

Name : Mudasir  
khan

ID : 7890

Section : A

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Subject : Structures Analysis

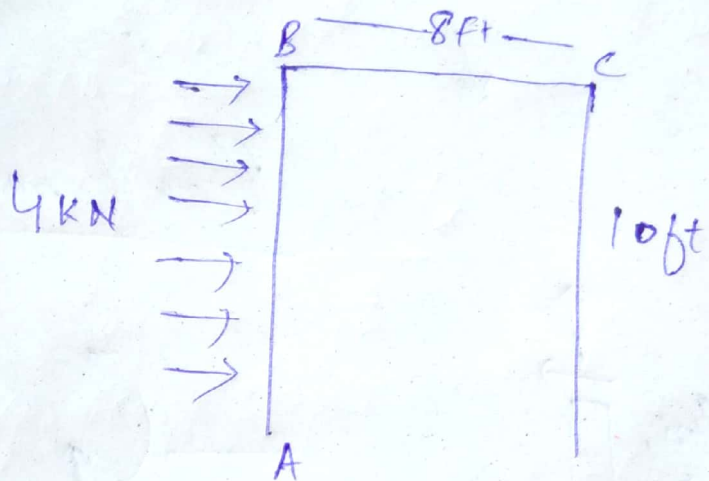
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(1)

Q No 1

Given Data

Ans:



$$E = 29 \times 10^3 \text{ ksi}$$

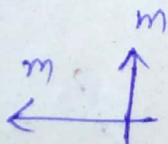
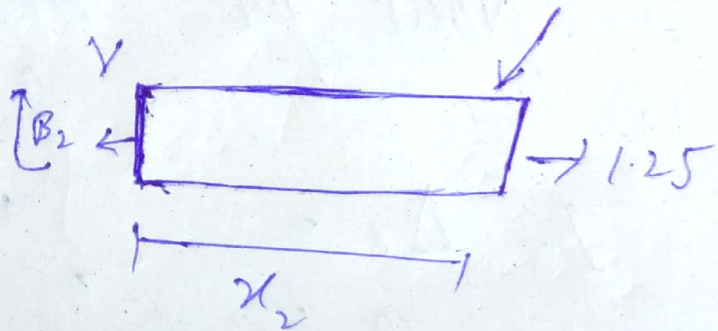
$$I = 600 \text{ in}^4$$

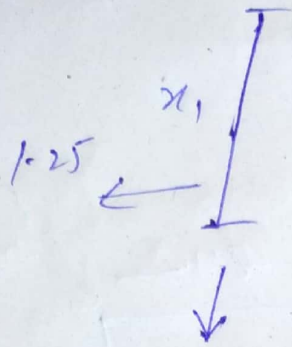
Required data:

Vertical displacement  $\Delta$ ?

Vertical moment  $\Delta$ ?

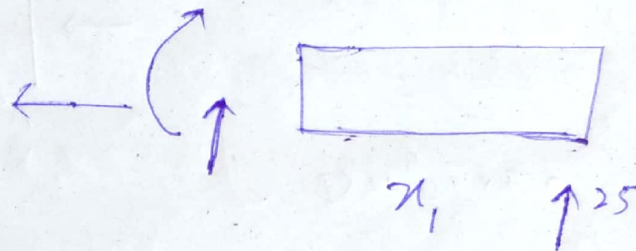
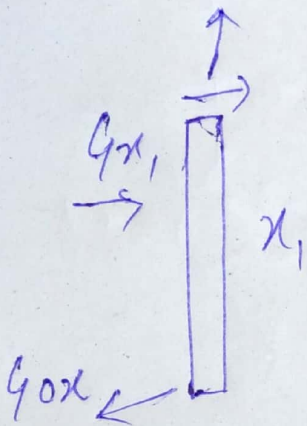
Solution  $\Rightarrow$





$$m_2 = 1.25x$$

Real moment



$$m_2 = 25x_2$$

$$M = 40x_1 - 2x \frac{1}{2} (x_1)$$

$$= 40x_1 - 2x^2$$

Now put virtual work

$$I - \Delta c = \int_0^2 m \frac{M}{E} dx$$

$$= \int_0^{10} 1x_1 \left( \frac{40x_2 - 2x^2}{E} \right) dx + \int_0^8 \frac{(1.25x_1)(25x_2)}{EI} dx$$



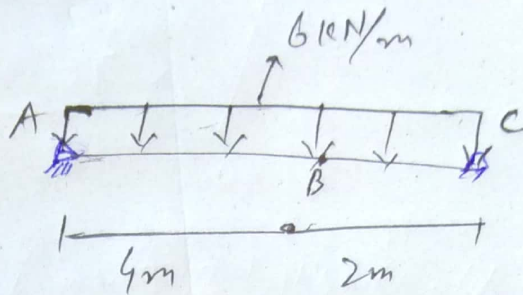
$$\Delta I = \frac{1}{EI} \left( \frac{40x^3}{3} - \frac{2x^4}{4} \right) \Big|_0^{10} + \left( \frac{31.25x^3}{3} \right) \Big|_0^8$$

$$\Delta I = \frac{1}{EI} (2.333 + 18666.66)$$

$$\Delta I = \frac{33999.99}{(200)(60 \times 10^6)}$$

$$\Delta I = 2.833 \times 10^{-6} \text{ in}$$

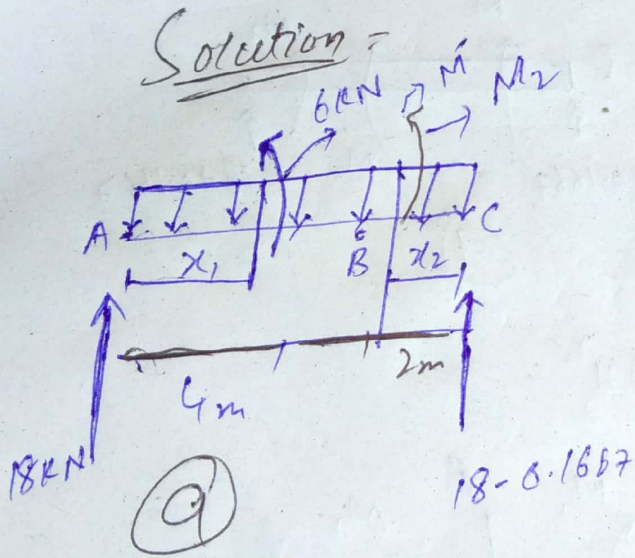
# Q No 2



Required -

Slop and displacement at point B.

Solution -



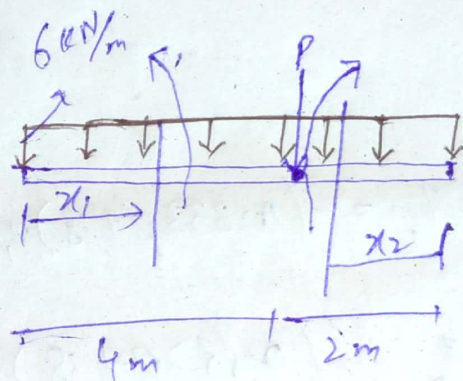
$$R_1 + R_2 = 0 \rightarrow \text{①}$$

$$\sum M_A = 0 \hookrightarrow +$$

$$1 + R_2(6) = 0$$

$$\Rightarrow -0.16667 \text{ put in ①}$$

P.T.O



②

$$R_1 + R_2 = 1$$

$$\hookrightarrow + \sum M_A = 0$$

$$-(1)(4) + R_2(6) = 0$$

$$R_2 = 0.6667 \text{ kN}$$



$$R_1 + (-0.1667) = 0$$

$$R_1 = 0.16667 \text{ kN}$$

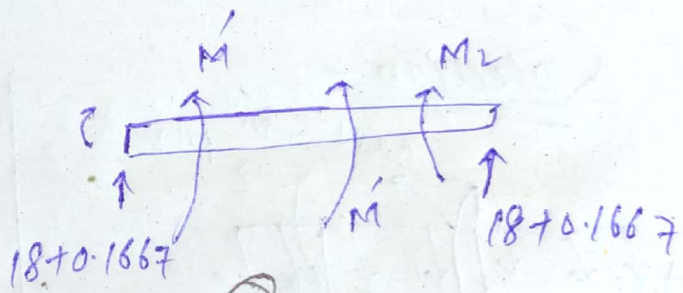
$$R_2 = 1 - 0.1667 \text{ kN}$$

$$R_2 = 0.8333 \text{ kN}$$

Shown

$$M_1 = (18 + 0.1667 M') x_1 - 2x_1^2$$

$$M_2 = (18 - 0.1667 M') x_2 - 2x_2^2$$

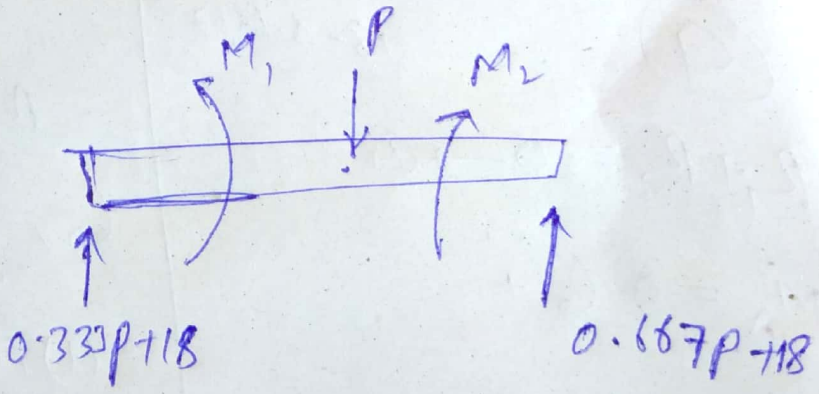


$$M_1 = (0.333p + 18) x_1 - 2x_1^2$$

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$$M_2 = (0.667p + 18) x_2 - 2x_2^2$$

(b)



The displacement function shown in the figure "a" above

$$\frac{\partial M_1}{\partial M} = 0.1667x_1, \text{ and } \frac{\partial M_2}{\partial M} = 0.1667x_2$$

$$\text{Set } M' = 0 \text{ then } M_1 = (18 + 0.1667(0)x_1 - 2x_1^2)$$

$$\rightarrow M_1 = (18x_1 - 2x_1^2)$$

$$\rightarrow M_2 = (18x_2 - 2x_2^2)$$

$$Q_B = \int_0^2 M \left( \frac{\partial M}{\partial M_1} \right) \frac{dx}{EI} = \int_0^4 \frac{(18x_1 - 2x_1^2)(0.1667x_1)}{EI} dx_1$$

$$\int_0^4 \frac{(18x_2 - 2x_2^2)(0.1667x_2)}{EI} dx_2$$

$$Q_B = \frac{42.65}{EI} + \frac{6.66}{EI}$$

$$Q_B = \frac{49.31}{EI}$$

$$Q_B = \frac{49.31}{(200 \times 10^6 \text{ kPa})(0.60006)}$$

$$Q_B = 0.4411 \text{ rad}$$

→ For the displacement function are shown in figure "b"

$$\frac{\partial M_1}{\partial MP} = 0.333x_1 \quad \text{and} \quad \frac{\partial M_2}{\partial P} = 0.667x_2$$

also set  $P = 0$  then

$$M_1 = (18x_1 - 2x_1^2) \text{ kN}\cdot\text{m}$$

$$M_2 = (18x_2 - 2x_2^2) \text{ kN}\cdot\text{m}$$

thus



$$\Delta B = \int_0^L \frac{(30x_1 - 2x_1^2)(0.333x_1)}{EI} dx +$$

$$\int_0^2 \frac{(30x_2 - 2x_2^2)(0.6667x_2)}{EI} dx$$

$$\Delta B = \frac{218.5}{EI} \Rightarrow \frac{218.5}{(200 \times 10^6)(0.0006)} =$$

$$\boxed{0.018 \text{ m or } 18 \text{ mm}}$$



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# Q No 3

Given data :-  $W_0 = \text{Uniform load} = 400 \text{ lb/ft}$

$h = 10 \text{ ft}$  ,  $L = 15 \text{ ft}$

Required - Equation of curve and force in cable = ?

Solution: We know that

$$y = \frac{h}{L^2} x^2$$

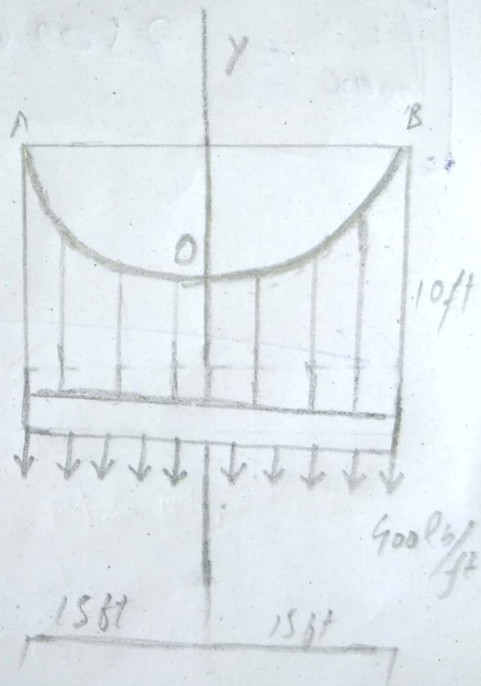
putting the value

$$y = \frac{h}{L^2} x^2$$

$$= \frac{10}{(15)^2} x^2 = 0.044 x^2$$

$$T_0 = F_H = \frac{W_0 L^2}{2h} = \frac{400 \times (15)^2}{2 \times 10}$$

$$T_0 = 4500 \text{ lb} = 4.5 \text{ K}$$





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$$T_B = T_{max} \sqrt{(F_H)^2 + (W_0 L)^2}$$
$$= \sqrt{(4500)^2 + (400 \times 15)^2}$$

$$T_{max} = 7500 \text{ lb} = 7.5 \text{ k}$$

Now " $T_{max}$ " by another Equation

$$T_B = T_{max} = W_0 L \sqrt{\left(1 + \frac{L}{2h}\right)^2}$$
$$= 400 \times 15 \sqrt{1 + \left(\frac{15}{2 \times 10}\right)^2}$$

$$T_{max} = 7500 \text{ lb} = 7.5 \text{ k}$$

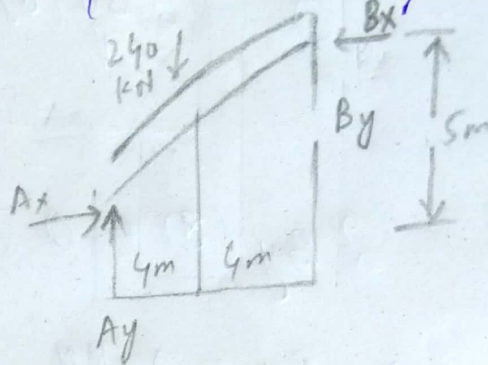
# Q NO 4

(B)

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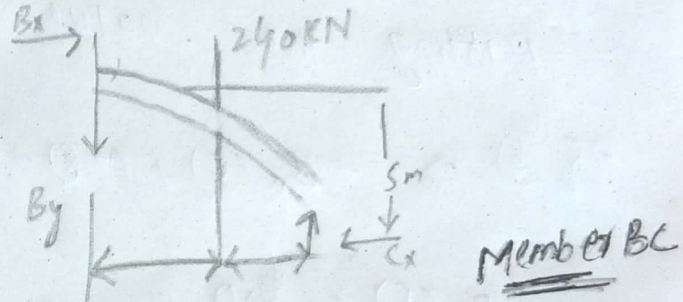
Given data:

Uniform load =  $30 \text{ kN/m}$



Required data:

Internal moment at D = ? Member AB



Solution:

Dividing into two members

AB and BC.

AB →

$$\hookrightarrow + \sum M_A = 0$$

$$B_x(5) + B_y(8) - 240(4) = 0 \quad \rightarrow \text{(a)}$$

BC →

$$\hookrightarrow + \sum M_B = 0$$

$$-B_x(5) + B_y(8) + 240(4) = 0 \quad \rightarrow \text{(b)}$$



Adding eq (A) and (B)

$$B_x(5) + B_y(8) - 240(4) = 0$$

$$-B_x(5) + B_y(8) + 240(4) = 0$$

$$0 + 2B_y(8) + 0 = 0$$

$$2B_y(8) = 0$$

$$\Rightarrow \underline{B_y = 0 \text{ kN}}$$

Putting the value of "B<sub>y</sub>" in eq (A)

$$\text{eq (A)} \Rightarrow -B_x(5) + 0(8) + 960 = 0$$

$$B_x(5) = 960$$

$$\frac{B_x(5)}{5} = \frac{960}{5}$$

$$\boxed{B_x = 192 \text{ kN}}$$

" Now at Segment "DB"

$$\curvearrowright \sum M_D = 0$$

$$192(2) - 150(2.5) - M_D = 0$$

$$384 - 375 - M_D = 0$$

$$9 - M_D = 0$$

$$\Rightarrow \boxed{M_D = 9 \text{ kNm}}$$