

NAME

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ID

7724

SECTION

(A)

SUBJECT

STRUCTURE - A-II

DATE

25/09/2020

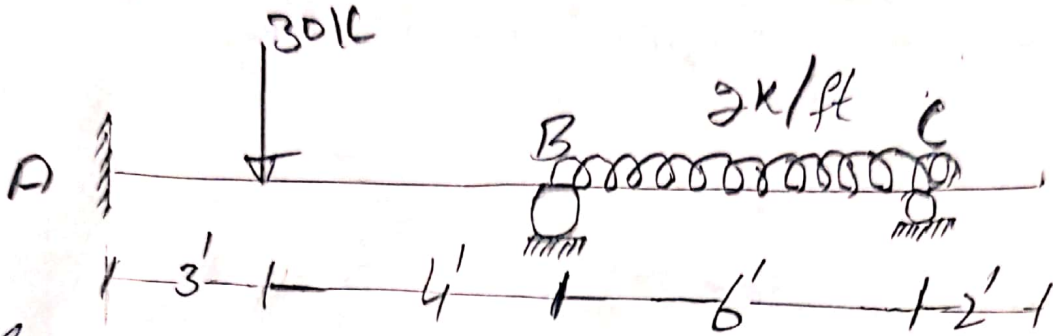
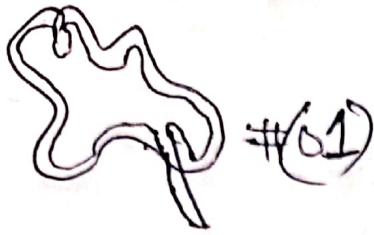
TEACHER

Engr. Sir ADEED

EXAME

Fo Term

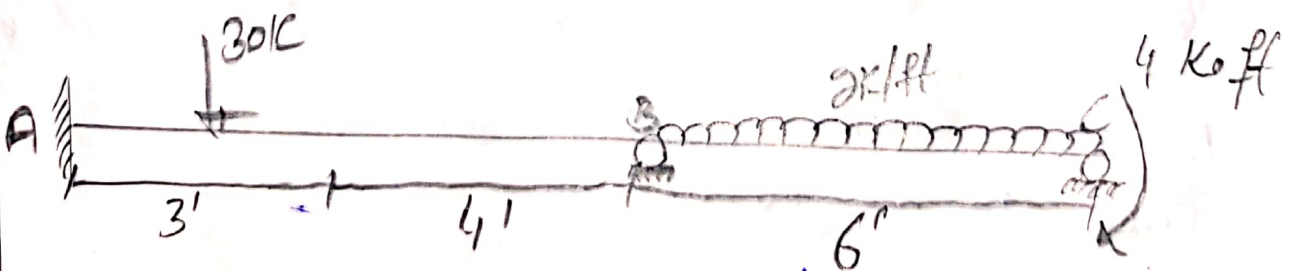
# 01/01



SOLUTION

#01 \* Determining Kinematic Indeterminacy  
 $\Rightarrow K_I = 5^{\circ}$

\* So we have to reduce the Extended portion:-

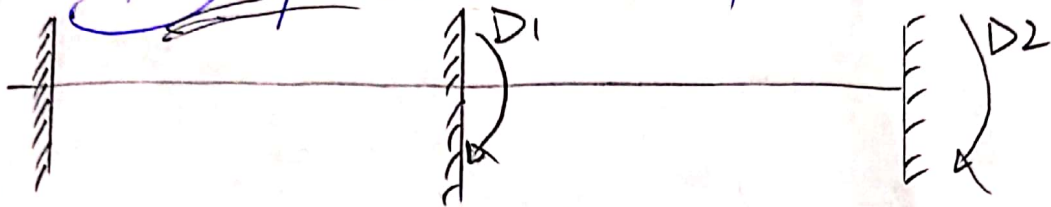


$\Rightarrow$  Now  $(K_I = 2^{\circ})$   $\frac{2(2)}{1} = 4 k_{eff}$

# 01/02

2-10-14

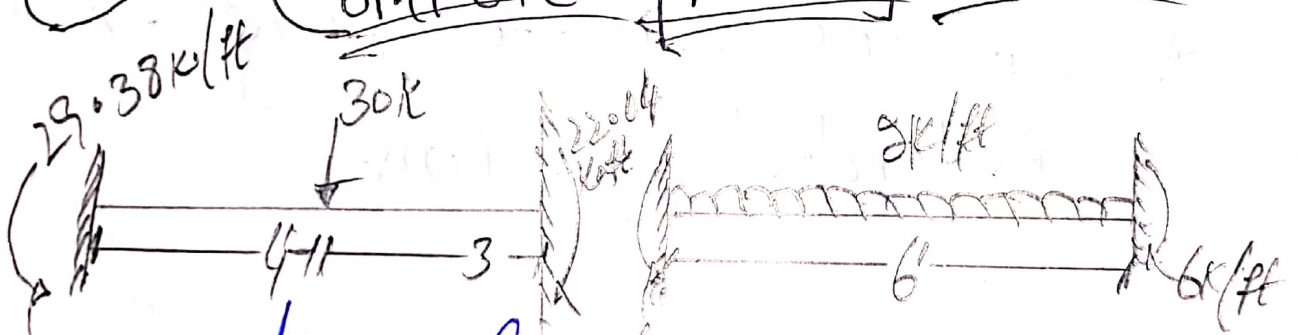
# #02 Determine Unknowns Joint Displacement



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

2-10-14

# #03 COMPUTE [ADL] Matrices



→ For point load (not at mid.)

→ For left End:  $\frac{Pab^2}{L^2} = \frac{(30)(3)(4)^2}{(7)^2}$

$(29.38 \text{ k/ft})$

#01/03

For Right End:

$$\frac{pab}{L^2} = \frac{(30)(3)(4)}{(7)^2} \Rightarrow \text{Group of } 22.04 \text{ k/ft}$$

For Uniformly Distributed Load:

$$= \frac{wL^2}{12} \Rightarrow \frac{(2)(6)^2}{12} \Rightarrow \boxed{6 \text{ k/ft}}$$

$$ADL_1 = +22.04 - 0.6 = \boxed{16.04 \text{ k/ft}}$$

$$ADL_2 = \boxed{6 \text{ k/ft}} \text{ Ans}$$

~~Q1 = 1k~~

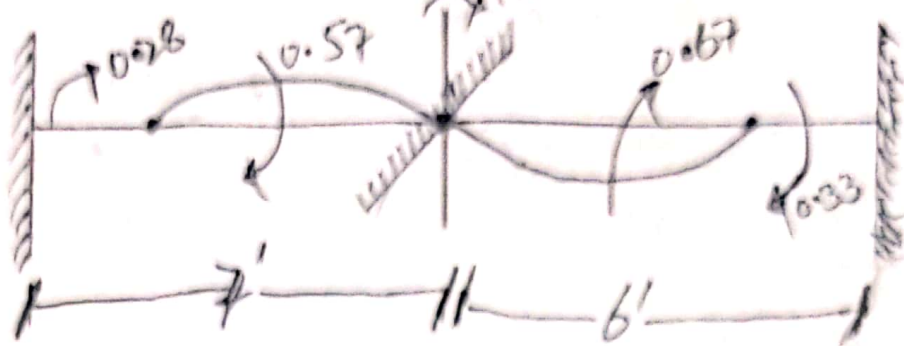
PREP #04 Now Compute

[S] MATRIX:

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

#01/04

#7  $D_1 = 1k$  ,  $D_2 = 0$



$$\frac{4EI}{7} = 0.57$$

$$\frac{2EI}{6} = 0.33$$

$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{7} = 0.28$$

$$S_{11} = 0.57 + 0.67$$

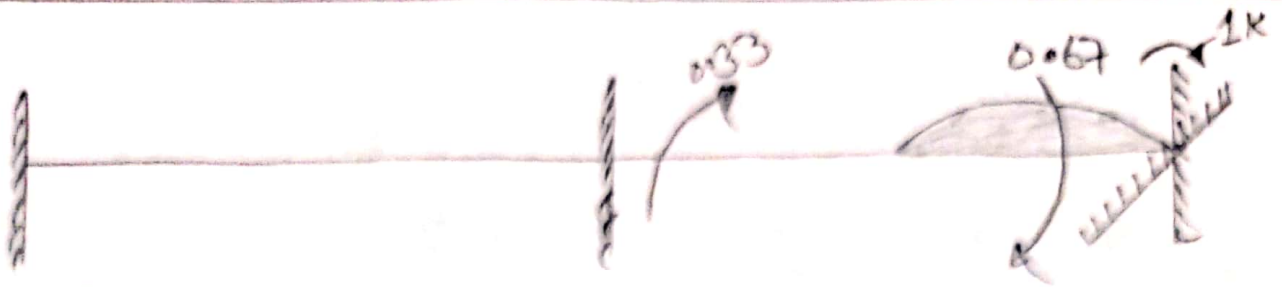
$$S_{11} = 1.24EA$$

$$S_{21} = 0.33EA$$

02) For  $D_1 = 0$

$D_2 = 1k$

#101/05



$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$S_{12} = 0.33$$

$$S_{22} = 0.67$$

$$S = \begin{bmatrix} 1.024 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$$

STEP

#105/17

Now COMPUTE [D]

MATRIX

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}^{-1} \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$\Rightarrow \frac{1}{\begin{bmatrix} 0.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}} \times \text{Adj} AX \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

# 01/06

$$\rightarrow |S| = (1.24 \times 0.67) - (0.33 \times 0.33)$$

$$\rightarrow |S| = 0.8308 - 0.1089$$

$$\rightarrow |S| = 0.7219$$

$$\text{Adj} A = \begin{bmatrix} & \\ & \end{bmatrix}$$

Now

$$\begin{bmatrix} AD_1 - AD_1 \\ AD_2 - AD_2 \end{bmatrix} = \begin{bmatrix} 0 - 16.04 \\ 4 - 6 \end{bmatrix} = \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} E$$

$$\begin{aligned} \rightarrow \begin{bmatrix} D_1 \\ D_2 \end{bmatrix} &= \frac{1}{|S|} \times \text{Adj} A \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} \\ &= \frac{\begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}}{0.7219} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} \\ &= \begin{bmatrix} 0.919 & -0.452 \\ 0.452 & 1.70 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} \end{aligned}$$

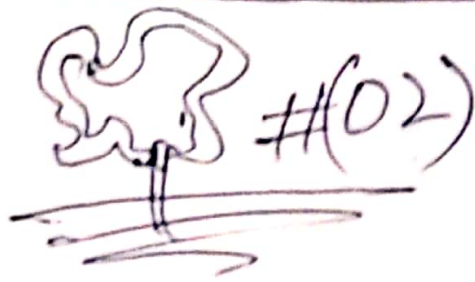
# 01/07

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.83 \\ 3.85 \end{bmatrix}$$

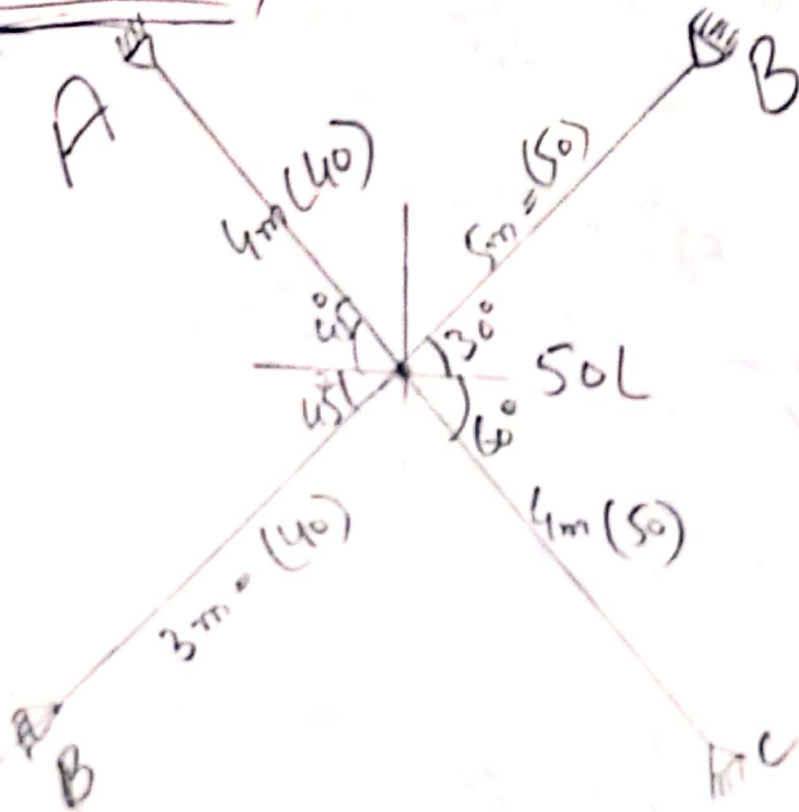
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Q # 01 To 01/07  
Page # 01/01 To 01/07



#02 / 01



#1) DIAGRAM



$$E = 2080 \pm \text{km}^2$$

SOLUTION

FOR B = A

$$\sin 45^\circ = \frac{P}{H} = \frac{P}{H}$$

$$\rightarrow P = 2082.8 \text{ m}$$

$$\cos 45^\circ = \frac{b}{H} = \frac{b}{H}$$

#02/02

$$\rightarrow b = 2.828 \text{ m}$$

$$\underline{\text{For \#B}} \quad \sin 45 = \frac{P}{H} = \frac{P}{3}$$

$$\rightarrow D = 2.12 \text{ m}$$

$$\cos 45 = \frac{b}{H} = \frac{b}{3}$$

$$\rightarrow b = 2.12 \text{ m}$$

$$\underline{\text{For \#C}} \quad \sin 60 = \frac{P}{H} = \frac{P}{4}$$

$$\rightarrow (\sin 60)(4) = D$$

$$\rightarrow P = 3.46$$

$$\cos 60 = \frac{b}{H} = \frac{b}{4} \quad \cos 60 \times 4 = b$$

For \#D

$$\sin 30 = \frac{P}{5}$$

$$\rightarrow P = 2.5 \text{ m}$$

$$b = 2$$

# 02/03

$$\Rightarrow \cos 30 = \frac{b}{5}$$

$$b = 4.33 \text{ m}$$

Now

$$EA(A) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(C) = 2000 \times 50 = 80,000 \text{ t}$$

$$EA(D) = 2000 \times 50 = 100,000 \text{ t}$$

Step #1 KI

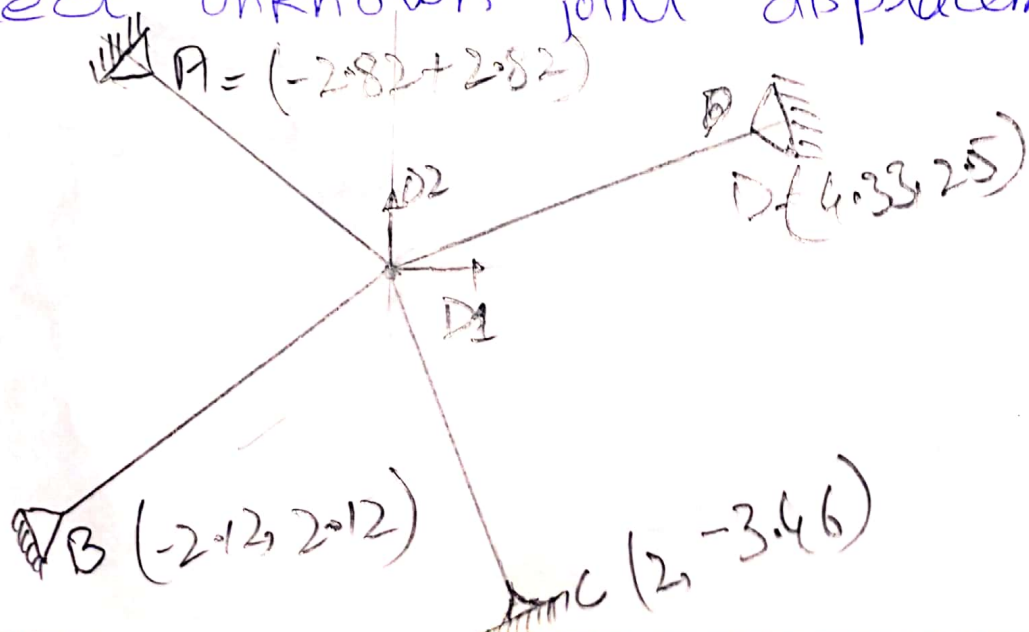
$$KI = 2j - \gamma$$

$$= 2(5) - 8$$

$$KI = 2$$

Step #2

Select unknown joint displacement



# 09/04

$$D_1 = ? \quad AD_1 \quad S_0$$

$$D_2 = ? \quad AD_2 \quad -100$$

#03

AMD S

$$D_1 = 1K \quad D_2 = 0$$

$$AMD = \frac{EA}{L^2} (X_k - X_j)$$

$$AMD_{11} = \frac{80000}{(400)^2} \times (0 + 282) = 141$$

$$AMD_{21} = \frac{80000}{(300)^2} \times (0 + 212) = 188.491$$

$$AMD_{31} = \frac{100,000}{(500)^2} \times (0 - 483) = -173$$

$$AMD_{41} = \frac{100,000}{(400)^2} \times (0 - 200) = -12$$

~~AMD~~

$$\sum_{i=1}^M \frac{EA}{L^3} (X_k - X_j)^2$$

#02/08

$$= \frac{80,000}{(400)^3} (282)^2 + \frac{80,000}{(300)^3} \times (212)$$

$$+ \frac{100,000}{(500)^3} \times (-433)^2 + \frac{100,000}{(400)^3} \times (-200)^2$$

$$S_{11} = 99.408 + 133.107 + 149.891 + 625$$

$$S_{11} = 445.063$$

$$\Rightarrow S_{12} = S_{21} = \sum_{I=1}^m \frac{EA}{L^3} \times (y_k - y_j)$$

$$(y_k - y_j)$$

$$= \frac{80,000}{(400)^3} (282)(-282) + \frac{80,000}{(300)^3} (212)$$

$$(212) + \frac{100,000}{(500)^3} (-433)(0-200) + \frac{100,000}{(400)^3}$$

$$(-200)(0-346)$$

$$\Rightarrow S_{12} = S_{21} = 12.237$$

#02/08

$$ii) D_1 = 0 \quad D_2 = 1k$$

$$AMD = \frac{EA}{L^2} (y_t - \frac{1}{j})$$

$$AMD_{12} = \frac{80,000}{(400)^2} (-282) = -141$$

$$AMD_{22} = \frac{80,000}{(400)^2} (212) = 188.44$$

$$AMD_{32} = \frac{100,000}{(500)^2} (-250) = -100$$

$$AMD_{42} = \frac{100,000}{(400)^3} (346) = 216.25$$

$$\text{Now } S_{22} = 469.628$$

$$\underline{\text{Step \#4:}} \quad [D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

#02/07

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.003 & 12.237 \\ 12.237 & 469.628 \end{bmatrix} \times \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

#102/08

#705

[AM]

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.44 & 188.44 \\ 173.2 & -100 \\ -125 & 216.25 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ 0.216 \end{bmatrix}$$

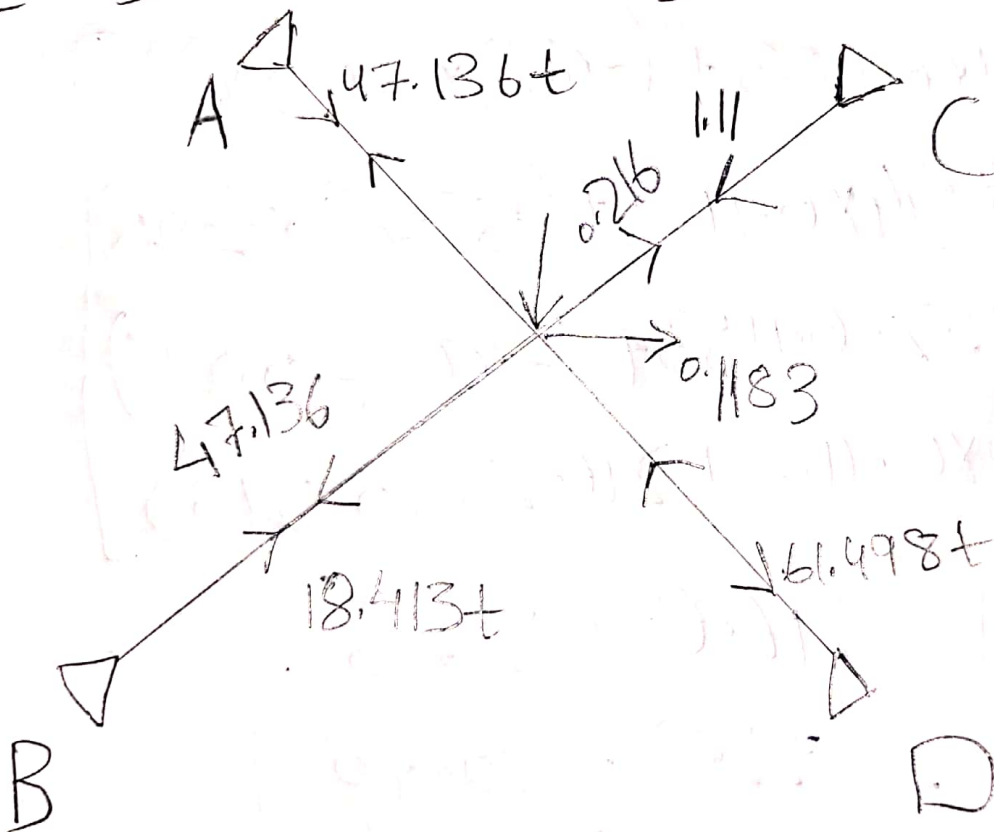
$$= \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + (188.44) \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ 125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 16.68 + 30.46 \\ 22.29 - 40.70 \\ -20.49 + 21.6 \\ -14.79 + 46.71 \end{bmatrix}$$



#02/09

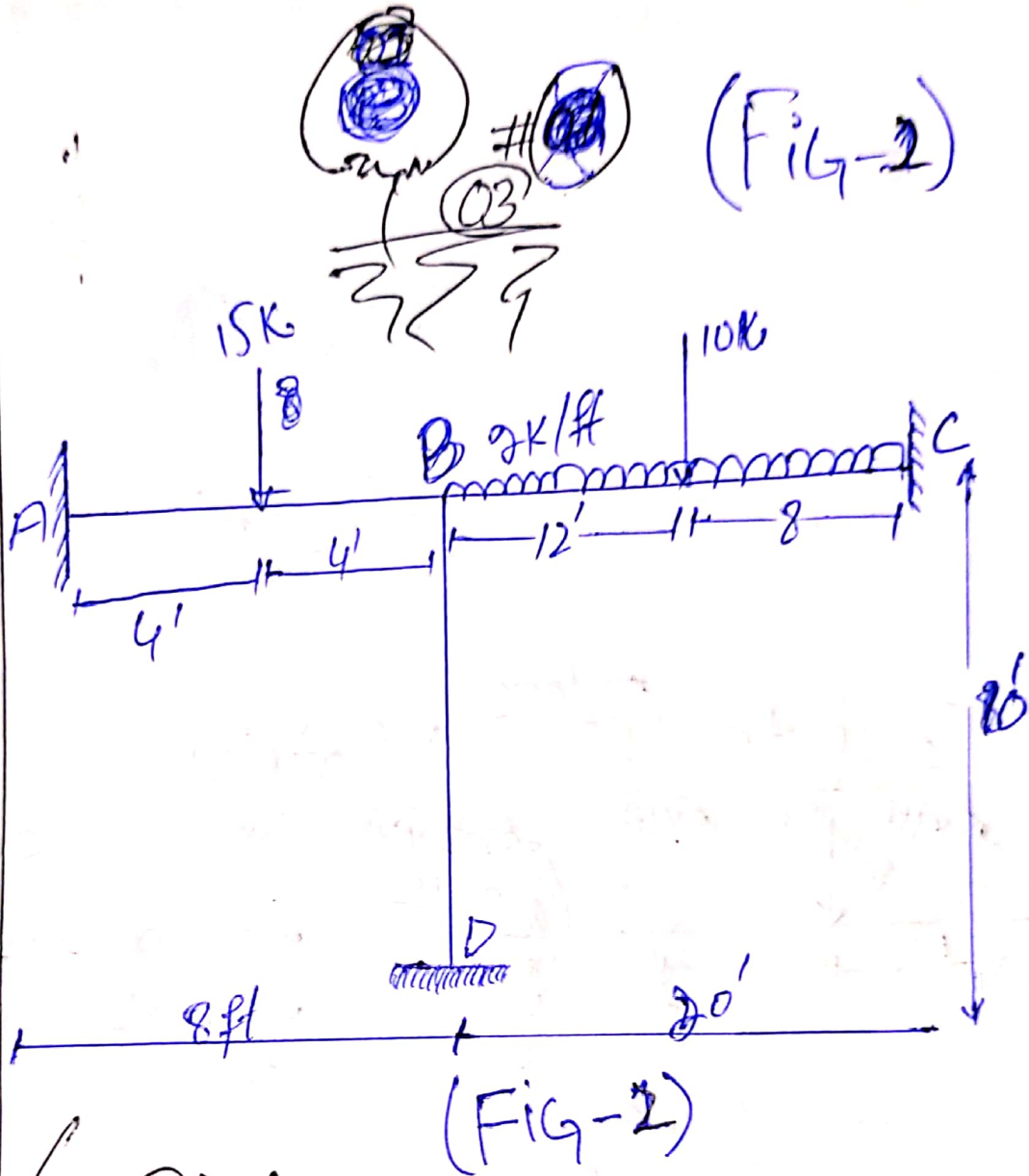
$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 47.136t \\ -18.413t \\ 1.11t \\ -61.498t \end{bmatrix}$$



Completed

Q # 02  
Page # 02/01 To # 02/09

# 3/01



SOLUTION

(Fig-2)

Q1  $\Rightarrow$  Determine Kinematic Indeterminacy  
Step  $K.I = 1^0$

Q2  $\Rightarrow$  Determine Unknown Joint Displacement.  
Step

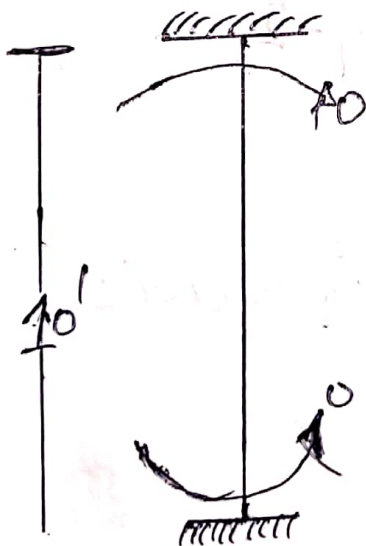
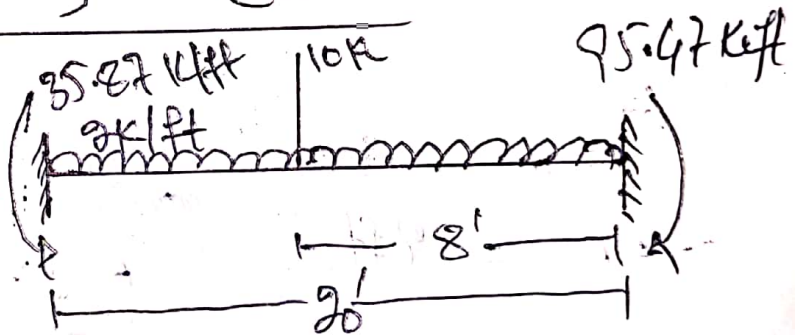
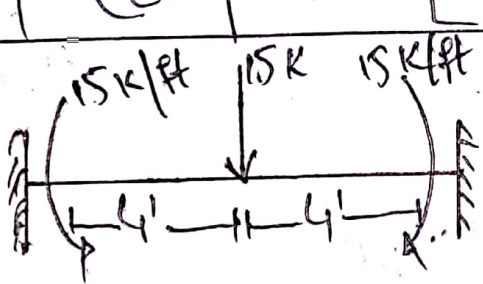
# 3/02



$$[D] = [?]$$

$$[AD] = [0]$$

Q3)  $\Rightarrow$  Compute  $[ADL]$  Matrix



$\Rightarrow$  point load at Center  $\Rightarrow$

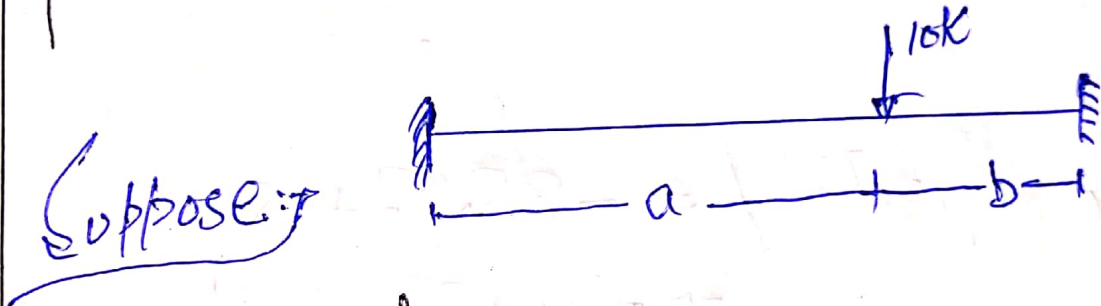
$$\Rightarrow PL/8 \Rightarrow \frac{(15)(8)}{8} \Rightarrow \boxed{15 \text{ k/ft}}$$

#3/03

⇒ Uniformly Distributed load ⇒

$$\Rightarrow \frac{wL^2}{12} \Rightarrow \frac{2(20)^2}{12} = \boxed{66.67 \text{ k-ft}}$$

⇒ Point Load (Not at Mid) ⇒



✓ For Left End ⇒

$$\Rightarrow \frac{Pab^2}{L^2} \Rightarrow \frac{(10)(10)(8)^2}{(20)^2} = \boxed{19.2 \text{ k-ft}}$$

✓ For Right End ⇒

$$\Rightarrow \frac{Pa^2b}{L^2} \Rightarrow \frac{(10)(10)^2(8)}{(20)^2} = \boxed{28.8 \text{ k-ft}}$$

N/A 03/04

# 03/04

⇒ So Total Moment at left end is

$$\Rightarrow 19.2 + 66.67 = \boxed{85.87 \text{ K.ft}}$$

⇒ Similarly at Right End is

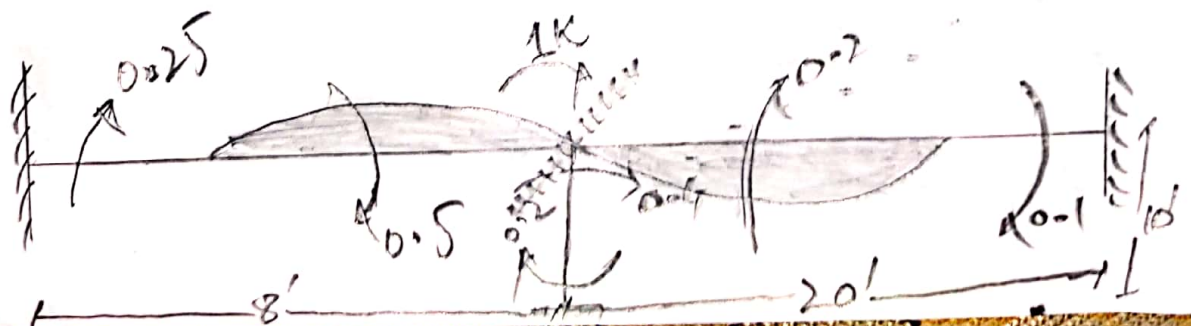
$$\Rightarrow 28.8 + 66.7 = \boxed{95.47 \text{ K.ft}}$$

$$\Rightarrow \text{So } [ADL] \Rightarrow -85.87 + 15 \\ \Rightarrow -70.87 \text{ K.ft}$$

Q4) Determine [S] Matrix for

$$[S] = [S_{ij}]$$

Now (D) = (1K)



# 03/05

$$\rightarrow \frac{4EI}{8} = 0.5 \quad \frac{2EI}{8} = 0.25$$

$$\rightarrow \frac{4EI}{20} = 0.2 \quad \frac{2EI}{20} = 0.1$$

$$\rightarrow \frac{4EI}{10} = 0.4 \quad \frac{2EI}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2) EI$$
$$= 1.1 EI$$

$$[S] = 1.1 EI$$

# 05 Compute [D] Matrix

$$[D] = [S]^{-1} \times [AD] - [ADL]$$

# 05

#03/06

$$[D] = \frac{1}{1.01} \times [0] - [-70.87]$$

$$\Rightarrow \frac{70.87}{1.01}$$

$$[D] = [64.042] \frac{1}{EI}$$

Completed

Q # 03

Page # 03/01 to 03/06