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# Q. No 1

Explain in detail types of stirrups with figures & Also explain ACI codes for shear design.

Ans:-

Stirrup:- stirrups are closed-loop bars tied at regular intervals in beam reinforcement to hold the bars in position.

Types of stirrups:-

i. single legged stirrup:- The single-leg stirrups have rarely been used because they are mostly used when binding only two rods.

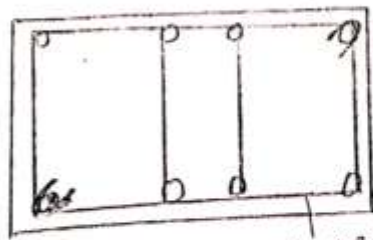


ii. Two legged stirrup:- It is most commonly & widely used stirrup. Minimum 4 bars are required for providing this stirrup.



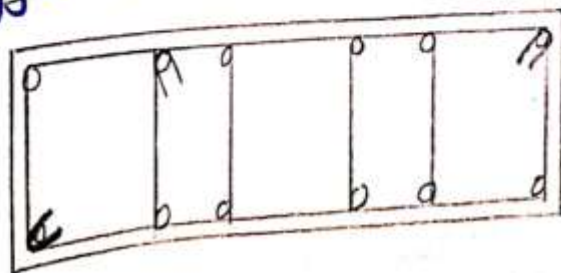
2 legged stirrup.

iii. Four legged stirrup:- These stirrups are used in case of web reinforcement.



4 legged stirrup

iv. Six legged stirrup:-



## ACI codes for Shear Design of a Beam:-

According to ACI-318, following are the formulas used for the shear design of a beam.

1- Critical section:- Critical section occurs at  $45^\circ$  & is at distance  $(d)$  from the face of support which is equal to effective depth.

2- Shear strength capacity of concrete is

$$V_c = 2 \times \sqrt{f'_c} \times b_w \times d$$

3- Minimum Web Reinforcement:-

If  $V_u \leq \phi V_c$ , then theoretically no web reinforcement is required. However ACI code require provision of at least a minimum area of web reinforcement equal to.

$\phi = 0.75$  —> For shear design.

( $\because V_u =$  Total factored shear applied at a given section)

For minimum Reinforcement Area:-

$$A_{\min} = 0.75 \times \frac{\sqrt{f'_c} \times b_w \times S}{f_y} \quad \text{or} \quad \frac{S_0 \times b_w \times S}{f_y} \rightarrow \left[ \begin{array}{l} \text{highest} \\ \text{value is} \\ \text{selected} \end{array} \right]$$

By interchanging the above formulas, we can obtain the formula for maximum spacing.

$$S_{\max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w} \quad \text{or} \quad \frac{A_u \times f_y}{S_0 \times b_w} \left[ \begin{array}{l} \text{lesser value} \\ \text{is selected} \end{array} \right]$$

4- No web-reinforcement is required if

$$V_u < \frac{1}{9} \phi V_c$$

$\Rightarrow$  Between critical section " $V_u$ " & " $\phi V_c$ ", spacing b/w web reinforcement can be find by

$$S = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c}$$

5- If  $V_s \leq 4 \times \sqrt{f'_c} \times b_w \times d$ , then max spacing for stirrups will be the smallest of the following.

i- 24"

ii-  $d/2$

iii-  $S_{max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$

iv-  $S_{max} = \frac{A_u \times f_y}{50 \times b_w}$

$\therefore (V_s = \text{shear force carried by web reinforcement})$

$\Rightarrow$  If  $V_s > 4 \times \sqrt{f'_c} \times b_w \times d$

$\downarrow$   
max. spacing will be halved

$\Rightarrow$  If  $V_s > 8 \times \sqrt{f'_c} \times b_w \times d$

$\downarrow$   
Then either increase cross-sectional dimensions or increase  $f'_c$ .

## Q. No 2

4

### Given data :-

Breadth of web of beam ( $b_w$ ) = 14"

Effective depth ( $d$ ) = 29"

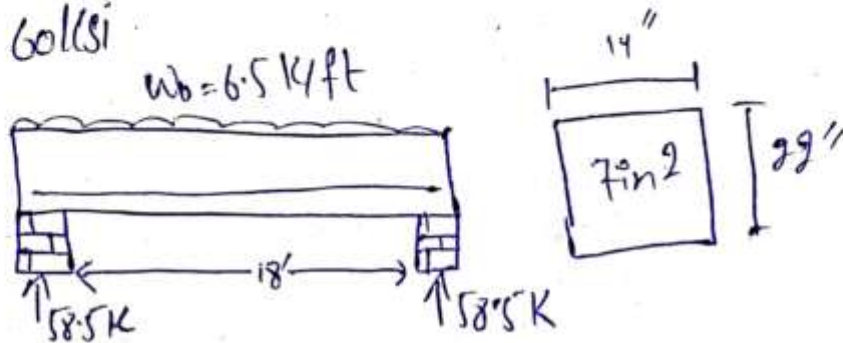
Given load = 6.5 k/ft

Steel Area = ~~6~~ 7 in<sup>2</sup>

$f'_c$  = 4 ksi

$f_y$  = 60 ksi

Sol:-



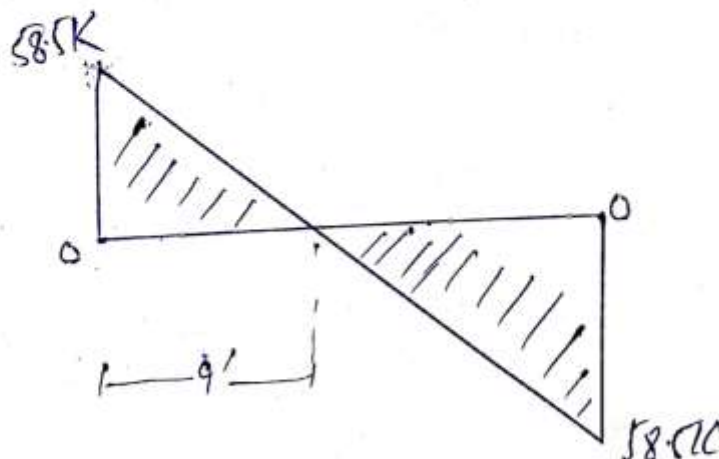
### Step # 01 :- Reactions on supports

Finding the reactions due to applied load

$$\text{Total Load} = \frac{6.5 \times 18}{2} = 58.5 \text{ kips}$$

### Step # 02 :- Shear Force Diagram

The required shear diagram will be



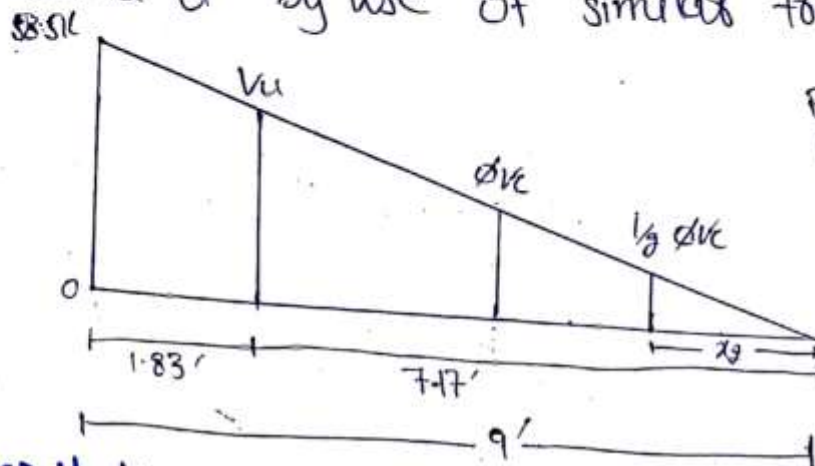
### Step #03:-

Finding the value of critical shear ' $V_u$ ' & its location.

As

we know that critical shear is located at distance ' $d$ ' from face to support  $(d) = 22'' = 1.83'$

$\Rightarrow$  we will find the values of critical shear at distance ' $d$ ' by use of similar triangles.



From similar Triangles

$$\frac{58.5}{9} = \frac{V_u}{8.17}$$

$$V_u = \frac{58.5 \times 7.17}{9}$$

$$V_u = 46.61 \text{ kips}$$

### Step #04:-

Finding the value of ' $\phi V_c$ ' & ' $1/2 \phi V_c$ ' & also its distances from zero shear to right side.

By formula,

$$\Rightarrow \phi V_c = \phi \times 2 \times \sqrt{f_c} \times b_w \times d$$

$$= 0.75 \times 2 \times \sqrt{4000} \times 14 \times 22$$

$$= 29219 \text{ lbs}$$

$$= 29.219 \text{ kips}$$

$\Rightarrow$  location of  $\phi V_c$  by similar triangles,

$$\frac{58.5}{9} = \frac{\phi V_c}{x_1} \Rightarrow \frac{58.5}{9} = \frac{29.21}{x_1}$$

$$\Rightarrow x_1 = 4.49'$$

Similarly,

$$1/2 \phi V_c = \phi V_c / 2 \Rightarrow 29.21 / 2 = 14.60 \text{ kips}$$

$\Rightarrow$  location of  $1/2 \phi V_c$  will be

$$\frac{58.5}{9} = \frac{14.60}{x_2} \Rightarrow x_2 = 2.94'$$

### Step # 05:-

Finding the value of  $\phi V_s$

$$\text{By formula, } V_u = \phi V_s + \phi V_c$$

$$\Rightarrow \phi V_s = V_u - \phi V_c$$
$$= 46.61 - 29.21$$

$$\phi V_s = 17.4 \text{ kips}$$

### Step # 06:-

check on section adequacy,

By formula,

$$= \phi \times 8 \times \sqrt{f_c} \times b_w \times d$$

$$= 0.75 \times 8 \times \sqrt{4000} \times 14 \times 22 = 116877 \text{ lb}$$
$$= 116.87 \text{ kips}$$

As  $\phi \times 8 \times \sqrt{f_c} \times b_w \times d > \phi V_s$

So section is adequate!

### Step # 07:-

check on Maximum <sup>spacing</sup> for stirrups,

$$= \phi \times 4 \times \sqrt{f_c} \times b_w \times d$$

$$= 0.75 \times 4 \times \sqrt{4000} \times 14 \times 22$$

$$= 58438 \text{ lbs}$$

$$= 58.43 \text{ kips}$$

As  $\phi \times 4 \times \sqrt{f_c} \times b_w \times d > \phi V_s$

So maximum will be selected from the following 4 conditions.

1-  $S_{max} = 24''$

2-  $d/8 = 22/8 = 11''$

3-  $S_{max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f_c} \times b_w}$

Here we are using #3 stirrup,  
dia =  $(3/8)'' = 0.375''$

$$\text{So Area} = \frac{\pi}{4} (0.375)^2 = 0.11 \text{ in}^2$$

for 2-legged stirrup

$$\Rightarrow \text{Area} \times 2$$

$$\Rightarrow 0.11 \times 2 = 0.22 \text{ in}^2$$

$$S_{max} = \frac{0.99 \times 60000}{0.75 \times 14000 \times 14} = 19.87''$$

$$4-S_{max} = \frac{A_u \times f_y}{50 \times b_w} = \frac{0.99 \times 60000}{50 \times 14} = 18.85''$$

From above 4 conditions, least value of spacing for # 3, 2 legged stirrup will be selected as,

$$S_{max} = 11''$$

Step # 8:-

stirrups spacing from/at critical section will be

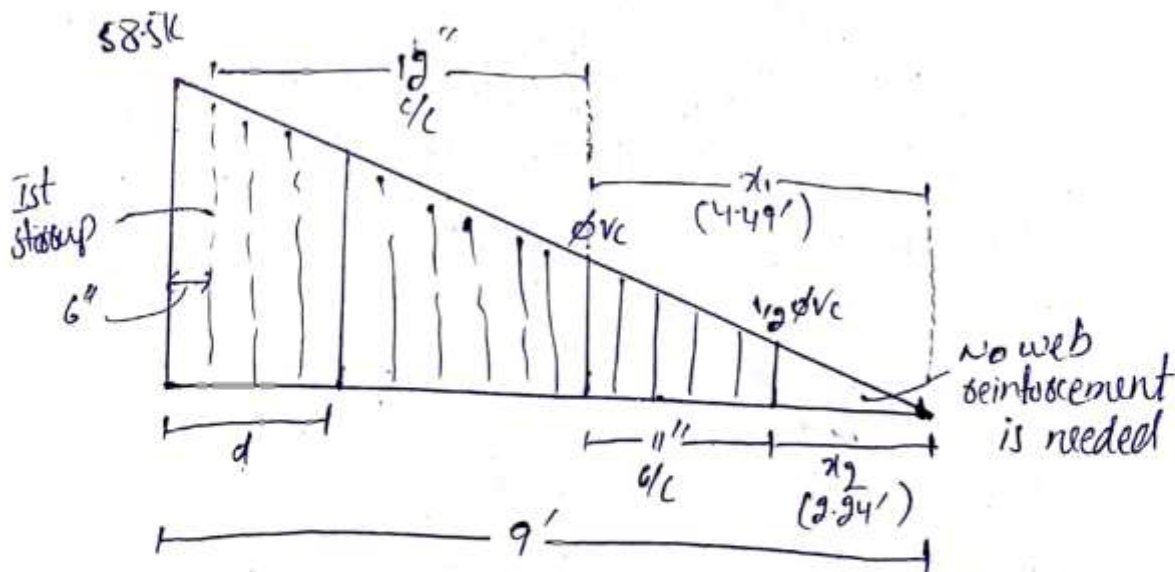
$$S = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.99 \times 60 \times 33}{46.61 - 39.91}$$

$$S = 12.5'' \approx 12''$$

So 12" c/c

Step # 09:-

Final sketch will be



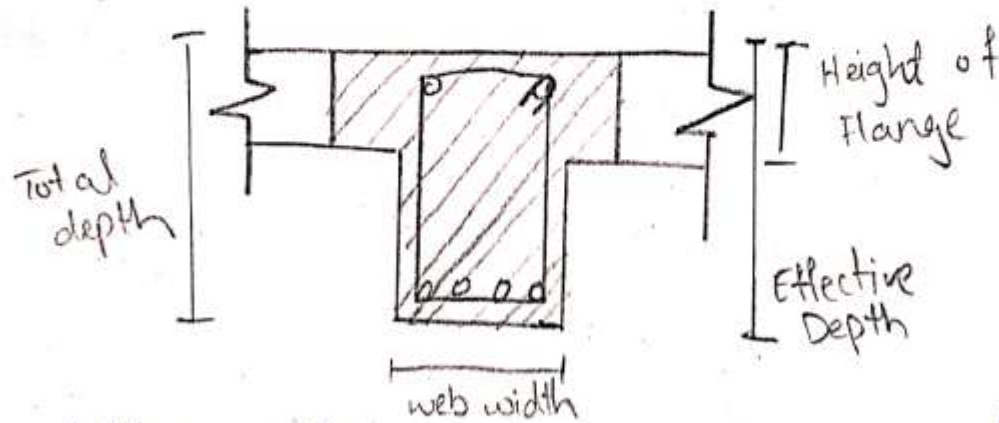
As first stirrup from face of support

$$S/9 = 12/9 = 6''$$



T-Beam:-

=> In most of the reinforced concrete structures, concrete slabs are cast monolithically with the slab so, in this case the beam that act as an intermediate beam are called T-Beams



=> Because of their T-shape, these beams are called T-Beams

=> It is provided at the center of the slab to resist the loads.

=> The upper most area of the beam attached to the slab is called Flange.

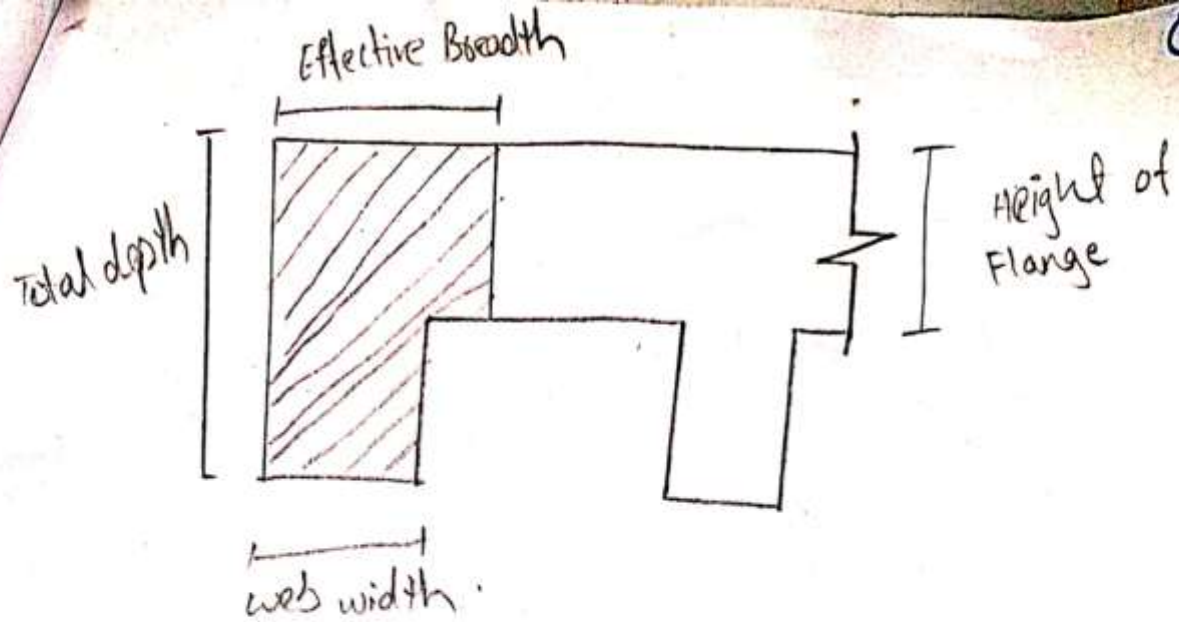
=> The bottom rectangular portion of the beam is called web of the beam.

L-Beam:- L-shaped structure that is in contact with the slab & present at the corners of the floor is called L-Beam.

=> L-Beams are also called Edge Beams

=> It is always provided at the corners of the slab.

=> L-Beams are typically floor beams because of their reduced overall structural depth, the beams are in prestressed or reinforced concrete.



## Flexural Analysis of T-Beam:-

Flexural Analysis of T-Beam consists of the following steps:-

1- For finding the ultimate factored moment, we use the following formula,

$$M_u = \frac{W_u \times L^2}{8}$$

( $W_u$  = Total factored load  
 $L$  = Total span of the beam)

2- Effective width ( $b_e$ ) for T-Beam is calculated as:-

i-  $16(h_f) + b_w$

ii- c/c distance

iii-  $\text{span}/4$

iv-  $\frac{c_t s}{2} + b_w$

$\therefore$  ( $h_f$  = height of flange  
 $c_t s$  = clear transverse span)

- we have to select the least value from above formula.

- If c/c distance is given, then there is no need to of " $\frac{c_t s}{2} + b_w$ "

3- checking whether Rectangular or T-Beam Analysis is required:-

i- If  $a > h_f \rightarrow$  special Analysis is required

ii- If  $a < h_f \rightarrow$  Rectangular beam Analysis is required.

whose

( $a$  = Depth of compression block)  
( $h_f$  = Height of flange)

(15)

4- For Finding Area of steel, we have to use

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

$\phi$  = strength reduction factor  
 $d$  = effective depth  
 $a$  = compression block depth  
 $b_w$  = web width of beam

5- For checking the range of Reinforcement ratio,

$$I_{max} = 0.85 \times B \times \frac{f'_c}{f_y} \times \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$I_{min} = \frac{200}{f_y}$$

$$I = \frac{A_{st}}{b \times d}$$

6- Formula for finding no. of bars required is

$$\text{No. of bars} = \frac{\text{Area of steel}}{\text{Area of single bar}}$$

7- for checking minimum width for bars accommodation

$$b_{min} = 2(\text{clear cover}) + 2(\text{dia of stirrup}) + \text{No. of bars} \times (\text{dia of bar}) + \frac{\text{spacing}}{b/w \text{ bars}} (\text{dia of bar})$$

8- Design moment of given by

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2) \rightarrow \text{if } a < h_f$$

$$M_d = \phi \times [A_s \times f_y \times (d - h_f/2) + (A_s - A_{st}) \times f_y \times (d - a/2)]$$

if  $a > h_f$

## Q.No 4

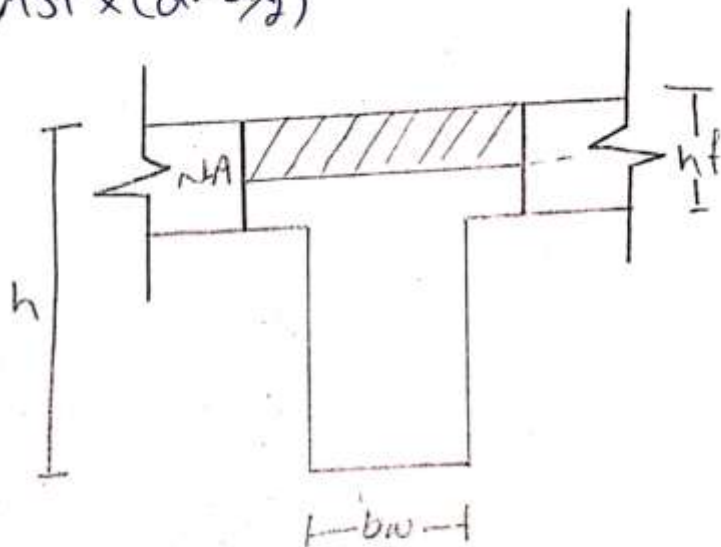
What is the difference b/w CASE-1 & CASE-2 in the design of T-Beam?

### CASE:-01

From the Figure  $a < hf$   
So in this case, Rectangular Beam Analysis is required.

So, the design moment formula will be

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2)$$

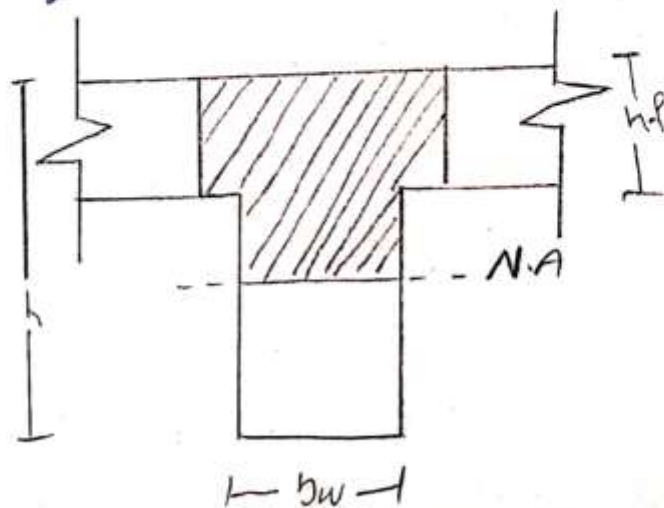


### CASE 2:-

From the Figure  $a > hf$   
So in this, special beam Analysis i.e., T-Beam Analysis is required.

So, the required Design Moment <sup>formula</sup> will be

$$M_d = \phi \times [A_s \times f_y \times (d - \frac{hf}{2}) + (A_s - A_{st}) \times f_y \times (d - a_g)]$$



## Q. No 5

A floor system consists of 3.5" concrete slab supported by 16' simple span spaced at 9' c/c the beam having a web width of 10" & effective depth of 18" & total height is 23". Calculate the necessary flexural reinforcement if the factored applied moment is 5800 kip-inch. Use  $f_c' = 3 \text{ ksi}$  &  $f_y = 60 \text{ ksi}$

Given:-

Height of flange  $(h_f) = 3.5''$

c/c distance = 9'

length/span of the beam = 16'

web width  $(b_w) = 10''$

Height  $(h) = 23''$

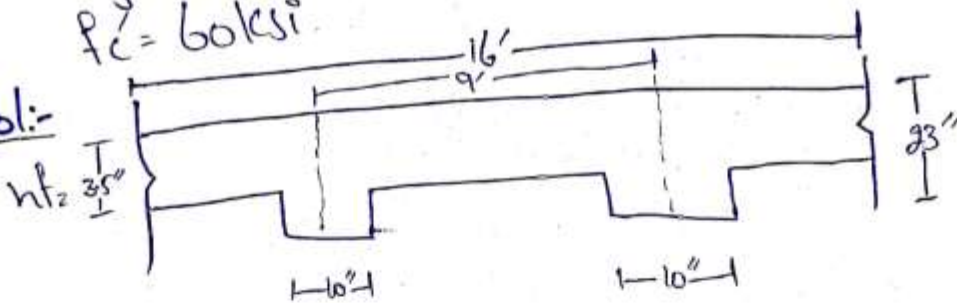
Effective depth  $(d) = 18''$

Total factored moment  $(M_u) = 5800 \text{ kip-inch}$

$f_y = 60 \text{ ksi}$

$f_c' = 3 \text{ ksi}$

Sol:-



Step # 01:-

Calculate the effective  $(b_e)$  for T-beam

$$1 - b_f(h_f) + b_w = 16(3.5) + 10 = 66''$$

$$2 - \text{span}/4 = \frac{16}{4} \times 12 = 48''$$

$$3 - \text{c/c distance} = 9 \times 12 = 108''$$

Selecting the least value of  $b_e$  as,

$$b_e = 48''$$

Step # 02:-

check whether Rectangular or T-beam Analysis is required

Trial #01:- Let  $a = hf = 3.5''$

$$A_{st} = \frac{Mu}{\phi \times f_y \times (d - a/2)} = \frac{5800}{0.90 \times 60 \times (18 - 3.5/2)} = 6.61 \text{ in}^2$$

Trial #02:-  $a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b \times \phi}$

$$a = \frac{6.61 \times 60}{0.85 \times 3 \times 48} = 3.2''$$

$$\epsilon_t A_{st} = 6.55 \text{ in}^2 \Rightarrow 3.2'' < 3.5''$$

So Rectangular Beam Design is required

Trial #03:-

$$a = 3.21''$$

$$\epsilon_t A_{st} = \frac{5800}{0.90 \times 60 \times (18 - 3.21/2)} = 6.55 \text{ in}^2$$

So Area of steel is  $6.55 \text{ in}^2$

Step # 03:-

check  $S_{max}$  &  $S_{min}$

$$\Rightarrow S_{max} = 0.85 \times B \times \frac{f'_c}{f_y} \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_t} \right)$$

$$= 0.85 \times 0.85 \times \frac{3}{60} \left( \frac{0.003}{0.003 + 0.005} \right) = 0.0013$$

$$\Rightarrow S_{min} = \frac{200}{f_y} = \frac{200}{60000} = 0.003$$

$$\Rightarrow S_r = \frac{A_{st}}{b \times d} = \frac{6.55}{10 \times 18} = 0.036$$

$$S_{min} < S < S_{max}$$

$$0.003 < 0.036 < 0.013$$

As the value of  $\rho_{max}$  is less than  $\rho$ , so we have to design it as "doubly reinforced beam"  
2) First we have to find the Area of steel against  $\rho_{max}$ .

$$\rho_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = \rho_{max} \times (b \times d)$$

$$A_{st} = 0.013 \times (10 \times 18)$$

$$A_{st} = 2.34 \text{ in}^2$$

Step # 04:-

Finding the value of  $M_{ug}$ :-

By formula.

$$M_{ug} = \phi \times A_{st} \times f_y \times (d - a/2)$$

First finding the value of 'a'

$$\Rightarrow a = \frac{A_{st} \times f_y}{0.85 \times F_c \times b} = \frac{2.43 \times 60}{0.85 \times 3 \times 10}$$

$$a = 5.79''$$

$$\Rightarrow M_{ug} = 0.90 \times 2.43 \times 60 \times (18 - 5.79/2)$$

$$\Rightarrow M_{ug} = 1986.67 \text{ kip-inch}$$

$$\text{As } M_{ug} < M_u$$

$$1986.67 < 5800$$

So we have to design the beam in such way that it can resist more bending moment than the applied external moment.

Step # 05:-

Finding difference in moments & Area of steel.

$$M_{u1} = M_u - M_{ug}$$

$$= 5800 - 1986.67$$

$$M_{u1} = 3813.33 \text{ kip-inch}$$

By formula,

$$A_{st} = \frac{Mu}{\phi \times f_y \times (d-d')} = \frac{3813.33}{0.90 \times 60 \times (18-2.5)}$$

$$A_{st} = 4.56 \text{ in}^2$$

Step #06:-

Finding total steel Area

$$A_s = A_{st} + A_{st}' \\ = 2.43 + 4.56 = 6.99 \text{ in}^2$$

Step #07:-

Selection of Bar:-

In tension zone

Let we use #8 bars

$$\text{dia } (8/8) = 1" \rightarrow A_{\text{area}} = \frac{\pi}{4} (1)^2 = 0.785 \text{ in}^2$$

By formula

$$\text{No. of bars} = \frac{\text{Area of steel}}{\text{Area of single bar}} = \frac{6.99}{0.785} = 8.9 \approx 9$$

So 9 #8 bars

In compression zone:-

Let we use #7 bars

$$\text{dia } (7/8)" \rightarrow A_{\text{area}} = \frac{\pi}{4} (7/8)^2 = 0.601 \text{ in}^2$$

By formula

$$\text{No. of bars} = \frac{\text{Area of steel}}{\text{Area of single bar}} = \frac{4.56}{0.601} = 7.58 \approx 8$$

So 8 #7 bars.

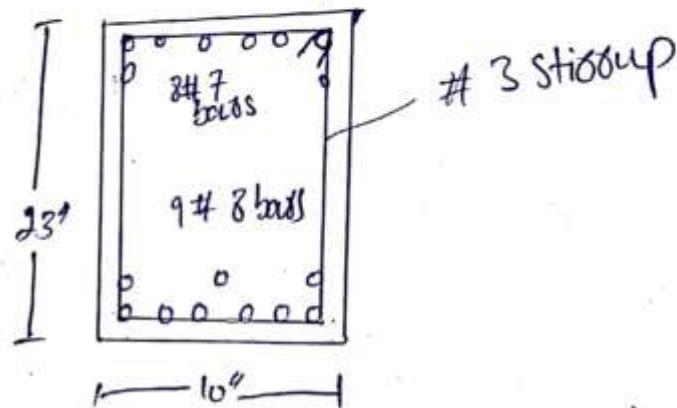




### Step # 08:-

Min width for Accomodation of bars.  
$$D_{min} = (2 \times 1.5) + (2 \times 3/8) + 9(8/8) + 8(8/8)$$
$$= 20.75''$$

As  $20.75'' > 10''$   
So, the bars will be placed in multiple layers.



$$\text{Effective depth } (d) = 23 - 1.5 + \frac{3}{8} + \frac{8}{8} + \frac{1}{2}(8/8) = 19.6''$$

$$\text{Effective cover } (d') = 1.5 + \frac{3}{8} + \frac{7}{8} + \frac{1}{2}(\frac{7}{8}) = 3.18''$$

### Step # 09:-

Finding the Design Moment

$$M_d = \phi [A_s' \times f_y \times (d - d') + (A_{st} - A_s') \times f_y \times (d - a/2)]$$

$$\text{First } a = \frac{(A_s - A_s') \times f_y}{0.85 \times f_c' \times b} = \frac{(9 \times 0.785 - 8 \times 0.601) \times 60}{0.85 \times 3 \times 10} = 5.31''$$

$$\Rightarrow M_d = 0.90 [(8 \times 0.601) \times 60 \times (19.6 - 3.18) + (9 \times 0.785 - 8 \times 0.601) \times 60 \times (19.6 - \frac{5.31}{2})]$$

$$M_d = 6328.38$$

$$\text{As } 6328.38 > 5800$$

Design is perfect.

## Q.No 6

(17)

A beam is revised to developed & ultimate moment of 6000 kip-inches limited to 14x26 inch size, use  $f'_c$  is 4 ksi &  $f_y$  is 60 ksi. Determine flexural reinforcement assume two rows of tensile reinforcement & effective depth of beam is 22 inch.

Sol:-

Concrete compression strength ( $f'_c$ ) = 4 ksi

Steel Tensile strength ( $f_y$ ) = 60 ksi

Breadth (b) = 14"

Height (h) = 26"

Ultimate Factored Moment ( $M_u$ ) = 6000 kip-inch

Effective depth of beam (d) = 22"

Assume effective cover (d') = 2.5"

Step # 01 :- (Reinforcement ratio)

By formula

$$S_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_t} \right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$S_{max} = 0.0180$$

Step # 02 :- Area of steel

As we know that

$$S_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = S_{max} \times (b \times d)$$

$$A_{st} = 0.0180 \times (14 \times 22)$$

$$A_{st} = 5.54 \text{ in}^2$$

### Step # 03 Design Moment

By using formula

$$M_{u2} = \phi \times A_{st} \times f_y \times (d - a/2)$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f_c \times b} = \frac{5.54 \times 60}{0.85 \times 4 \times 14} = 6.98''$$

$$a = 6.98''$$

$$\text{So } M_{u2} = 0.90 \times 5.54 \times 60 \left( 22 - \frac{6.98}{2} \right) \\ = 5537.4 \text{ kip-inch}$$

$$\underline{As}; \quad 5537.4 < 6000$$

So we have to design a section as doubly reinforced

### Step # 04 (Difference in Moments)

$$M_{u1} = M_u - M_{u2} \\ = 6000 - 5537.4$$

$$M_{u1} = 462.6 \text{ kip-inches}$$

### Step # 05: Area of steel

$$M_{u1} = \phi \times A_{st}' \times f_y \times (d - d')$$

compression zone area,

$$A_{st}' = \frac{M_{u1}}{\phi \times f_y \times (d - d')} = \frac{462.6}{0.90 \times 60 \times (22 - 2.5)}$$

$$A_{st}' = 0.44 \text{ in}^2$$

### Step # 06 Total Steel Area

$$A_s = A_{st} + A_{st}' \\ = 5.54 + 0.44$$

$$A_s = 5.98 \text{ in}^2$$

## Step # of Selection of bars & No. of bars (19)

① Steel in tension zone :-

we use #7 bars

$$\text{dia } (7/8)'' = 0.875$$

$$\text{Area} = \frac{\pi}{4} (0.875)^2$$

$$A = 0.601 \text{ in}^2$$

$$\text{So, No. of bars} = \frac{A_s}{\text{Area of single bar}}$$
$$= \frac{5.98}{0.601} = 9.9 \approx 10 \text{ bars}$$

So, 10 #7 bars

② steel in compression zone :-

we use #5 bars

$$\text{dia} = (5/8)'' = 0.625''$$

$$\text{Area} = \frac{\pi}{4} (0.625)^2$$

$$A = 0.306 \text{ in}^2$$

$$\text{No. of bars} = \frac{A_s}{\text{Area of single bar}}$$

$$= \frac{0.44}{0.306} = 1.43 \approx 2 \text{ bars}$$

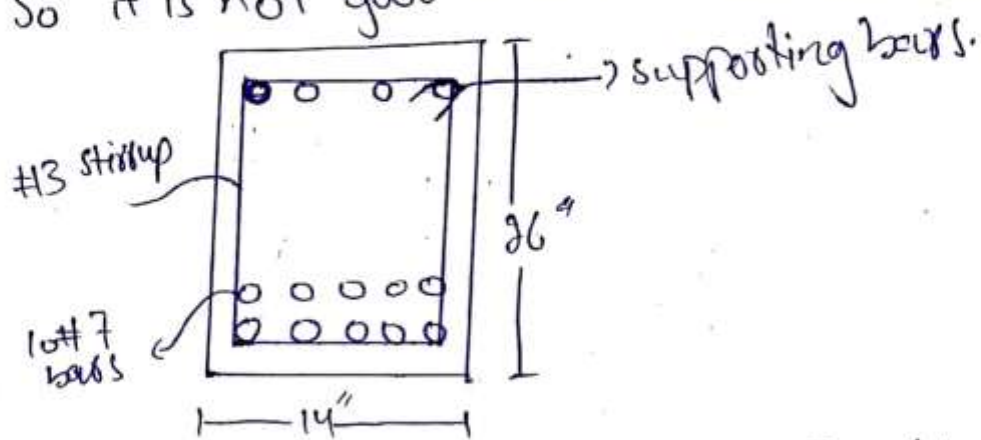
So, 2 #5 bars

### Step # 8:- Minimum width of beam

$$b_{min} = 2(1.5) + 2(3/8) + 10(7/8) + 9(7/8)$$

$$b_{min} = 20.39 > 14$$

So it is not good in one layer.



$$\Rightarrow \text{effective depth } (d) = 26 - 1.5 - 3/8 - 7/8 - 1/2 (7/8)$$
$$= 22.82''$$

$$\Rightarrow \text{effective cover } (d') = 1.5 + \frac{3}{8} + 1/2 (5/8)$$
$$= 2.18$$

### Step # 9:- Design Moment

$$M_d = \phi \times [A_{st} \times f_y \times (d - d') + (A_{st} - A_{st}') \times f_y \times (d - a/2)]$$

$$a = \frac{(A_{st} - A_{st}') \times f_y}{0.85 \times f_c' \times b}$$

$$= \frac{(10 \times 0.601 - 2 \times 0.306) \times 60}{0.85 \times 4 \times 14} = 6.80''$$

$$M_d = 0.90 [(2 \times 0.306) \times 60 \times (22.82 - 2.18) + (10 \times 0.601 - 2 \times 0.3 \times 60 \times 60 \times (22.82 - 6.80/2))]$$

$$M_d = 7047.6 \text{ kip-inch}$$

$$= 7047.6 > 6000$$

Design is OK.