



## **IQRA NATIONAL UNIVERSITY PESHAWAR**

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<b>Program</b>	<b>MS Transportation Engineering</b>
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**IQRA NATIONAL UNIVERSITY**  
**PESHAWAR**

Q No 02

Given Data:

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ID = 14374

$$F = 14 \text{ N}$$

$$\text{Elastic Limit} = 207000 \text{ KPa}$$

$$E = 223 \times 10^6 \text{ KPa}$$

$$n = 0$$

$$F.O.S \quad N = 1$$

$$X = 14 + 5 = 19 \text{ cm}$$

$$Y = 14$$

Required data Determine diameter of shaft = ?

Sol The moment at section A is

$$M = 11000 \times 14 = 154000$$

and The Torque on the shaft is  $J = 11000 \times 0.14 = 1540$   
The normal stress due to M at A is

$$S = \frac{64Md}{\pi d^4} = \frac{32M}{\pi d^3}$$

Maximum shear stress due to T at A is

$$T = \frac{32Td}{\pi d^4} = \frac{16T}{\pi d^3}$$

The shear stress due to shear force is zero at A

$$S_{ns} = \frac{1}{2} S \pm \frac{1}{2} (S^2 + T^2)^{1/2}$$

Maximum shear stress theory

$$T_{max} = \frac{1}{2} (S_1 - S_2)$$
$$T_{max} = \frac{1}{2} \left( \frac{32M}{\pi d^3} \right) (N^2 + T^2)^{1/2}$$

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$$\begin{aligned} &= \frac{16}{\pi d^3} (M^2 + T^2)^{1/2} \\ &= \frac{16}{\pi d^3} (154000^2 + 15400^2)^{1/2} \\ &= \frac{2464123.197}{\pi d^3} \end{aligned}$$

$$\tau_{\text{Time}} = \frac{784752.61 \text{ Pa}}{d^3}$$

This should not exceed the maximum shear stress volume at yielding in uniaxial shear stress volume at yielding in uniaxial tension test.

$$\frac{1}{d^3} 784752.61 = \frac{\sigma_y}{2} \Rightarrow \frac{1}{d^3} 784752.61 = \frac{207 \times 10^6}{2}$$

$$\Rightarrow 103.5 \times 10^6$$

$$d^3 = 7582.15 \times 10^6$$

$$d = 19.64 \times 10^{-6} \text{ m}^3$$

$$d = 19.64 \text{ cm}^3$$

⑩ Octa shear stress theory

$$\tau = \frac{1}{3} \left[ (\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2 \right]^{1/2}$$

with  $\sigma_2 = 0$

$$\tau = \frac{1}{3} \left[ 2\sigma_1^2 + 2\sigma_3^2 - 2\sigma_1\sigma_3 \right]^{1/2}$$

$$\tau = \frac{\sqrt{2}}{3} (\sigma^2 + 3\tau^2)^{1/2}$$

$$\begin{aligned}
 &= \frac{19\sqrt{2}}{3\pi d^3} (4M^2 + 3T^2)^{3/2} \\
 &= \frac{19\sqrt{2}}{3\pi d^3} [4(154000)^2 + 3(1540)^2]^{3/2} \\
 &= \frac{19\sqrt{2}}{3\pi d^3} [4(154000)^2 + 3(1540)^2]^{3/2} \\
 &= (9.4864 \times 10^6 + 7114800)^{3/2} \\
 &= \frac{19\sqrt{2}}{3 \times 3.14 d^3} (308011.54) = \frac{\sqrt{2}}{3\pi d^3} (308011.54) \\
 &= \frac{\sqrt{2}}{3} 864
 \end{aligned}$$

Equating the oct shear stress at yielding of an uniaxial tension bar's and using factor = 14

$$\begin{aligned}
 \frac{\sqrt{14}}{3} 864 &= \frac{\sqrt{14}}{3\pi d} = 14 \times 308011.54 \\
 &= 14 \times 308011.54 = \pi d^3 \sigma_m = \pi d^3 \times 207 \times 10^6 \\
 d^3 &= 162.72 \times 10^6 \\
 d &= 162.72 \text{ cm}^3
 \end{aligned}$$

Q No 2

Page # 01

ID = 14374

Solution: Apply a free body analysis to the bar BDE to find the forces exerted by links AB and DC  
→ Evaluate the deformation of links AB and DC or Displacements of B and D  
→ Work out the geometry to find the deflection at E. Given the deflection at B and D

Data

$$E_{Al} = 70 \text{ GPa}$$

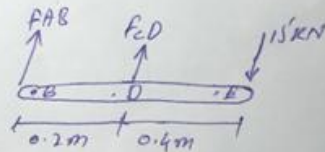
$$A_{Al} = 500 \text{ mm}^2$$

$$E_{St} = 200 \text{ GPa}$$

$$A_{St} = 60 \text{ mm}^2$$

Required data: Deflection a) of B, b) of D and c) of E

Free body BAR BDE



$$\sum M_B = 0$$

$$0 = -(14 \times (0.2 + 0.4)) + F_{CD} \times 0.2$$

$$0 = 8.4 = F_{CD} \times 0.2$$

$$F_{CD} = \frac{8.4}{0.2} \Rightarrow F_{CD} = \boxed{42 \text{ kN}}$$

$$\sum M_D = 0$$

$$0 = -(14 \times 0.4) - F_{AB} \times 0.2 \text{ m}$$

$$0 = -5.6 - F_{AB} \times 0.2 \text{ m}$$

$$\Rightarrow -5.6 = -F_{AB} \times 0.2 \text{ m}$$

$$F_{AB} = \frac{-5.6}{0.2}$$

$$= -28 \text{ kN}$$

Displacement of B  $\delta_B = \frac{PL}{AE}$

$$= \frac{(-28 \text{ kN} \times 10^3)(0.3)}{(500 \times 10^6)(70 \times 10^9)}$$

$$= \frac{8400}{350000000}$$

$$= 2.4 \times 10^{-4} \text{ m}$$

$$\delta_B = \boxed{0.24 \text{ mm}}$$

Displacement of D

$$\delta_D = \frac{PL}{AE}$$

$$= \frac{(42 \times 10^3)(0.4)}{(600 \times 10^6)(200 \times 10^9)}$$

$$= \frac{16800}{120000000} = 1.4 \times 10^{-4}$$

$$\delta_D = 0.14 \text{ mm}$$

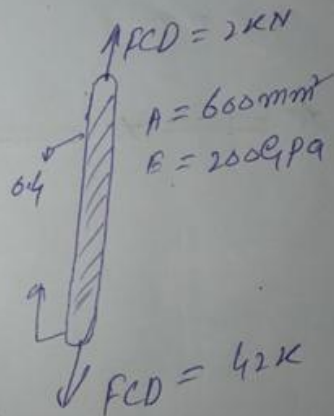
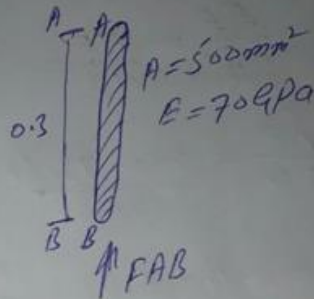
Displacement of D

$$\frac{BB'}{DD'} = \frac{BH}{HD}$$

$$\frac{0.24}{0.14} = \frac{(200 \text{ mm}) - x}{x}$$

$$0.24 \times x = (200 - x)(0.14)$$

$$0.24x = 28 - 0.14x$$



Q1102

page #03

ID = 14374

$$0.24x + 0.14x = 28$$

$$0.38x = 28$$

$$\Rightarrow x = \frac{28}{0.38}$$

$$x = 73.68 \text{ mm}$$

Dia

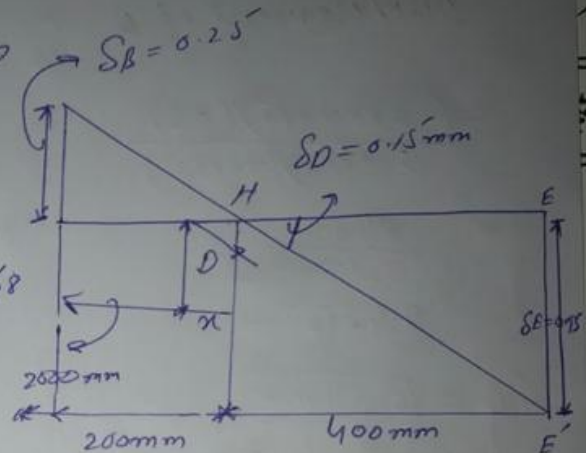
Now

$$\frac{EE'}{DD'} = \frac{HE}{HD}$$

$$\frac{\delta E}{0.14} = \frac{400 + 73.68}{73.68}$$

$$\delta E = 0.14 \times 6.42$$

$$\delta E = \boxed{0.9 \text{ mm}}$$



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Q No 03

3D = 14374  
Given Data:

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$$Q = 14 \times 10^6$$

Allowable shearing stress = ~~10~~ 10 ksi

$$x = 14 + 10$$

$$x = 24$$

Required Data: Largest Torque  $T_0 = ?$

Sol Apply a static equilibrium analysis on the two shafts to find a relation between  $T_{CD}$  and  $T_0$

→ Apply a kinematic analysis to relate the angular rotation of gear's.

$$\sum M_B = 0 = F(0.875 \text{ in}) - T_0$$

$$\sum M_C = 0 = F(2.45 \text{ in}) - T_{CD}$$

$$T_{CD} = 2.8 T_0$$

now  $\gamma_B \phi_B = \gamma_C \phi_C$

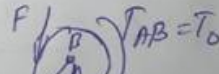
$$\phi_B = \frac{\gamma_C}{\gamma_B} \phi$$

$$\frac{2.45}{0.875 \text{ in}} \phi$$

$$\phi_B = 2.8 \phi_C$$



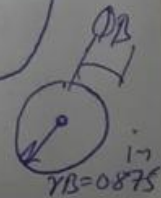
$$C = 2.45 \text{ in}$$



$$\gamma_B = 0.875 \text{ in}$$



$$\gamma_C = 2.45 \text{ in}$$





$$\bar{L}_{max} = \frac{\bar{T}_{ABC}}{J_{AB}} \quad 10000 = \frac{T_0 (0.375 \sin)}{\frac{\pi}{2} (0.375 \sin)^4}$$

$$= \frac{10000 (0.3104)}{0.375} = T_0 = \boxed{827.9}$$

$$\bar{L}_{max} = \frac{T_{CD}}{J_{CD}} \quad 10000 = \frac{2.8 T_0 (0.5 \sin)}{\frac{\pi}{2} (0.5 \sin)^4}$$

$$\frac{10000 \times 0.0981}{2.8 \times 0.5} = T_0 = \frac{981.25}{1.4}$$

$$= 700.89 \text{ Nm}$$

$$\phi_{A/B} = \frac{T_{ABC}}{J_{AB} G} = \frac{(700)(24)}{\frac{\pi}{2} (0.375)^4 (24 \times 10^6)} = \frac{16800}{1.57 \times 10^{10}}$$

$$\frac{16800}{742296} = \phi_{A/B} = 0.02263 \text{ radian}$$

$$= 1.2^\circ$$

$$\phi_{C/D} = \frac{T_{CD}}{J_{CD} G} = \frac{2.8 \times 700 \times 24}{\frac{\pi}{2} (0.5 \sin)^4 (24 \times 10^6)} = \frac{47040}{1.57 \times 10^{10}}$$

$$= \frac{47040}{2355000} = 0.019 \text{ radian}$$

$$= 1.14^\circ$$

$$\phi_D = 2.8 \phi_C = 2.8 \times 1.14 = 3.192$$

$$\phi_A = \phi_B + \phi_{A/B} = 3.192 + 1.2$$

$$\boxed{\phi = 4.392}$$

Q No 04

page # 02

ID = 14374

Given Data:

$$b = 4 \text{ in}$$

$$h = 6 \text{ in}$$

$$t = 0.3 \text{ in}$$

Required Data:

Shear stress distribution for  $V = ?$

Sol

$$e = \frac{Fh}{I}$$

Now

$$F = \int_0^b \tau ds = \int_0^b \frac{VQds}{I} = \frac{V}{I} \int_0^b st \frac{h}{2} ds$$
$$= \frac{Vthb^2}{4I}$$

$$I = I_{\text{web}} + 2I_{\text{flange}} = \frac{1}{2}th^3 + 2 \left[ \frac{1}{12}bt^3 + bt \left( \frac{h}{2} \right)^2 \right]$$
$$= \frac{1}{12}th^2(6b+h)$$

$$\text{Combining } e = \frac{b}{2 + \frac{h}{3b}} = \frac{4 \text{ in}}{2 + \frac{6 \text{ in}}{3 \text{ in}}}$$

$$e = 1.6 \text{ m}$$

Find The Shear stress Distribution for  $V = 14 + 300k$

\* Shear stress in the flange = 17 KIPS

$$\bar{\tau} = \frac{\tau}{t} = \frac{29}{1t}$$

★ Q No 04

Shear stress in the flanges - Page # 02 ID = 14374

$$\bar{\tau} = \frac{VQ}{It} = \frac{V(st) \frac{h}{2}}{It} = \frac{Vh}{2I} s$$

$$\bar{\tau}_B = \frac{Vhb}{2 \left( \frac{1}{12} th^3 \right) (6b+h)} = \frac{6Vb}{th(6b+h)}$$

$$= \frac{6 (17 \text{ kips}) (4 \text{ in})}{(0.15 \text{ in}) (6 \text{ in}) (6 \times 4 \text{ in} + 6 \text{ in})}$$

Shear stress in the web:

$$\bar{\tau}_{\text{max}} = \frac{VQ}{It} = \frac{V \left( \frac{1}{8} ht \right) (4b+h)}{\frac{1}{12} th^3 (6b+h) t} = \frac{3V(4b+h)}{2th(6b+h)t}$$

$$= \frac{3 (\text{kips}) (4 \times 4 \text{ in} + 6 \text{ in})}{2 (0.15 \text{ in}) (6 \text{ in}) (6 \times 6 \text{ in} + 6 \text{ in})}$$

$$= \frac{3 (16+6)}{(0.3)(46)(42)}$$

$$= \frac{66}{75.6}$$

$$= \boxed{0.873 \text{ kips}} \quad \checkmark$$

$$0.873 \text{ kip/in}^2$$

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بعد

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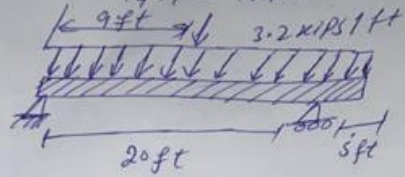
مقدمه

تاریخ

Sol

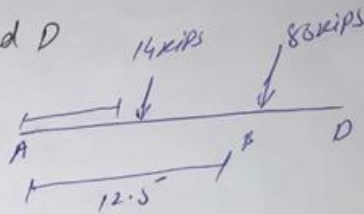
$$S_{all} = 14 + 4 = 18 \text{ ksi}$$

$$T_{all} = 14 + 1 = 15 \text{ ksi}$$



Solution: Reaction at A and D

$$3.2 \times 25 = 80 \text{ k}$$



Taking  $m$  at A  $\rightarrow$

$$14 \times 9 \times 80 \times 12.5 - R_D \times 20 = 0$$

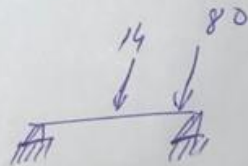
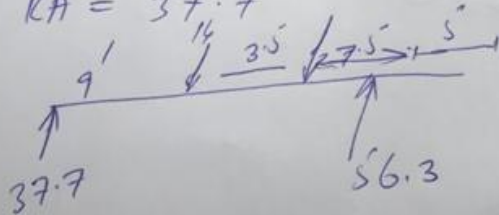
$$R_D = \frac{1126}{20}$$

$$R_D = 56.3$$

Now  $m$  at D  $\rightarrow$

$$R_A \times 20 - 14 \times 11 - 80 \times 7.5 = 0$$

$$R_A = 37.7$$



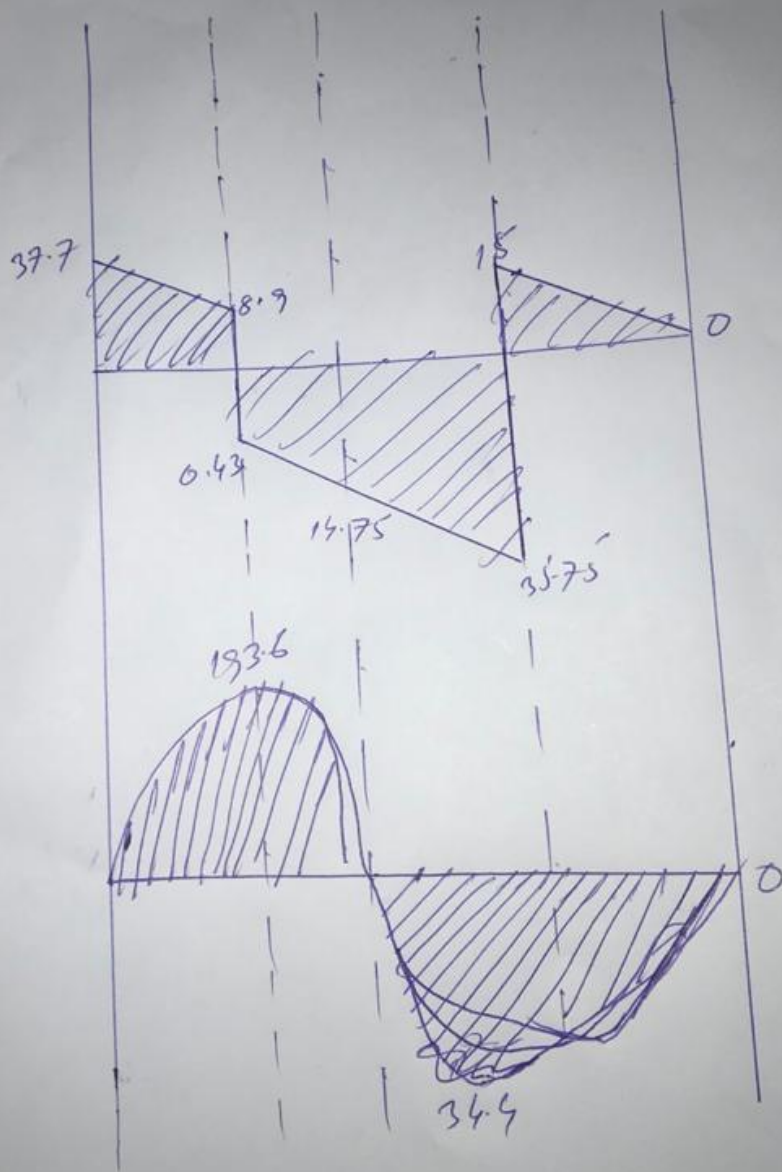
Check

$$14 + 80 = 56.3 + 37.7$$

$$94 = 94$$

Q.5

②



بعد الحساب

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$$1) +ve = (37.25 - 8.9) + (9 \times 0.43) + (8.9 \times 9) \\ = 193.6$$

$$2) -ve = (35.75 - 5.5) \times 11 \times 0.43 + 5.5 \times 11 \\ = 203.58$$

$$3) (16 \times 5) \times 0.43 = 34.4$$

$$4) \text{Maximum normal stress} = 193.6$$

$$5) \text{Max shear} = 34.4$$