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ID #

7831

Section

B

Semester

5th

Subject

Hydraulic Engineering

QNO(01) :-Given Data :-

- ⊙ velocity of paraffin is 3.0 m s^{-1}
- ⊙ Density and viscosity are 800 kg m^{-3} and $0.002 \text{ kg m}^{-1} \text{ s}^{-1}$.
- ⊙ Kinematic viscosity of water
= $1.0 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$

Required :-

- ⓐ velocity of water in the model for dynamic similarity.
- ⓑ Ratio of the quantities of flow in prototype and model.
- ⓒ pressure drop in prototype if 60 kPa in model.

Solution :-

The pressure drop Δp is expected to depend upon the gate opening h , the overall depth d , the velocity V , density ρ and viscosity μ .

"List the relevant variable"

$$\Delta p, h, d, V, \rho, \mu$$

write down dimensions:

$$\Delta p = ML^{-1}T^{-2}$$

$$h = L$$

$$d = L$$

$$v = LT^{-1}$$

$$f = ML^{-3}$$

$$c\mu = ML^{-1}T^{-1}$$

① Number of variable $n = 6$

Number of independent dimension $m = 3$ (M, L and T)

② Number of non dimensional groups $n - m = 3$

choose ($m = 3$) Scaling variables
geometric (d) Kinematic/time dependent (v)
dynamic/mass dependent (f).

From dimensionless groups by non dimensionalising the remaining variables Δp , h and $c\mu$.

$$\begin{aligned} \textcircled{3} \Pi_1 &= \Delta p d^a v^b f^c \\ M^0 L^0 T^0 &= (ML^{-1}T^{-2})(L)^a (LT^{-1})^b (ML^{-3})^c \\ &= M^{1+c} L^{-1+a+b-3c} T^{-3-b} \end{aligned}$$

7831 (P-3)

$$M: 0 = 1 + c \Rightarrow c = -1$$

$$T: 0 = -2 - b \Rightarrow b = -2$$

$$L: 0 = -1 + a + b - 3c$$

$$\Rightarrow a = 1 + 3c - b = 0$$

$$\odot \Pi_2 = \Delta p V^{-2} \rho^{-1} = \frac{\Delta p}{\rho V^2}$$

$\Pi_2 = h/d$ (By inspection, since h is length)

$$\odot \Pi_3 = \mu d^a V^b \rho^c$$

(probably obvious by now, but here goes anyway)

$$M^0 L^0 T^0 = (ML^{-1}T^{-1})^a (L)^b (LT^{-1})^c (ML^{-3})^d$$

$$= M^{1+c} L^{-1+a+b-3c} T^{-1-b}$$

$$M: 0 = 1 + c \Rightarrow c = -1$$

$$T: 0 = -1 - b + 0 \Rightarrow b = -1$$

$$L: 0 = -1 + a + b - 3c \Rightarrow a = 1 + 3c - b$$

$$b = -1$$

$$\Rightarrow \Pi_3' = \mu d^{-1} V^{-1} \rho^{-1} = \mu / \rho V d$$

Recognition of the Reynold number suggests that ~~replace~~ replace

Π_3 by Π_3'

$$\Pi_3' = (\Pi_3)^{-1} = \rho V d / \mu$$

$$\Pi_3 = \left(\frac{\rho v d}{\mu} \right) = \left(\frac{\rho v d}{\mu} \right)_m$$

From the last we have a velocity Ratio

$$\frac{v_p}{v_m} = \frac{(\mu/\rho)^p}{(\mu/\rho)_m} \times \frac{d_m}{d_p}$$

$$= \frac{0.002/800 \times 1/5}{1.0 \times 10^{-6}} = 0.5$$

Hence:

$$v_m = \frac{v_p}{0.5} = \frac{3.0}{0.5} = 6.0 \text{ m s}^{-1}$$

⑥ The ratio of Quantities of flow is

$$\frac{Q_p}{Q_m} = \frac{(\text{Velocity} \times \text{Area})_p}{(\text{velocity} \times \text{area})_m}$$

$$= \frac{v_p}{v_m} \times \left(\frac{d_p}{d_m} \right)^2 = 0.5 \times 5^2 = 12.5$$

⑦ Finally for pressure drop.

$$\Pi_1 = \left(\frac{\Delta P}{\rho v^2} \right) = \left(\frac{\Delta P}{\rho v^2} \right)_m$$

$$\Rightarrow \frac{(\Delta P)_p}{(\Delta P)_m} = \left(\frac{\rho_p}{\rho_m} \right) \left(\frac{v_p}{v_m} \right)^2 = \frac{800}{1000} \times 0.5^2$$

$$= 0.2$$

Hence

$$\Delta P = 0.2 \times \Delta P_m = 0.2 \times 60 = 12.0 \text{ KPa}$$

thus the Required results //

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QNO(02)

Given Data :-

- ⊙ Maximum Depth (H) = 78m
- ⊙ Specific Gravity = $G = 2.4$
- ⊙ Height of wave $H_w = 1.2m$
- ⊙ $f_{av} = 783 T/m^2$

Solution :-

$$\textcircled{1} \quad "H"_{\text{limiting}} = \frac{f_{av}}{\gamma_w (G - U + 1)}$$

put values

$$\begin{aligned} H_{\text{limiting}} &= \frac{7830 \times 1000}{1000 (2.4 - 0 + 1)} \\ &= \frac{783000}{3400} \end{aligned}$$

$$H_{\text{limiting}} = 230.29m$$

ⓐ Top width "a"

$$\begin{aligned} \text{Free board} &= 1.5 \times h_{\text{Wave}} \\ &= 1.5 \times 1.2 \\ &= 1.8m \end{aligned}$$

$$\boxed{F.B = 1.8m}$$

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$$\text{height of Dam} = HD = Hw + F.B$$

$$HD = 78 + 1.8$$

$$HD = 79.7$$

$$a = 14\% \text{ of } HD$$

$$a = 0.14 \times 79.7$$

$$a = 11.173 \text{ m}$$

③ Base width 'b' :-

$$b' = \frac{Hw}{CG} \quad \text{put values}$$

$$b' = \frac{78}{0.7 \times 2.4}$$

$$= 46.41 \text{ m}$$

$$b' = 47 \text{ m}$$

④ For no tension Criteria :-

$$b' = \frac{Hw}{\sqrt{G}} = \frac{78}{\sqrt{2.4}}$$

use $b' = 50.33 \text{ m}$

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(4) Depth of vertical portion
u/s side :-

$$h' = 2a \sqrt{G-cu}$$

$$h' = 2 \times 11.173 \sqrt{2.4-0}$$

$$h' = 34.602$$

$$h' = 35 \text{ m}$$

(5) Upstream offset :-

$$a/16 = \frac{11.173}{16} = 0.69 \text{ m}$$

(6) Depth of below the water
level to the end of inclined
portion u/s = $3.14 a \sqrt{G}$
 $= 3.14 \times 11.173 \sqrt{2.4}$
 $= 54.332 \text{ m}$

(7) Total width of base of Dam :-

$$b = b' + \frac{a}{16} = 50.33 + \frac{11.173}{16}$$

$$b = 51.05 \text{ m}$$

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$$\textcircled{8} \quad \tan \theta = \frac{b'}{H} = \frac{50.33}{78}$$

$$\tan \theta = 0.64$$

$$\theta = \tan^{-1}(0.64)$$

$$\theta = 32.61^\circ$$

\textcircled{9} Depth of vertical portion on
D/S (formula on V/S side)

$$\tan \theta = \frac{a}{d_1} = \frac{11.173}{d_1}$$

$$\tan \theta = \frac{11.173}{d_1}$$

$$d_1 = \frac{11.173}{\tan \theta}$$

$$d_1 = \frac{11.173}{\tan(32.61)} \quad / 88.24$$

$$\boxed{d_1 = 0.126 \text{ m}}$$

Now

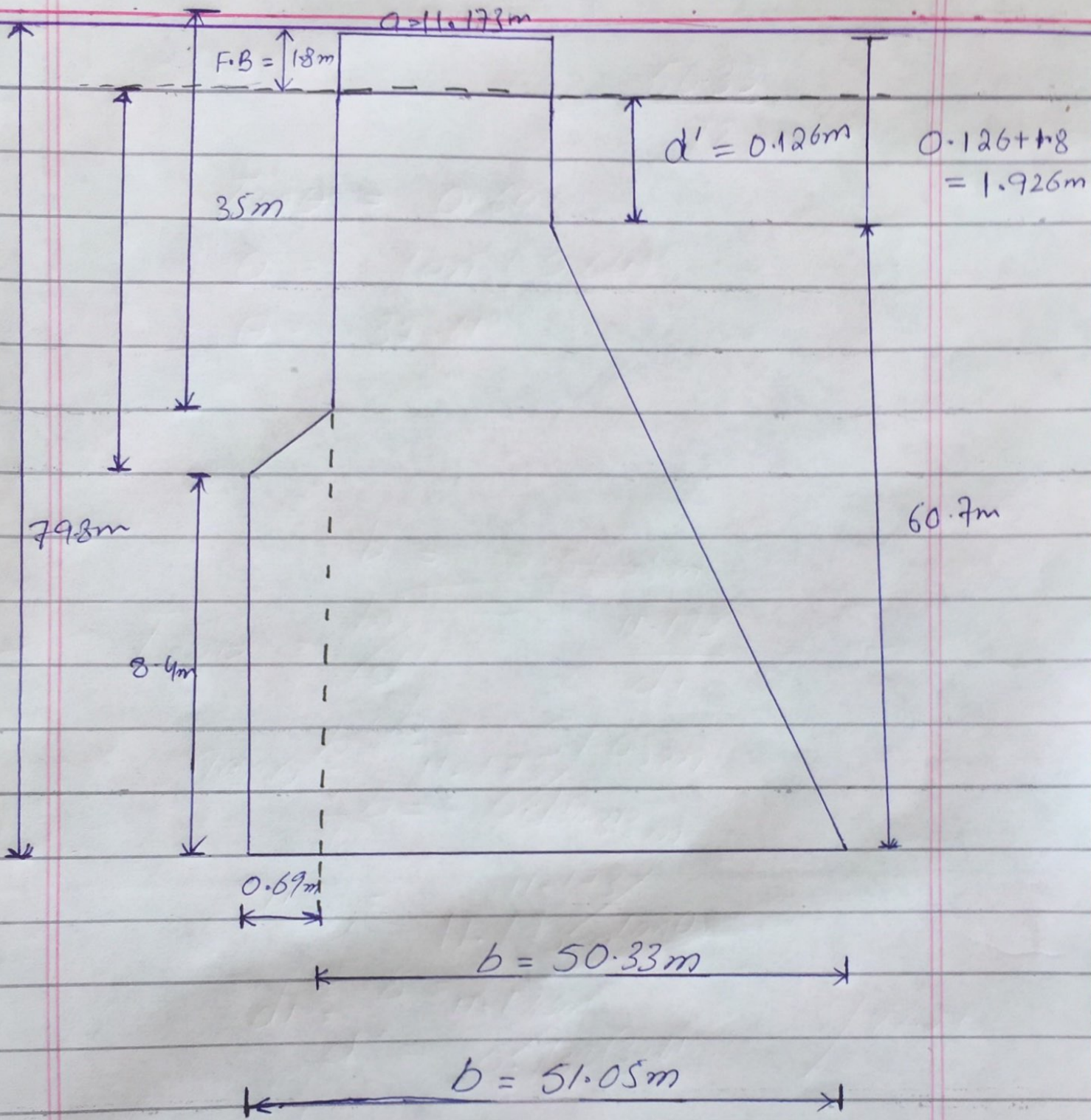
\textcircled{10} Depth of vertical portion:-

$$d = d' + F \cdot B$$

$$= 0.126 + 1.08$$

$$d = 0.22 \text{ m}$$

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QNO(03):-

"Concept of Dimensional Analysis and Similitude"

Back Ground :-

Although many practical engineering problem involving hydraulic engineering can be solved evaluations and analytical procedure but yet a large number of problems rely on experimental data for their solution.

- ① Similitude is used to express measurement on laboratory can be used to describe the behaviour of other system outside of laboratory.

Dimensional Analysis :-

- ⊙ Dimensional Analysis is a mathematical technique making wise study of dimensions.
- ⊙ It deal with dimension of physical Quantities involved in the phenomena
- ⊙ It helpful in experimental world b/c it provided a guide to those things.
- ⊙ Significant influence the phenomena this mathematical technique is used in research work for design and for conducting mode test.

Types of Dimensions :-

⊙ Fundamental Dimension

⊙ Secondary Dimension

These are derived Quantities

e.g. velocity = $\frac{\text{Length}}{\text{Time}}$

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Model Analysis and Similitude:

"Similitude of hydraulic model experiment for tidal mixing"

The treatment of diffusion due to tidal current in near shore and the similitude in the hydraulic model experiment are studied.

In broad and shallow tidal bays and in coastal seawater near irregular boundaries, horizontal eddy current induce geinical and turbulence caused by flows cascading have predominant effect on dispersion of river and waste water there. Turbulent diffusion process similarly reproduced in Froude model of turbulent

(P-13) 7831

resume by adding the
similitude for self similar
structure of the
spectral density of turbulence
or eddy diffusivity.
The similitude mean
take vertical length as
two thirds power scale
ratio of horizontal power
In this special case
there is no need satisfy
similitude for density
difference and vertical
effect on dispersion.

Kinematic Similarity :-

Ratio of velocity b/w
prototype and model

$$\frac{V_p}{V_m} = \sqrt[3]{\frac{V_p}{V_m}}$$

Kinematic similarity depend
on flow except force.

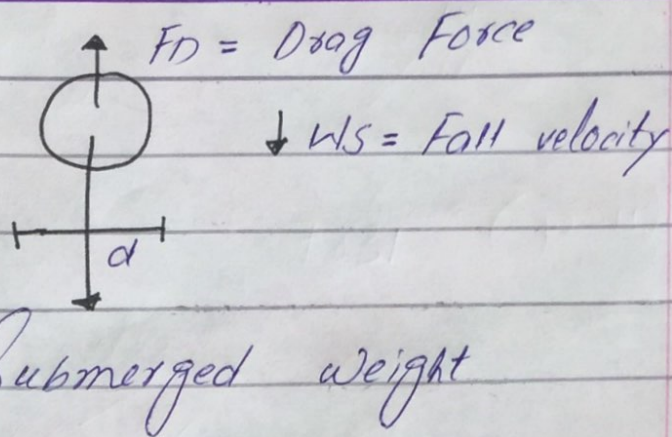
QNO(04):-

- ⊙ The downward velocity in a low dense fluid at equilibrium in which the sum of the gravity force bouyancy force and fluid drage are equal to zero
- ⊙ When a grain falls down in still water it obtain a constant velocity when the upward fluid drage force on the grain is equal to the downward submerged weight of grain. This is also called setting velocity.

Fall velocity effected due to the following terms.

- ⊙ particles diameter
- ⊙ particles density.
- ⊙ particles concentration
- ⊙ particles shape
- ⊙ velocity of water (Temp)
- ⊙ turbulence

7831 (P-15)



The Force balance b/w the drag force and the Submerged weight gives

$F_D = \text{Submerged weight}$

$$\frac{1}{2} \rho C_D \frac{\pi}{4} d^2 w_s^2 = (\rho_s - \rho) g \frac{\pi d^3}{6}$$

$$A = \frac{\pi d^2}{4} = \text{projected area}$$

$C_D = \text{Drag Co-efficient}$

$w_s = \text{Fall velocity of Sediment.}$

$$= \sqrt{\frac{4gd}{3C_D} \left(\frac{\rho_s - \rho}{\rho} \right)}$$

$\rho = \text{Density of water (G)}$

$\rho_s = \text{Density of Sediment particles / m}^3$

7831 (p-16)

Particle Size (Diameter)

Particle size is a notion introduced for comparing dimension of solid particles, liquid particles or gaseous particles.

particles density:

The particles density of particular solid or powder is density of particles that make up powder.

particles Shape:-

It is defined as the relative dimension of long intermediate and short axes of particles.

7831 (P-17)

viscosity of water:

Define as;

A fluid internal resistance to flow and may be through of a measure of fluid friction.

Turbulence: Turbulen

flow is the fluid motion characterized by chaotic changes in pressure and flow velocity. It is in contrast to laminar flow.