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PAPER :- Soil Mechanics

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Q.1 Define the following terms =

(a)  
Ans  $\Rightarrow$  Hydraulic Gradient :-

Definition :-

A line joining the points of highest elevation of water in a series of vertical open pipes rising from a pipe line in which water flows under pressure.

$\Rightarrow$  Coefficient of permeability :-

The coefficient of permeability of a soil describes how easily a liquid will move through a soil. It is also commonly referred to as the hydraulic conductivity of a soil. This factor can be affected by viscosity and its density.

$\Rightarrow$  Liquidity index :-

The liquidity index is used for scaling the natural water content of a soil sample to the limits. It can be calculated as a ratio of difference between natural water content plastic limit & liquid limit.

⇒ Porosity:-

Porosity is a measure of the void space in a material and is a fraction of the volume of voids over the total volume. It varies between 0 and 1 as a percentage.   
 Strictly speaking between 0 and 100%.

⇒ Formula:-

$$n = \frac{\text{Vol of void}}{\text{Total Vol of soil mass}}$$

$$\Rightarrow V_v / V$$

⇒ Degree of Saturation:-

$$S = \frac{\text{Vol. of water}}{\text{Vol of voids}}$$

$$= V_{wv} / V_v$$

Q.1  
(B)

GIVEN DATA: -

$$w = 32 \text{ kg}, V = 0.0192 \text{ m}^3, w_s = 28.5 \text{ kg}$$

$$G_s = 2.65$$

Required: -

$$\gamma_B = ?$$

~~So~~

$$w = ?$$

$$\gamma_d = ?$$

$$v_{sat}$$

~~So~~ 
$$h = ?$$

Sol: -

(i) Bulk Density

$$\gamma_B = \frac{w}{V}$$

$$= \frac{32}{0.0192}$$

$$= 1666.67 \text{ kg/m}^3$$

(ii) Water Content: -

$$w_w = \frac{w - w_s}{w_s} = \frac{32 - 28.5}{28.5} = 12.3\%$$

$$w = \frac{w_w}{w_s} \times 100 = \frac{3.5}{28.5} \times 100 = 12.3\%$$

(iii) dry density

$$\gamma_d = \frac{w_s}{V}$$

$$= \frac{28.5}{0.0192} = 1484.37 \text{ kg/m}^3$$

$$\gamma_d = \frac{G_s + \gamma_w}{1 + e} \Rightarrow e = \frac{G_s \times \gamma_w}{\gamma_d} - 1 = \frac{2.65 \times 1000}{1484.3} - 1$$

$$e = 0.785$$

(iv) Saturated density

$$\gamma_{sat} = \frac{G_s + e}{1 + e} \gamma_w$$

$$\gamma_{sat} = \frac{(G_s + e) \gamma_w}{1 + e} = \frac{(2.65 + 0.785) \times 1000}{1 + 0.785}$$

$$= 1924.37 \text{ kg/m}^3$$

(v) void ratio

$$h = \frac{e}{1 + e}$$

$$h = \frac{0.785}{1 + 0.785} = 0.44 \text{ or } 44\%$$

$$w = \frac{S \times e}{G_s}$$

$$S = \frac{w \times G_s}{e}$$

$$= \frac{0.123 \times 2.65}{0.785}$$

$$= 0.415 \text{ or } 41.5\%$$

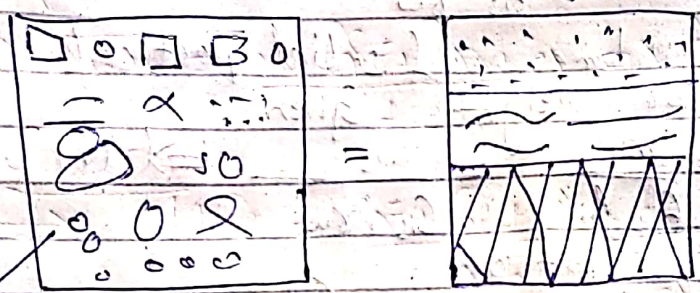
Q No (02)

(A) Prove that

$$\sigma = \frac{G_s \gamma_w (1 + w_c)}{\gamma_b} \cdot 1$$

Proof

Consider the following soil mass



Soil

Phase	Volume	mass	Weight
Air	$V_A$	0	0
water	$V_w$	$M_w$	$w_w$
Solid	$V_s$	$M_s$	$w_s$

As  $w = mg$  → (i)  
 unit :  $\gamma = \frac{w}{V}$  → (ii)

As  $w = mg$

$$\gamma = \frac{mg}{V}$$

$$\Rightarrow \gamma = \rho g$$

$$w = \gamma V \rightarrow \textcircled{B}$$

specific gravity

$$G_s = \frac{\text{Density of material}}{\text{Density of water}}$$

$$G = \frac{\gamma}{\gamma_w} \Rightarrow \text{(iii)}$$

for water  $G_s \approx 2.65$

$$\text{So } \rho_s = G_s \rho_w$$

hence volume of solid particle if mass or weight given

$$V_s = \frac{m_s}{\rho_s} = \frac{w_s}{\rho_s} \Rightarrow \text{(iv)}$$

As  $\rho$  ratio

$$e = \frac{V_v}{V_s} \rightarrow \text{(v)}$$

Porosity,  $n = \frac{V_v}{V} = \text{(vi)}$

$$\text{(v)} \& \text{(vi)} \Rightarrow V_s = V - V_v = (1 - n)V$$

$$\Rightarrow e = \frac{V_v}{(1 - n)V} \Rightarrow \text{(vii)}$$

So degree of saturation is

$$S = \frac{V_w}{V_v + V_w} \Rightarrow \text{(viii)}$$

$$\Rightarrow S = \frac{V_w}{eV_s}$$

$$V_w = eS V_s \Rightarrow S = \frac{V_w}{eV_s}$$

as  $V_a = V_v - V_w = eV_s (1 - S)$

Now

for figure (I)

Phase	Volume	mass	weight
Air	$e (1-s)$	0	0
water	$e_s$	$e_s \rho_w$	$e_s \gamma_w$
Solid	1	$G_s \rho_w$	$G_s \gamma_w$

$$\gamma_{bulk} = \frac{w}{V}$$

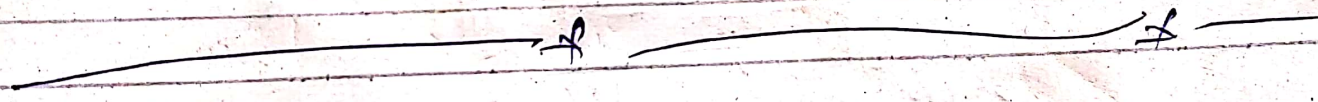
$$\Rightarrow \gamma_{bulk} = \frac{\gamma_w G_s + \gamma_w e_s}{1+e} \Rightarrow \text{A}$$

$$\text{A} \Rightarrow 1+e = \frac{\gamma_w G_s + \gamma_w e_s}{\gamma_b}$$

$$\text{II} \& \text{V} \Rightarrow 1+e = \frac{\gamma_w G_s + G_s v_w w_w}{\gamma_b} \Rightarrow \text{B}$$

$$e = \frac{G_s \gamma_w (1 - c_w)}{\gamma_b} - 1$$

Hence Proved.





Q. 2  
(b)

Ans Classification of Soil:-

→ Grain Size classification:-

① US - Bureau of Soil Classification:-

Clay	Silt	Sand				Gravel	
		very fine sand	Fine sand	medium sand	coarse sand	Fine Gravel	coarse Gravel
Practical Size	0.002 mm	0.05 mm	0.1 mm	0.25 mm	0.5 mm	1.00 mm	2.00 mm

② ASTM Soil Classification System

Clay	colloids clay	silt	Sand		Gravel
			Fine sand	coarse sand	
0.001 mm	0.005 mm	0.075 mm	0.25 mm	2.00 mm	

③ M.I.T Soil Classification System:-

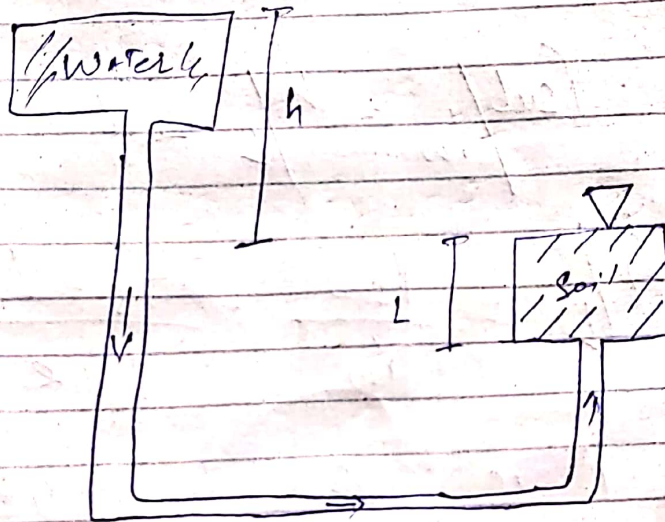
Clay			silt			Sand			Gravel
Fine clay	med clay	coarse clay	Fine clay silt	med silt	coarse silt	Fine sand	Med sand	coarse sand	
0.0002 mm	0.006 mm	0.002 mm	0.006 mm	0.02 mm	0.06 mm	0.2 mm	0.6 mm	2.00 mm	

Q3  
(A)

ANS

Physical Model:-

The total stress at the bottom of soil sample is.



$$\sigma = \gamma_{SAT} \times L$$

The upward pressure at the bottom of soil sample = water pressure from the left limb

$$u = \gamma_w \times (h + L)$$

Effective stress  $\sigma' = \sigma - u$

$$\sigma' = \gamma_{SAT} \times L - \gamma_w \times (h + L)$$

$$\sigma' = \gamma_{SAT} \times L - \gamma_w \times h - \gamma_w \times L$$

$$C = \gamma_{sub} \times L - \gamma_w \times h.$$

For Quick Condition

$$C = 0$$

$$\text{or } \gamma_{sub} \times L - \gamma_w \times h = 0$$

or

$$\frac{\gamma_{sub}}{\gamma_w} = \frac{h}{L} = i$$

$$\frac{h}{L} = \frac{\gamma_{sub}}{\gamma_w} = \frac{G_s - 1}{1 + e}$$

where,  $i$  is called hydraulic gradient

Taking the Specific gravity of soil as 2.65 and void ratio as 0.65. The value of  $i$  become unity.

if become Unity Then

$$i = 1$$

$$\text{i.e. } \frac{h}{L} = 1$$

$$\text{or } h = L$$

This indicates that when quick sand condition is achieved the head causing flow equal to the thickness of length of the specimen.

$$\tau = \bar{\sigma} \tan \phi$$

Where

$\tau$  = Shear Strength

$\bar{\sigma}$  = Effective Stress

$\phi$  = Angle of internal friction

When the effective normal stress

$$\bar{\sigma} = 0, \tau = 0.$$

If shear strength of soil is zero, it behaves as liquid.

When a natural soil becomes quick it cannot support the weight of man or animal.

Q No (03) (B)

GIVEN DATA: 0

$V = 65 \text{ ml} = 0.000065 \text{ m}^3$   
 As  $1 \text{ ml} = 10^{-6} \text{ m}^3$

$W = 0.96 \text{ N}$  ,  $W_d = 0.785 \text{ N}$ ,  
 $G_s = 2.65$

Required:  $S = ?$

Solution:

$$\gamma_B = \frac{\gamma_w \times (G_s + e \times S)}{(1 + e)} \rightarrow \text{①}$$

$$\gamma_B = \frac{W}{V} = \frac{0.96}{0.000065} = 14769 \text{ N/m}^3$$

$\gamma_w = 9800 \text{ N/m}^3$

As  $\gamma_s = \frac{w_s}{V_s}$

$e = \frac{V_v}{V_s}$

$V_s = 0.000030 \text{ m}^3$

$\gamma_s = \frac{w_s}{V_s}$

$e = \frac{0.000035}{0.000030}$

$\gamma_s = \frac{w_s}{V_s} = \frac{0.785}{0.000030} = 25970$

$e = 1.167$

But  $G_s = \frac{\gamma_s}{\gamma_w}$

Also

$V = V_v + V_s$

$\gamma_s = G_s \times \gamma_w$

$V_v = 0.000065 - 0.000030$

$\gamma_s = 2.65 \times 9800$

$V_v = 0.000035 \text{ m}^3$

$\gamma_s = 25970 \text{ N/m}^3$

Putting all the values in ① & solve it for "S"

$$S = 0.527 \text{ 00, } 52.7\%$$

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