

Question = 03

Solution #

(*) A generator is connected
of 20kVA which injects
P and Q into the busbar.

(*) A load of 20kVA is
connected which takes
P and Q from the Busbar.

(*) A load connected which takes
P and Q from Busbar.

∴ This bus bar connected to
other bus bar i.e. to
bus and through lines.

Voltage V_c at the bus
bar i.e., is equal to
the magnitude V_c and
the angle δ .

one thing we see that
 generation injects P_{Glc} and
 Q_{Glc} while load takes
 P_{Llc} from the bus bar
 then we can take P_{Llc}
 and Q_{Llc} from the bus bar
 then we can take
 the algebraic sum of generation
 and loads i.e. subtracting
 the loads from generation.
 i.e.

$$P_{Glc} = P_{Glc} - P_{Llc}$$

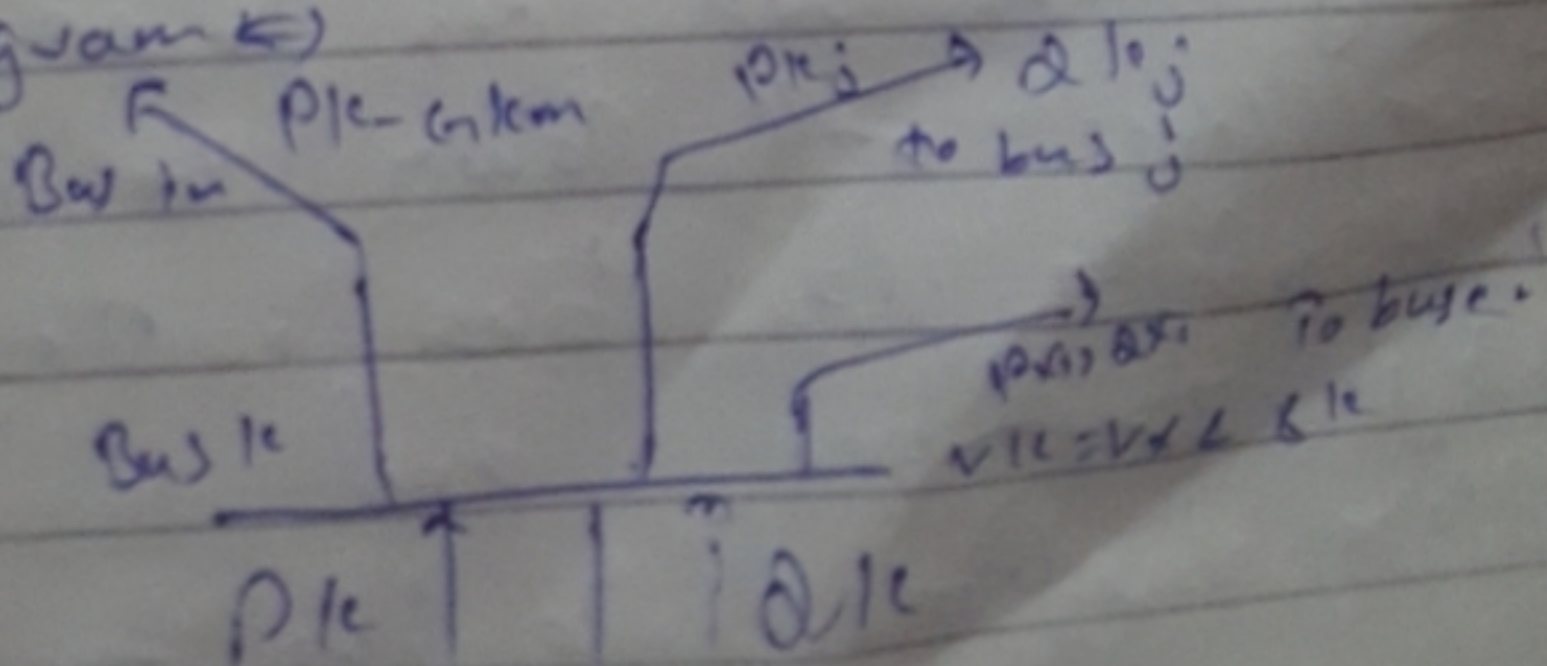
⇒ Real Power Injection

Similarly Reactive Power Injection

~~$$Q_{Glc} = Q_{Glc}$$~~

$$Q_{Glc} = Q_{Glc} - Q_{Llc}$$

Diagram ↪



*) Now we will say injection into bus bar rather saying the generation and loads if at particular bus bar load is connected the the net injection to that bus bar will be.

$$P_{10} = 0 - P_{L10}$$

$$P_{10} = -P_{L10}$$

$$Q_{10} = 0 - Q_{L10}$$

$$Q_{10} = -Q_{L10}$$

So load can be considered as negative injection

*) From the diagram we see that a three lines one going to bus bar, and to j and send one to m . These lines will carry the power P_{10j} , Q_{10j} to bus j , P_{10m} , Q_{10m} to bus bar m .

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- ⊛ Same of three power, a reverse direction. i.e. they may be coming from bus j to bus i in that case the value of P_{ij} & Q_{ij} will be negative.

So,

$$P_{ie} = P_{ei} + P_{ej} + P_{em}$$

$$Q_{ie} = Q_{ei} + Q_{ej} + Q_{em}$$

∴ Real and Reactive Power equal algebraic sum of P & Q power going out.

⊛ Power Flow Equations

we should that power flow equations are coming from the network equations.

i.e. $I_{Bus} = Y_{Bus} \cdot V_{Bus}$ (1)

I_{Bus} is the vector of current injection into the bus bars. Y_{Bus} is the $n \times n$ matrix of the admittance. V_{Bus} voltage phase bases of power system.

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$$I_k = \sum_{n=1}^n y_{kn} V_n \quad \text{--- (1)}$$

n = no of bus bar

y_{kn} = admittance of the k th element

V_n = voltage \angle phase at bus n

$$S_k = P_k + jQ_k = V_k I_k \quad \text{--- (2)}$$

now we know the values

eq (2) substitution I_k in eq (2)

$$P_k + jQ_k = V_k \left[\sum_{n=1}^n y_{kn} V_n \right] \text{ where } P_k, Q_k$$

V_n is a phase which has a magnitude and an angle

$$V_n = V_n e^{j\delta_n}$$

and $y_{kn} = y_{kn} e^{j(\theta_{kn} - \delta_n - \delta_k)}$

substituting V_n and y_{kn} value eq (2)

$$P_k + jQ_k = V_k \sum_{n=1}^n y_{kn} V_n e^{j(\theta_{kn} - \delta_n - \delta_k)}$$

- * All angles δ_k with V_k
- δ_n with V_n
- θ_{kn} with y_{kn}

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All negative ble of Conjugate, we can separate out the act & ^{injection} language Point. Then we can write the real power ~~injection~~ into Bus l as

$$P_l = V_l \sum_{n=1}^n Y_{ln} V_n \cos(\delta_l - \delta_n - \alpha_{ln})$$

Similarly the Reactive Power injection in

$$Q_l = V_l \sum_{n=1}^n Y_{ln} V_n \sin(\delta_l - \delta_n - \alpha_{ln})$$

(So) we can see that these injection is related to the voltage magnitude and angle at various bus bus.

So (h) & (5) in said on the the Power flow equations for the Power Network

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Question. 05

Answer Gauss-Serial

This is the first ~~impedance~~ interactive method to find out the power flow equation for these method & we gain start ~~also~~ with the bases of network equation.

(1-e) $I_{Bus} = Y_{Bus} V_{Bus}$
and for any particular bus l

$$I_l = \sum_{n=1}^n y_{ln} V_n$$

The Complex Power.

$$S_l = P_l + jQ_l = V_l I_l^*$$

$$P_l + jQ_l = V_l \left[\sum_{n=1}^n y_{ln} V_n \right]^*$$

where $l = 1, 2, \dots, N$.

From complex power.

$$I_l = \frac{P_l - jQ_l}{V_l}$$

* Also

$$I_{le} = \sum_{n=1}^{\infty} y_{le} v_n \quad \text{or}$$

$$I_{le} = y_{le} v_1 + y_{le} v_2 + \dots + y_{le} v_{le} + y_{le} v_n$$

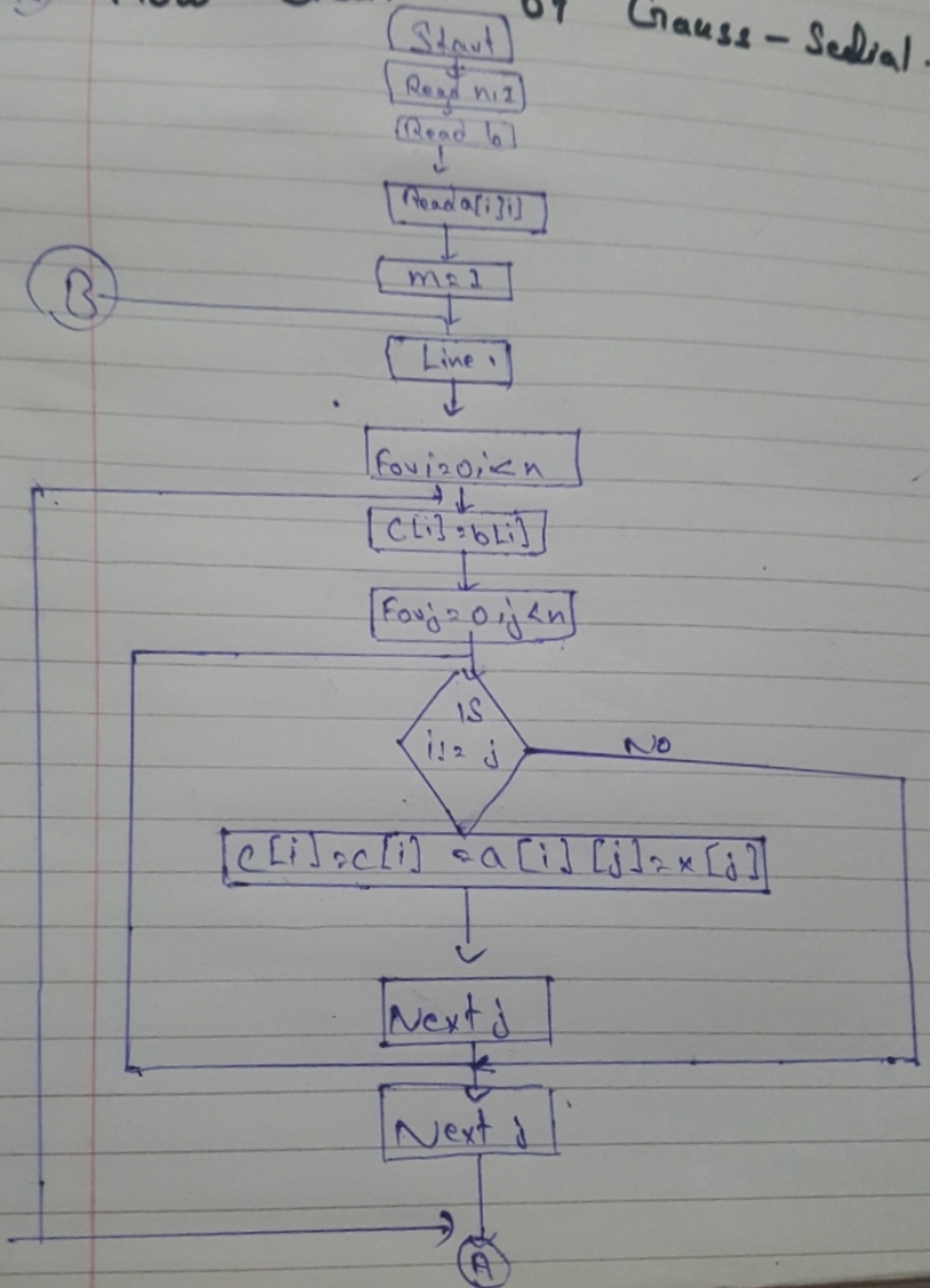
* From the above eq.

$$V_{le} = \frac{1}{y_{le}} \left[I_{le} = \left(\sum_{n=1}^{le} y_{le} v_n + \sum_{n=le+1}^{\infty} y_{le} v_n \right) \right]$$

$$V_{le} = \frac{1}{y_{le}} \left[\frac{P_{le} - j_{le}}{V_{le}} = \left(\sum_{n=1}^{le} y_{le} v_n + \sum_{n=le+1}^{\infty} y_{le} v_n \right) \right]$$

when $le = N$

(A) Flow Chart ⁽⁰⁹⁾ of Gauss - Seidel.



Question 04

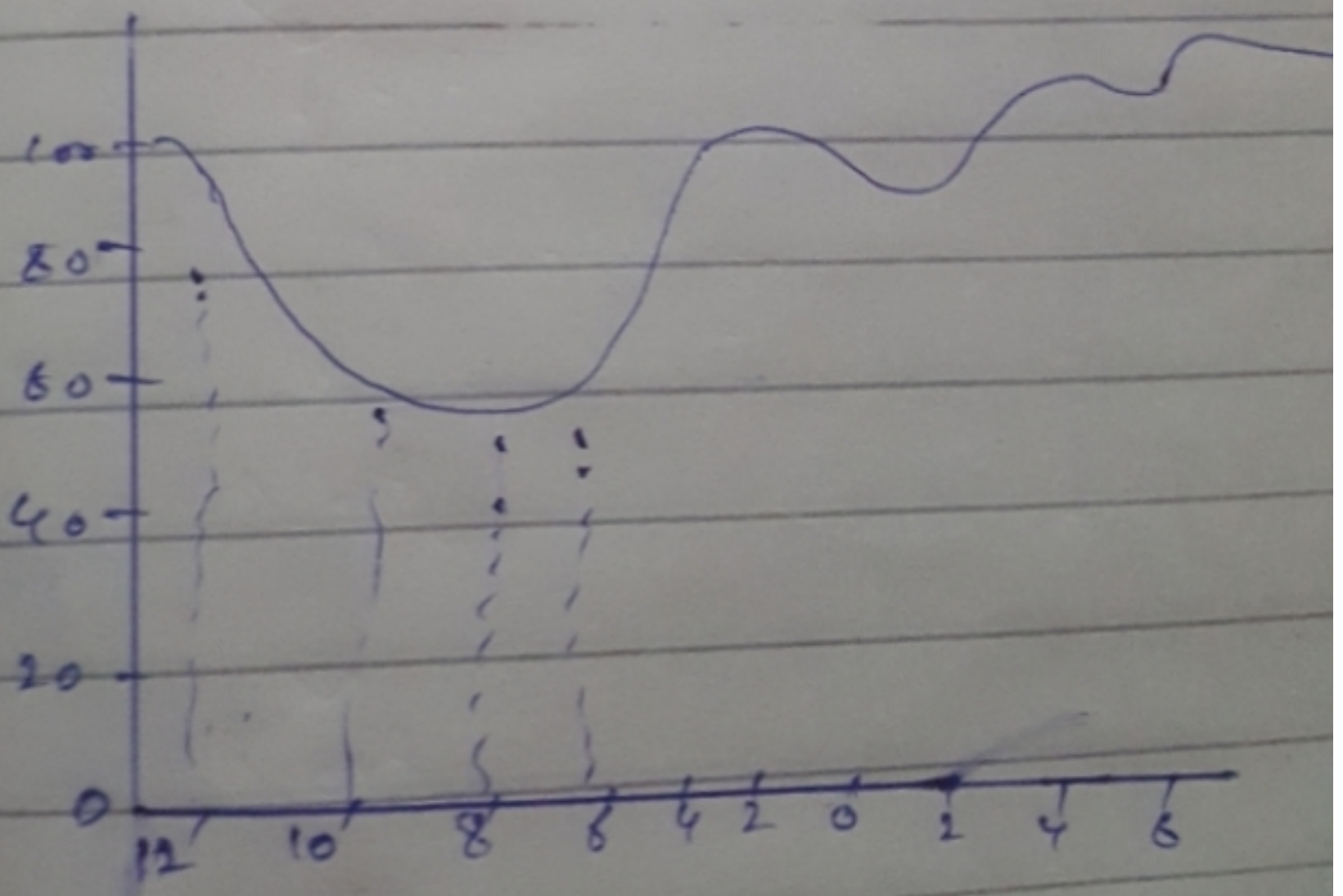
Answer (04)

There is one problem in doing power flow solution that we cannot know all the generation - All the load are known to us but generation are its own contract and one can say that all generation known to us but there is one problem. The problem is still all the the generation are available we don't know what is the loss in the system we cannot know the loss in the system and where and how much the loss.

Solution To overcome the we choose one bus as a reference bus which takes up all these

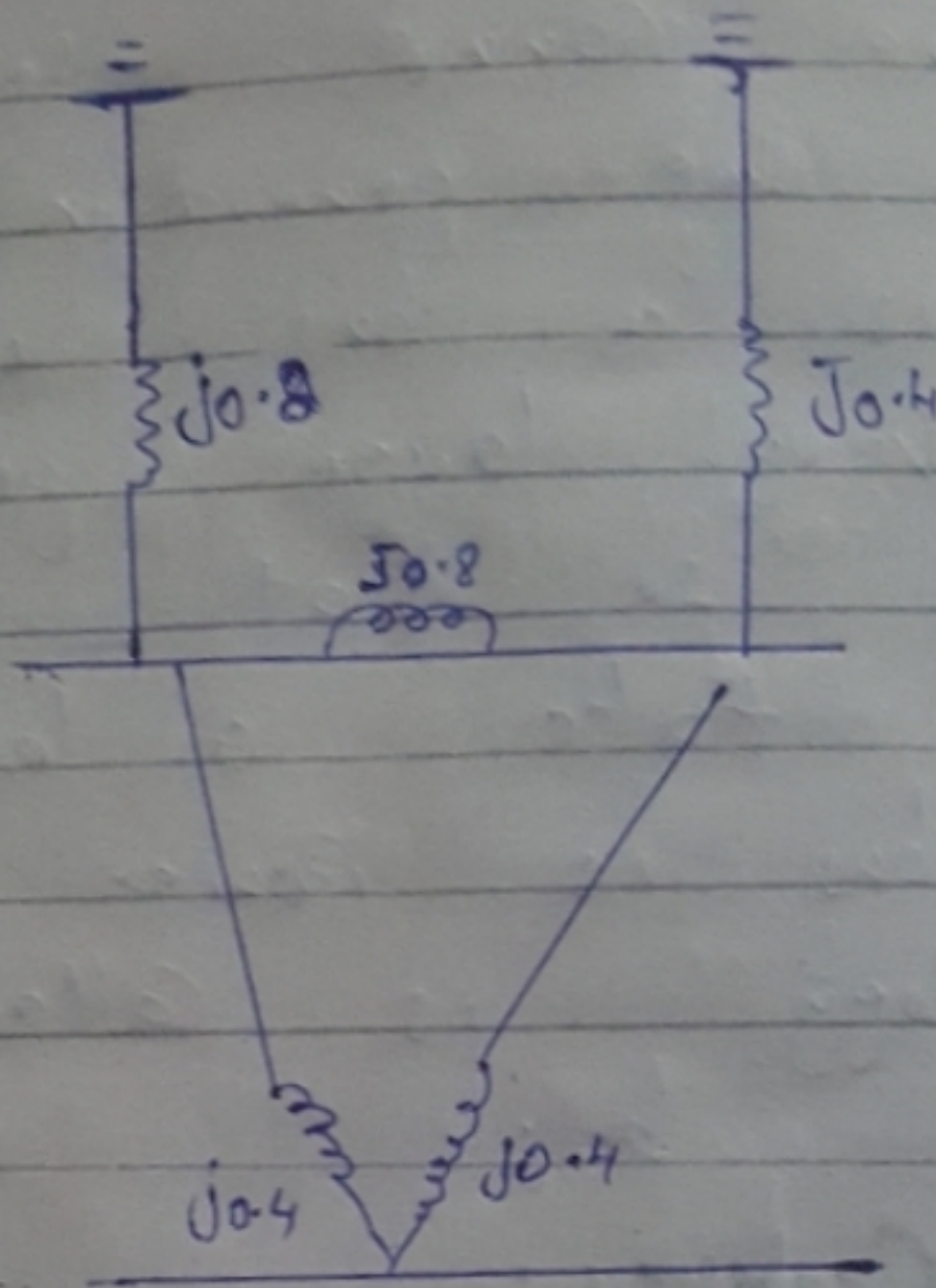
These losses which can find after solution P at once bus we cannot say a specify. the generation. Generally this is a bus which have very large generation available so that there is no trace a losses. this bus is power system terminology is called slack bus.

*) Load Curves.



Question = 02

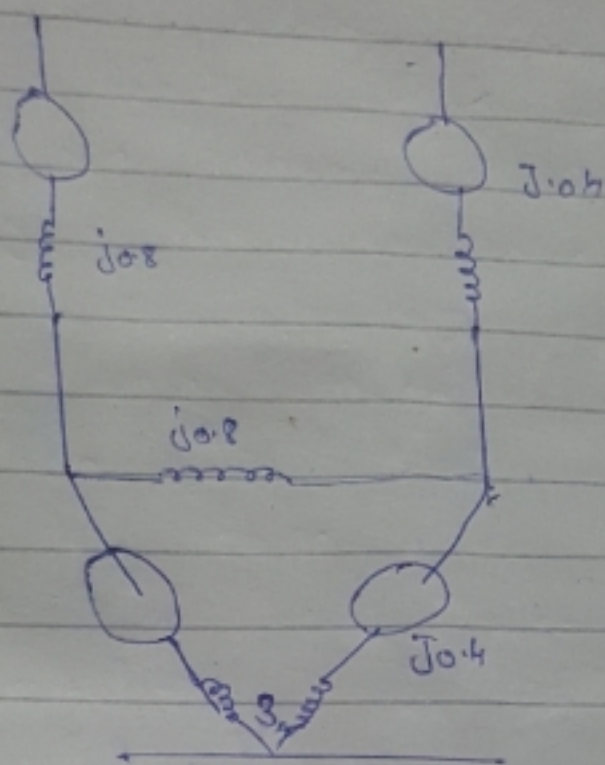
Solution 2)



Z base

Z base = y - bus

$$Z \text{ base} \begin{bmatrix} Z_{11} & Z_{12} & Z_{13} \\ Z_{21} & Z_{22} & Z_{23} \\ Z_{31} & Z_{32} & Z_{33} \end{bmatrix}$$



$$\begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} & Z_{13} \\ Z_{21} & Z_{22} & Z_{23} \\ Z_{31} & Z_{32} & Z_{33} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}$$

$$V_1 = Z_{11} \cdot I_1 + Z_{12} \cdot I_2 + Z_{13} \cdot I_3 \quad \text{--- (1)}$$

$$V_2 = Z_{21} \cdot I_1 + Z_{22} \cdot I_2 + Z_{23} \cdot I_3 \quad \text{--- (2)}$$

$$V_3 = Z_{31} \cdot I_1 + Z_{32} \cdot I_2 + Z_{33} \cdot I_3 \quad \text{--- (3)}$$

Question: 01

Solution:

The Current Source,

$$I_1 = I_s = \frac{2.5 \angle 0^\circ}{j 1.25}$$

$$= 1.2 \angle -90^\circ$$

$$= 0 - j 1.20 \text{ p.u.}$$

$$I_2 = \frac{2.5 \angle -36.87^\circ}{j 1.25}$$

$$= 1.2 \angle -126.87^\circ$$

$$= 0.72 - j 0.96 \text{ p.u.}$$

*) Self admittance in p.u.

$$y_{11} = -j 5.0 - j 4.0 + j 0.8$$

$$y_{11} = -j 9.8$$

$$y_{22} = j 5.0 - j 2.5 - j 0.8$$

$$y_{22} = j 8.3$$

$$y_{33} = j 4.0 - j 2.5 - j 0.8$$

total

6966

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$$y_{44} = -j18.0$$

and the mutual admittances in p.u

$$y_{12} = y_{21} = 0$$

$$y_{13} = y_{31} = -(-j4.0)$$

$$= +j4.0$$

$$y_{14} = y_{41} = +j5.0$$

$$y_{23} = y_{32} = +j9.5$$

$$y_{24} = y_{42} = +j5.0$$

$$y_{34} = y_{43} = +j8.0$$

The node equation is matrix form.

$$\begin{bmatrix} 0 - j12.0 \\ 0.72 - j0.76 \\ 0 - j1.20 \end{bmatrix} = \begin{bmatrix} -j9.8 & j0.0 & j4.0 & j5.0 \\ j0.0 & j8.3 & j2.5 & j5.0 \\ j4.0 & j2.5 & j15.3 & j8.0 \\ j5.0 & j5.0 & j8.0 & j18.0 \end{bmatrix}$$