

Name ROOHULLAH

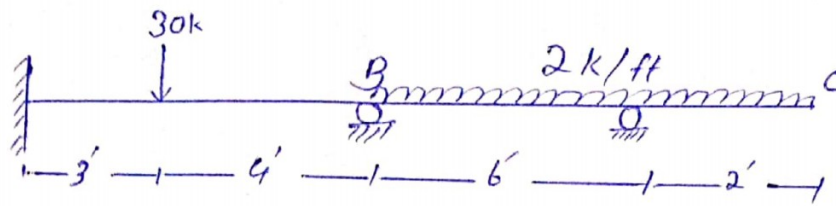
FD 7719

Section "B"

Subject Structure Analysis  
II

Teacher Engr Adeed Khan

Q NO # 01



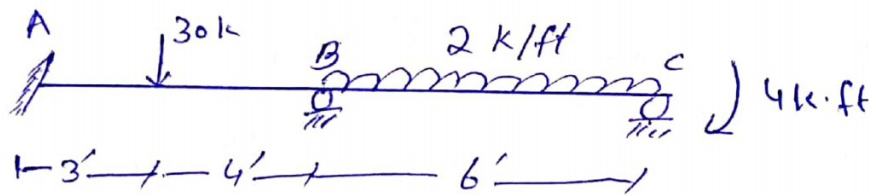
Soln. 01

Step #1

Determining kinematic indeterminacy,

$$K.I = 5^{\circ}$$

So we have to reduce the external portion.



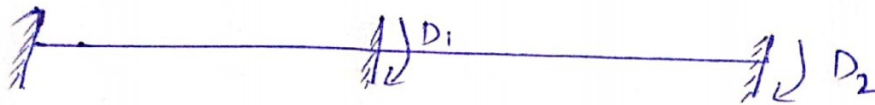
$$\Rightarrow \frac{2(2)}{1} = 4 \text{ k.ft}$$

Now ::

$$K.I = 2^{\circ}$$

Step #2

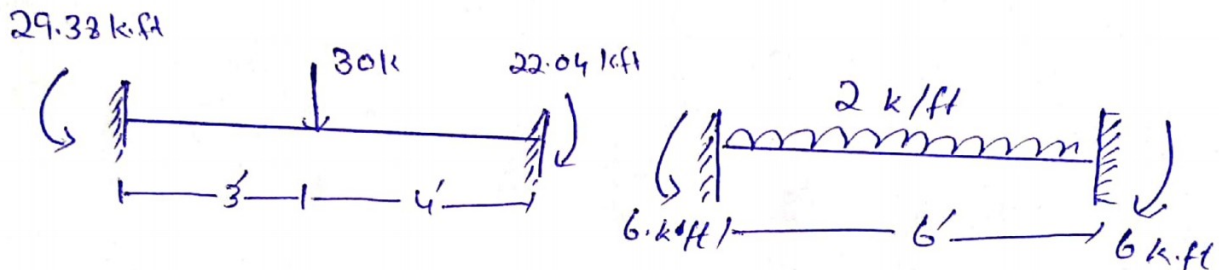
Determine unknown Joint Displacement.



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

Step#03

Compute  $[ADL]$  Matrix



$\Rightarrow$  For Pointed load (not at mid)  
 $\Rightarrow$  For Left end:

$$\frac{Pab^2}{L^2} = \frac{(30)(3)(4)^2}{(7)^2} = 29.38 \text{ k.ft}$$

$\Rightarrow$  For Right end:

$$\frac{Pa^2b}{L^2} = \frac{(30)(3)^2(4)}{(7)^2} = 22.04 \text{ k.ft}$$

$\Rightarrow$  For UDL:

$$\frac{WL^2}{12} \Rightarrow \frac{(2)(6)^2}{12} = 6 \text{ k.ft}$$

$$ADL_1 = +22.04 - 6 = 16.04 \text{ k}\cdot\text{ft}$$

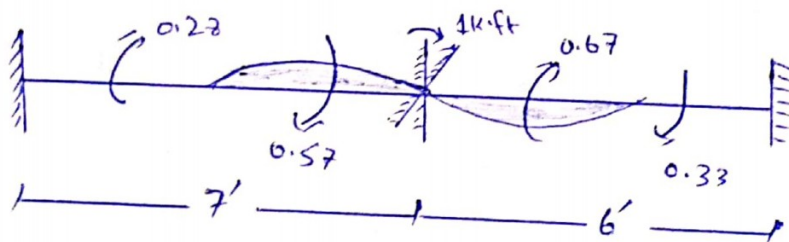
$$ADL_2 = 6 \text{ k}\cdot\text{ft}$$

Step #04

Compute  $[S]$  matrix

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

(9)  $D_1 = 1 \text{ k}, \quad D_2 = 0$



$$\textcircled{a} \quad \frac{4EI}{7} = 0.57$$

$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$\frac{2EI}{7} = 0.23$$

$$S_{11} = 0.57 + 0.67$$

$$= 1.24 EA$$

$$S_{21} = 0.33 EA$$

b)  $D_1 = 0$        $D_2 = 1 \cdot k$



$$\theta \quad \frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$S_{12} = 0.33$$

$$S_{22} = 0.67$$

$$S \begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$$

Step #05

Compute  $[D]$  Matrix

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}^{-1} \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$= \frac{1}{\begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}} \times \text{Adj } A \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$|S| = (1.24 \times 0.67) - (0.33 \times 0.33)$$

$$= 0.8308 - 0.1089$$

$$|S| = 0.7219$$

$$\text{Adj } A = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}$$

Now

$$\begin{bmatrix} AD_1 & -ADL_1 \\ AD_2 & ADL_2 \end{bmatrix} = \begin{bmatrix} 0 & -16.04 \\ 4 & -6 \end{bmatrix} = \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} E$$

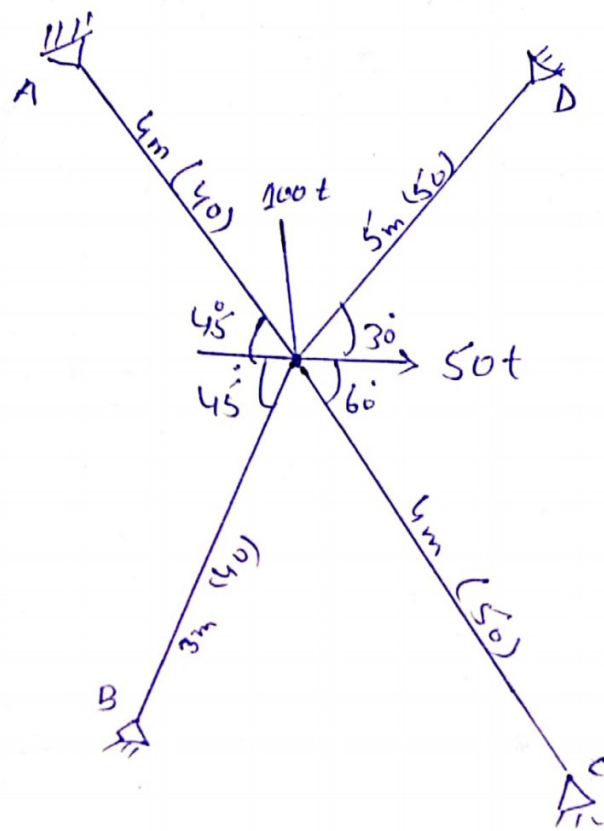
$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \frac{\begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}}{0.7219} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.919 & -0.452 \\ -0.452 & 1.70 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.83 \\ 3.85 \end{bmatrix}$$

Ans.

Q NO # 02



$$E = 20000 \text{ t/cm}^2$$

Solution:

For A

$$\sin 45^\circ = \frac{P}{H} = \frac{P}{4}$$

$$\rightarrow P = 2.828 \text{ m}$$

$$\cos 45^\circ = \frac{b}{H} = \frac{b}{4}$$

$$\rightarrow 2.828 \text{ m}$$

For B

$$\sin 45^\circ = \frac{P}{H} = \frac{P}{3}$$

$$\rightarrow P = 2.12 \text{ m}$$

$$\cos 45^\circ = \frac{b}{H} = \frac{b}{3}$$

$$\rightarrow b = 2.12 \text{ m}$$

For C

$$\sin 60 = \frac{P}{H} = \frac{P}{4}$$

$$\rightarrow \cancel{P} = (\sin 60) 4 = P$$

$$\rightarrow P = 3.46 \text{ m}$$

$$\cos 60 = \frac{b}{H} = \frac{b}{4}$$

$$\cos 60 \times 4 = b$$

$$\rightarrow b = 2 \text{ m}$$

For D:

$$\sin 30 = \frac{P}{5}$$

$$\rightarrow P = 2.5 \text{ m}$$

$$\cos 30 = \frac{b}{5}$$

$$\cancel{P} \rightarrow P = 4.33 \text{ m}$$



Now

$$EA(A) = 2000 \times 40 = 80,000t$$

$$EA(B) = 2000 \times 40 = 80,000t$$

$$EA(C) = 2000 \times 50 = 100,000t$$

$$EA(D) = 2000 \times 50 = 100,000t$$

Step # 01  $k \cdot I$

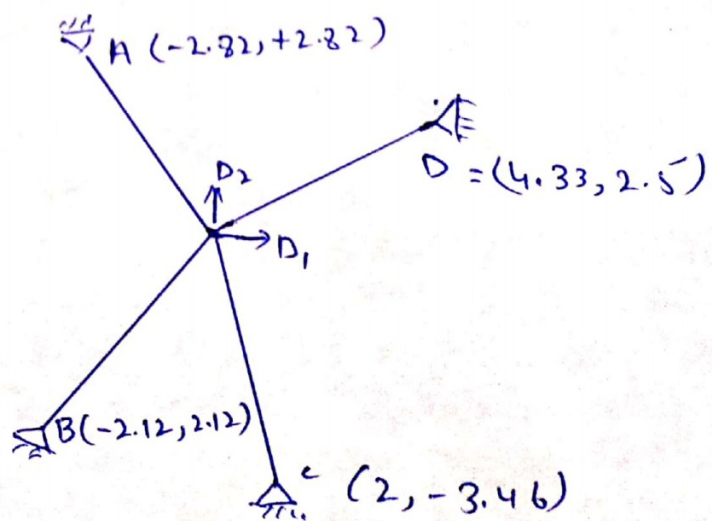
$$kI = 2j - 8$$

$$= 2(5) - 8$$

$$kI = 2^{\circ}$$

Step # 02

Select unknown joint displacement



$$\begin{bmatrix} P_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 2 \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

Step #03

$$[AMD]_{4 \times 2} \quad [S]_{2 \times 2}$$

i)  $D_1 = 1k$  ,  $D_2 = 0$

$$AMD = \frac{EA}{L^3} (x_k - x_j)$$

$$AMD_{11} = \frac{80000}{(400)^2} \times (0 + 282) = 141$$

$$AMD_{21} = \frac{80,000}{(300)^2} \times (0 + 212) = 188.44$$

$$AMD_{31} = \frac{100000}{(500)^2} \times (0 - 433) = -173.2$$

$$AMD_{41} = \frac{100,000}{(400)^2} \times (0 - 200) = -125$$

Now

$$S_{11} = \sum_{i=1}^m \frac{EA}{L^3} (x_k - x_j)^2$$

$$= \frac{80,000}{(400)^3} (282)^2 + \frac{80,000}{(300)^3} (212)^2$$

$$+ \frac{100,000}{(800)^3} \times (-433)^2 + \frac{100,000}{(400)^3} \times (-200)^2$$

$$S_{11} = 99.405 + 133.107 + 149.991 + 62.5$$

$$S_{11} = 445.063$$

⇒

$$S_{21} = \sum_{i=1}^m \frac{EA}{L^3} \times (x_k - x_j) (y_k - y_j)$$

$$= \frac{80,000}{(400)^3} (282) \times (-282) + \frac{80,000}{(800)^3} \times (212) (212)$$

$$+ \frac{100,000}{(800)^3} \times (-433)^2 \times (-250) + \frac{100,000}{(400)^3} (-200) \times (-346)$$

$$S_{12} = S_{21} = 12.237$$

(ii)  $D_1 = 0$        $D_2 = 1k'$

$$AMD = \frac{EA}{L^2} (y_k - y_j)$$

$$AMD_{12} = \frac{80,000}{(400)^2} (-282) = -141$$

$$AMD_{22} = \frac{80,000}{(300)^2} (212) = 188.44$$

$$AMD_{32} = \frac{100,000}{(500)^2} (-250) = -100$$

$$AMD_{42} = \frac{100,000}{(400)^2} (346) = 216.25$$

$$Now \quad S_{22} = \sum_{i=1}^m \frac{EA}{L^3} (y_{ik} - y_j)^2$$

$$\frac{80,000}{400^3} (-282)^2 + \frac{80,000}{300^3} (212)^2$$

$$+ \frac{100,000}{(500)^3} (-250)^2 + \frac{100,000}{(400)^3} (346)^2$$

$$S_{22} = 469.628$$

Step # 04

$$[D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.003 & 12.237 \\ 12.237 & 469.628 \end{bmatrix}^{-1} \times \begin{bmatrix} 50 \\ 100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

Step # 05

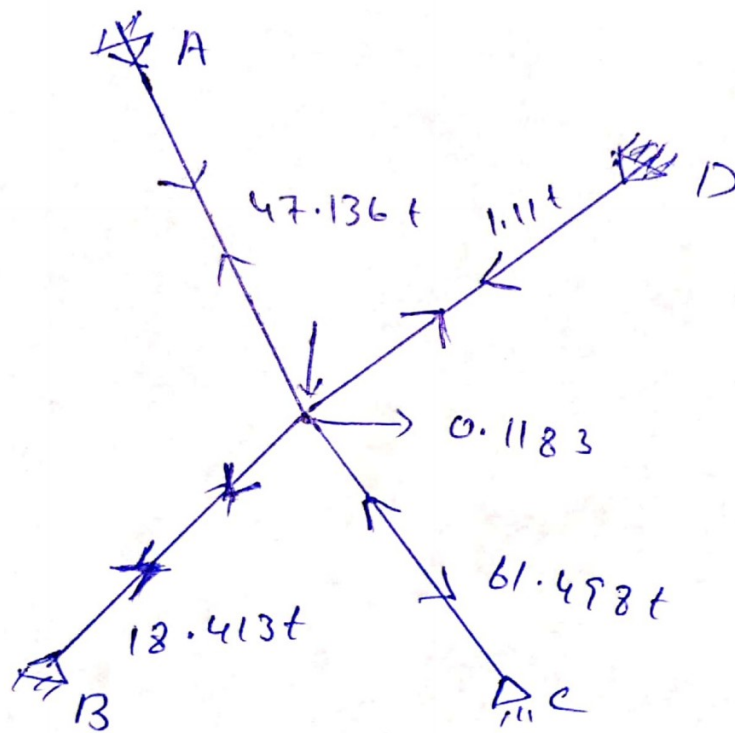
$$= [AM]$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.44 & 188.44 \\ -173.2 & -100 \\ -125 & 216.25 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

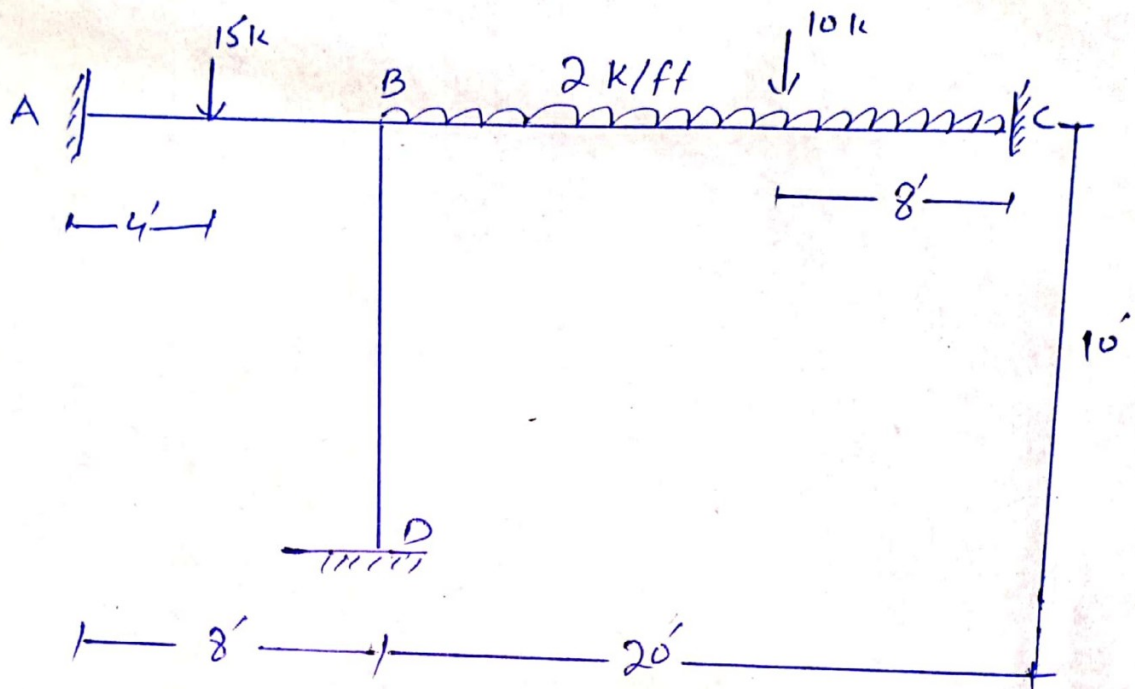
$$= \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + (188.44) \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ -125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 16.68 + 30.46 \\ 22.29 - 40.70 \\ -20.49 + 21.6 \\ -14.79 + 46.71 \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 47.136 t \\ -18.413 t \\ 1.11 t \\ 61.498 t \end{bmatrix}$$



Q NO # 03



Sol:

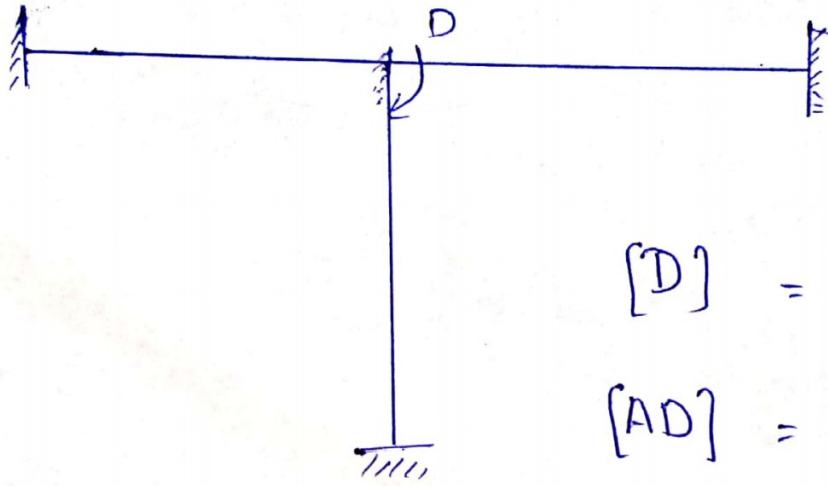
Step # 1

Determine kinematic indeterminacy.

$$K.I = 1^{\circ}$$

Step # 2

Determine unknown joint displacement

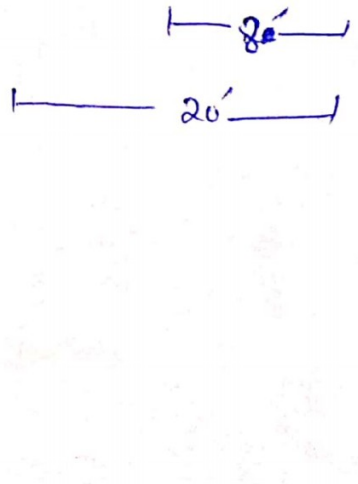
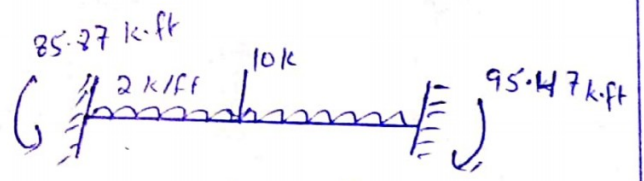
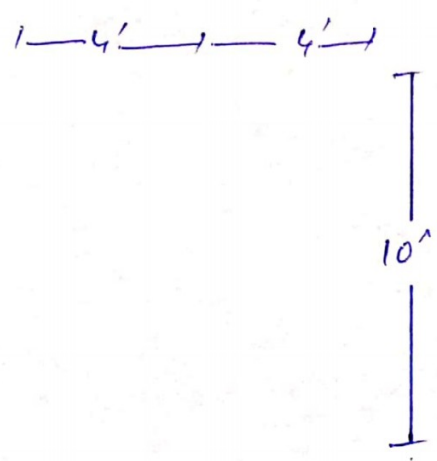
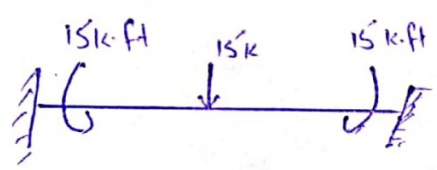


$$[D] = [?]$$

$$[AD] = [0]$$

Step #3 ::

Compute  $[ADL]$  Matrix



=> point load at center ::

$$\frac{PL}{8} \Rightarrow \frac{(15)(8)}{8} = 15 \text{ kip}\cdot\text{ft}$$

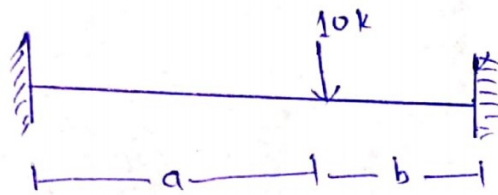


⇒ Uniformly Distributed load:

$$\frac{wL^2}{8} \Rightarrow \frac{2(20)^2}{12} = 66.67 \text{ k.ft}$$

⇒ Point load (Not at mid):

Suppose:



For Left end:

$$\frac{Pab^2}{L^2} \Rightarrow \frac{(10)(12)(8)^2}{(20)^2} = 19.2 \text{ k.ft}$$

For Right end:

$$\frac{Pa^2b}{L^2} = \frac{(10)(12)^2(8)}{(20)^2} = 28.8 \text{ k.ft.}$$

So Total Moment at left end:

$$19.2 + 66.67 = 85.87 \text{ k.ft}$$

Similarly at Right End:

$$28.8 + 66.67 = 95.47 \text{ k}\cdot\text{ft}$$

So  $[ADL] = -85.87 + 15 = -70.87 \text{ k}\cdot\text{ft}$

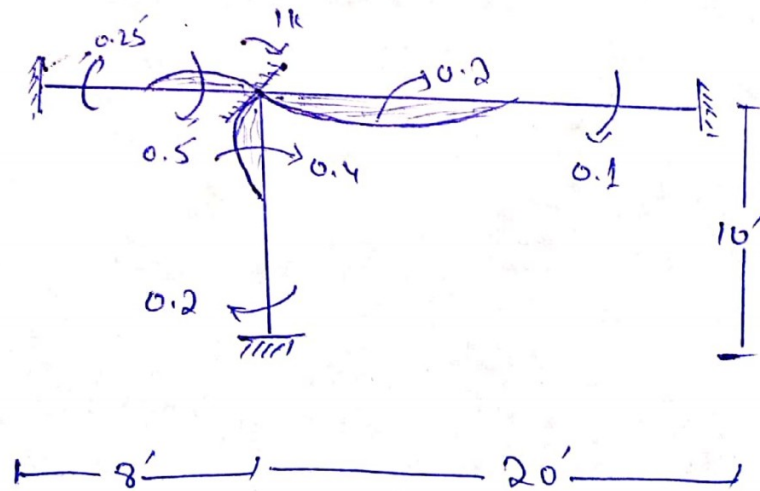
Step # 4

Determine  $[S]$  Matrix

$$[S] = [S_{ij}]$$

Now

$$D = 1 \text{ k}$$



$$\Rightarrow \frac{4EI}{8} = 0.5$$

$$\frac{2EI}{8} = 0.25$$

$$\Rightarrow \frac{4EI}{20} = 0.2$$

$$\frac{2EI}{20} = 0.1$$

$$= \frac{4EI}{10} = 0.4$$

$$\frac{2EI}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2) EI$$
$$= 1.1 EI$$

$$[S] = 1.1 EI$$

Step # 05

compute [D] Matrix

$$[D] = [S]^{-1} \times (AD) - (ADL)$$

$$D = \frac{1}{1.1} \times (0) - (-70.87)$$

$$= \frac{70.87}{1.1}$$

$$D = [64.42] \frac{1}{EI}$$