16.58x \text{ KN/m}}{12}$$

$$P_1 = \frac{w_0 \cdot x}{2}$$

$$P_1 = \frac{16.58x \cdot x}{12 \times 2}$$

$$P_1 = \frac{16.58x^2 \cdot \text{KN/m}}{24}$$

$$\text{Sumation } M = 0$$

$$M_{aa} - P_1 \left( \frac{x}{3} \right) - 33.16x = 0$$

$$M_{aa} + \left( \frac{16.58x^2}{24} \times \frac{x}{3} \right) - 33.16x = 0$$

$$M_{aa} + \frac{16.58x^3}{72} - 33.16x = 0$$

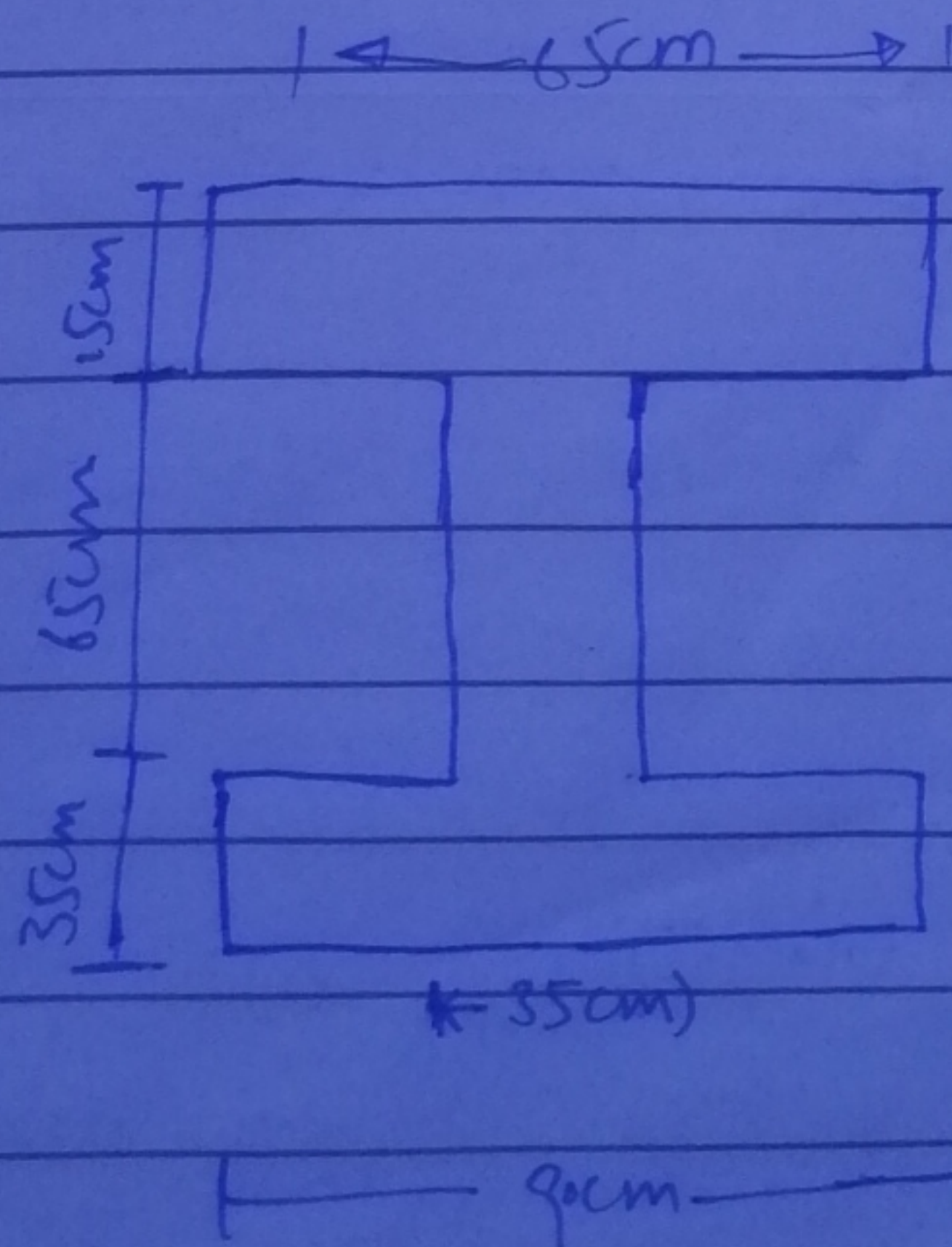
$$M_{aa} = 33.16x - \frac{16.58x^3}{72}$$

$$\boxed{\text{at } x = 0 \quad M_{aa} = 0 \text{ - KNm}}$$

$$\boxed{\text{at } x = 12 \quad M_{aa} = 0 \text{ - KN-m}}$$

QNo 4 (a)

Sol



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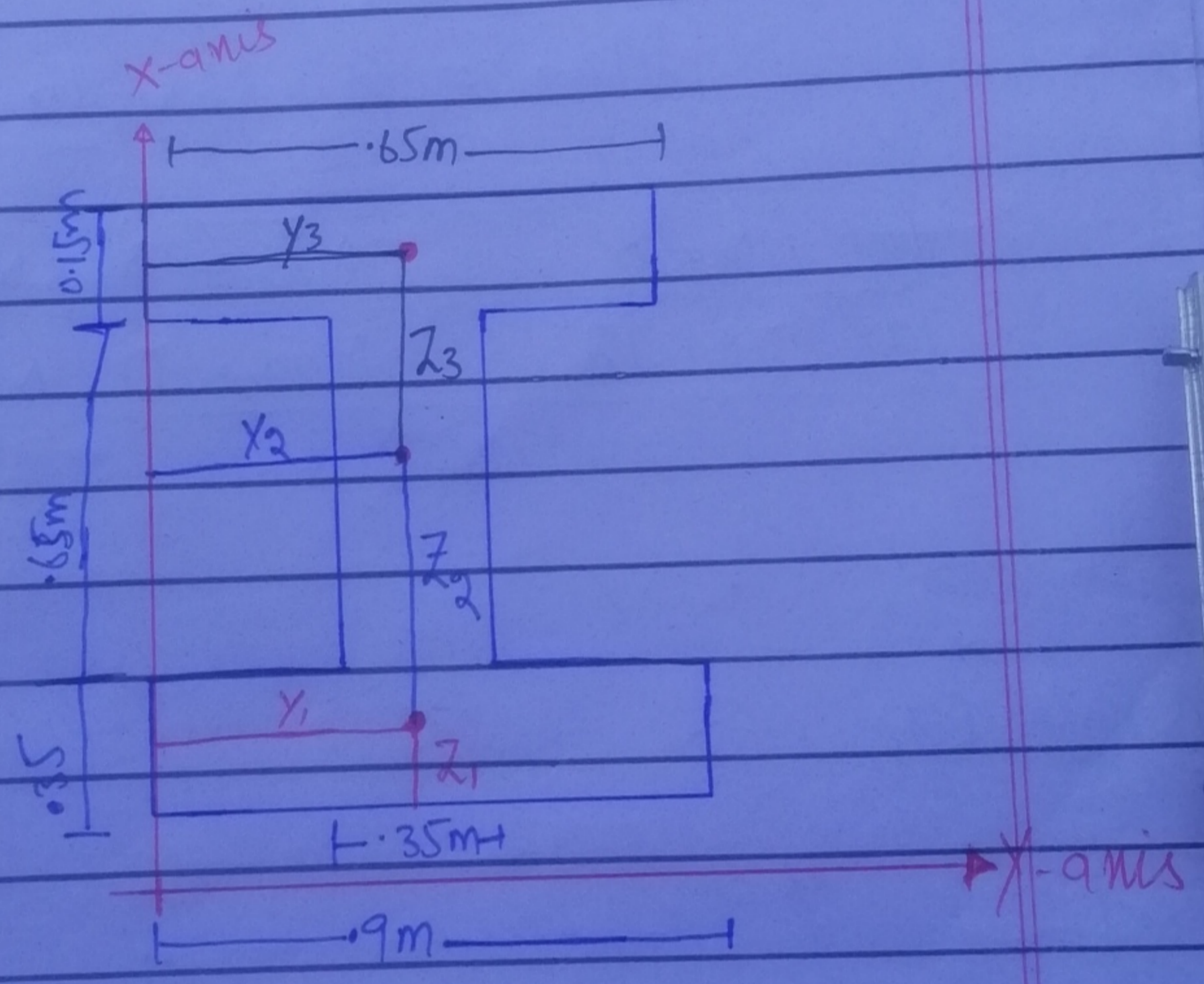
Change cm into meter.

90cm = .9m

35cm = .35m

65cm = .65m

15cm = 0.15m.



$A_1 = (0.9m) \times (0.35m) = 0.315m^2$

$A_2 = (0.65m) \times (0.35m) = 0.2275m^2$

$A_3 = (0.65m) \times (0.15m) = 0.0975m^2$

$x_1 = 0.9/2 = 0.45m$

$z_1 = 0.35/2 = 0.175m$

$x_2 = 0.9/2 = 0.45m$

$z_2 = 0.35 + \frac{0.65}{2} = 0.675m$

~~scribble~~

$x_3 = 0.65/2 = 0.325m, z_3 = 0.35 + 0.65 + \frac{0.15}{2} = 1m$

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$$y_1 = 0.45\text{m}, \quad y_2 = 0.45\text{m}, \quad y_3 = 0.325\text{m}$$

$$z_1 = 0.175\text{m}, \quad z_2 = 0.675\text{m}, \quad z_3 = 1\text{m}$$

$$y_c = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3}$$

$$= \frac{(0.315)(0.45) + (0.22)(0.45) + (0.097)(0.325)}{0.315 + 0.22 + 0.097}$$

$$= \frac{0.141 + 0.099 + 0.0315}{0.632}$$

$$= \frac{0.2715}{0.632}$$

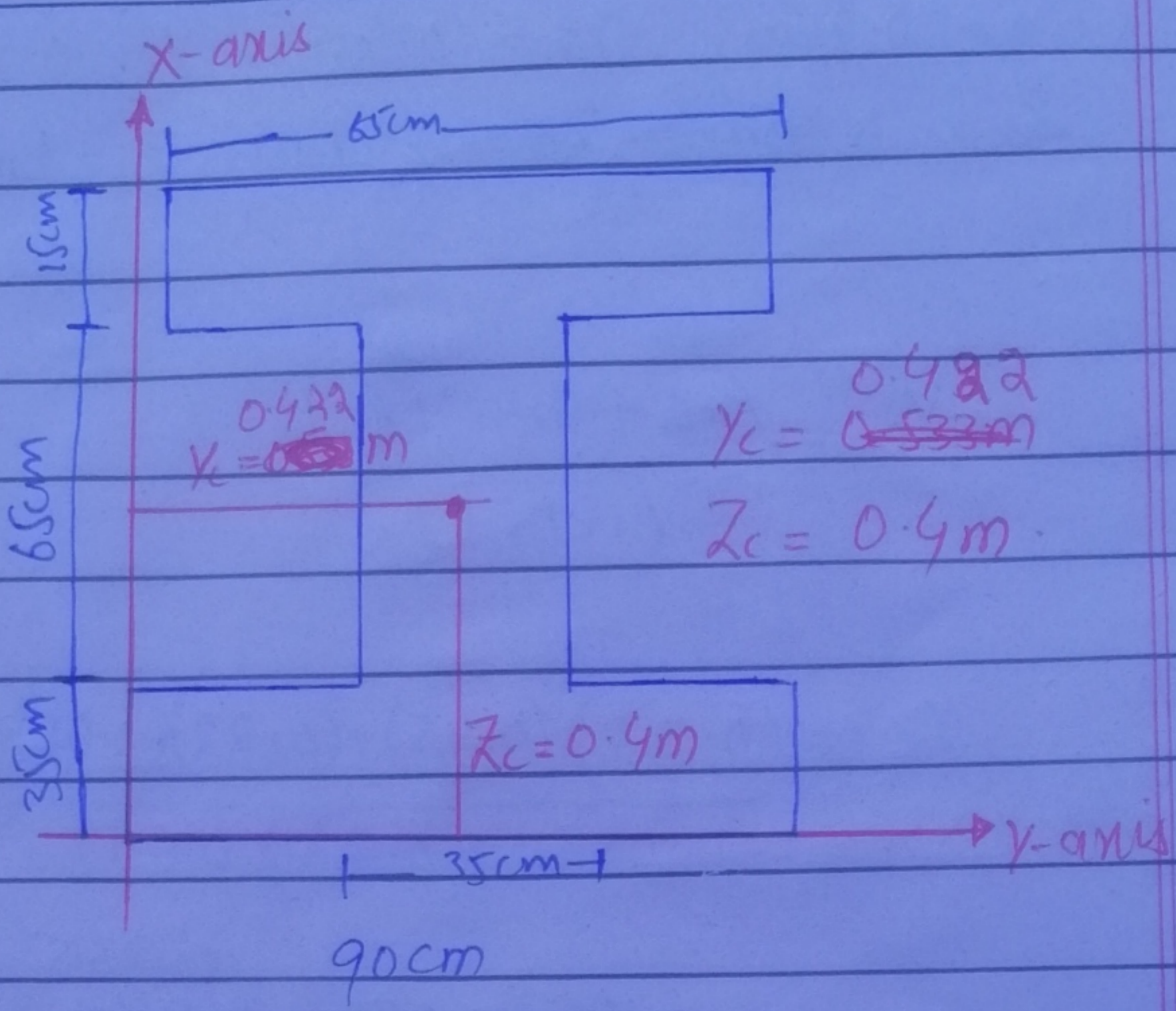
$$y_c = 0.429\text{m}$$

$$z_c = \frac{A_1 z_1 + A_2 z_2 + A_3 z_3}{A_1 + A_2 + A_3}$$

$$= \frac{(0.315)(0.175) + (0.22)(0.675) + (0.097)(1)}{0.315 + 0.22 + 0.097}$$

$$= \frac{0.055 + 0.148 + 0.097}{0.632} = \frac{0.3}{0.632}$$

$$z_c = 0.4\text{m}$$



" " " " "

Q No 5

Ans      WORK: →

WORK is said to be done to be done when a body or object moves with application of external force.

We can define work as an activity involving a movement & force in the direction of the force.

For Example, a force of 30 newtons pushing an object 3 meter in the same direction of the force will

will do 90 joules (J) of work.

$$W = F \cdot d$$

$$W = Fd \cos \alpha$$

there are several good examples of work in real life that can be observed in everyday life. A horse pulling a plow through the fields, a father pushing a grocery cart down the aisle of a grocery store.

A freshman lifting a backpack full of books upon her shoulder, a weightlifter lifting a barbell above his head, etc.

Energy →

~~Energy~~ Energy is the ability to do work. energy can neither be created nor destroyed. it can only be transformed from one object to another.

Examples →

An object possessing mechanical energy has both kinetic & potential energies.

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Although the energy of one of the forms may be equal to zero.

A moving car has kinetic energy. If you move the car up a mountain, it has kinetic & potential energy.

A ~~book~~ book sitting on a table has potential energy.

power →

power can be defined as the work done per unit time. power is a physical concept that has several different meanings, depending on the context & the information that is available. we can define power is the rate of doing work. it is the amount of energy consumed per unit time.

$$P = \frac{W}{t}$$

The unit of power is joule per second.

Example of power → A garage hoist lifts a truck



truck up 2 meters above the ground in 15 second. Find the power delivered to the truck?

Sol

$$F = mg = 1000 \times 9.81 = 9810 \text{ N}$$

$$W = F \cdot d = 9810 \text{ N} \times 2 \text{ m} = 19620 \text{ Nm}$$

$$W = 19620 \text{ J}$$

$$P = W/t = 19620 \text{ J} / 15 \text{ s}$$

$$P = 1308 \text{ J/s}$$

|| || || || ||

Q No 4 (b)

Given data

Sol

$$\text{Area} = 65 \text{ cm} \times 35 \text{ cm}$$

Required = ?

moment of Inertia = ?

Radius of Gyration = ?

Section of moduli = ?

For moment of Gyration:  $\rightarrow$

$$I_x = \frac{1}{3} bh^3$$

$$= \frac{1}{3} (65)(35)^3$$

$$I_x = 928958 \text{ mm}^4$$

$$I_y = \frac{1}{3} b^3 h = \frac{1}{3} (65)^3 (35)$$

$$I_y = 3203958 \text{ mm}^4$$

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$$\bar{I}_{x'} = \frac{1}{12} bh^3$$

$$\bar{I}_{x'} = \frac{1}{12} (65)(35)^3$$

$$\boxed{\bar{I}_{x'} = 232239.5 \text{ mm}^4}$$

$$\bar{I}_{y'} = \frac{1}{12} b^3 h$$

$$\bar{I}_{y'} = \frac{1}{12} (65)^3 (35)$$

$$\boxed{\bar{I}_{y'} = 800989.5 \text{ mm}^4}$$

$$\bar{I}_z = \frac{1}{12} bh (b^2 + h^2)$$

$$= \frac{1}{12} (65)(35) \left( (65)^2 + (35)^2 \right)$$

$$= \frac{1}{12} (65)(35)(5450)$$

$$\boxed{\bar{I}_z = 1033229 \text{ mm}^4}$$

Radius of gyration →

$$r_y = \sqrt{\frac{\bar{I}_{x'}}{A}}$$

$$A = b \times d$$

$$r_y = \sqrt{\frac{392395.8}{2275}}$$

$$= 2275$$

$$r_y = \sqrt{1408.3}$$

$$\boxed{r_y = 37.52 \text{ mm}}$$

$$y_z = \left( \frac{I_z}{A} \right)^{1/2}$$

$$= \left( \frac{1033229.16}{2275} \right)^{1/2}$$

$$y_z = \sqrt{454}$$

$$y_z = 21.3 \text{ mm}$$

Section moduli : →

$$S = \frac{Lbh^2}{6}$$

$$S = \frac{(65)(35)^2}{6}$$

$$S = \frac{79625}{6}$$

$$S = 13270 \text{ mm}^2$$

the end -