



Department Of AHS

Summer-2020

Subject: Applied Mathematics-I

Duration: Minutes

Instructor: Anwar Shamim

Total Marks: 30

Semester: Summer Semester

Note: Attempt all questions. Manage your time properly.

Q.No. (01)

(3+3+4)

Find the Integration of the following.

a. $\int (x^2 e^x) dx$

b. $\int (5x^2 + x^{-2} + 15) dx$

c. $\int (x^3 + x^{-2} + 5) dx$

Q.No. (02)

((3+3+4)

Find the solution of the following.

- If 56% of the homes in a colony have a car. What %age of homes does not have a car?
- There are 1029 students in a school. 504 of them are girls. Find the ratio of boys to the girls.
- Amna scored 46 out of 50 in a math test, 64 out of 75 in a chemistry test and 72 out of 80 in a physics test. In which subject did she perform best?

Q.No. (03)

(3+3+4)

Find the derivatives of the following.

a) $S = -4t^{-5} + 4/t + 5t + 1/4$

b) $Y = x^5 + 3x^3 - x^2 + 4$

c) $T = 6x^{-3} + x^3 + 5x - 2$

Name : Natasha Khan
Student ID: 15981
Department : HND

Q#1:-

Find Solution of the following.

- a) If 56% of the homes in a colony have a car. What %age of homes does not have a car.

Solution:

Percentage of homes with car = 56%

Without car = $100 - 56$

= 44%

44% of homes does not have car.

- b) There are 1029 students in a school. 504 of them are girls. Find the ratio of boys to the girls.

Solution:-

No of girls = 504

No of boys = 525

PAGE #2

$$\rightarrow \frac{525}{1029} : \frac{504}{1029}$$

$$\rightarrow \frac{525 \div 21}{1029 \div 21} : \frac{504 \div 21}{1029 \div 21}$$

$$\rightarrow \frac{25}{49} : \frac{24}{49}$$

$$\rightarrow \frac{25 \times 49}{49} : \frac{24 \times 49}{49}$$

$$\rightarrow 24 : 25 \text{ (Ans)}$$

c) Amna scored 46 out of 50 ----- In which subject did she perform best.

Solution:

$$\rightarrow \text{Maths} = \frac{46}{50} \times 100 = 92\%$$

$$\rightarrow \text{Chemistry} = \frac{64}{75} \times 100 = 85.3\%$$

$$\rightarrow \text{Physics} = \frac{72}{80} \times 100 = 90\%$$

She performed the best in maths.

COPY

Page #3:

Q #3:

Find the derivatives of the following.

$$a) S = -4t^{-5} + \frac{4}{t} + 5t + \frac{1}{4}$$

Solution:

$$\rightarrow S = -4t^{-5} + 4t^{-1} + 5t + \frac{1}{4}$$

$$\rightarrow \frac{ds}{dt} = (-4)(-5)t^{-5-1} + 4(-1)t^{-1-1} + 5(1)t^{1-1}$$

$$\rightarrow 20t^{-6} - 4t^{-2} + 5$$

$$\rightarrow 20t^{-6} - \frac{4}{t^2} + 5 \quad (\text{Ans})$$

$$b) y = x^5 + 3x^3 - x^2 + 4$$

Solution:

$$\rightarrow \frac{dy}{dx} = \frac{d}{dx}(x^5) + \frac{d}{dx}(3x^3) - \frac{d}{dx}(x^2) + \frac{d}{dx}(4)$$

$$dy/dx = 5x^{5-1} + 3(3)(x^{3-1}) - 2x^{2-1} + 0$$

$$\rightarrow \frac{dy}{dx} = 5x^4 + 9x^2 - 2x + 0 \quad (\text{Ans})$$

PAGE # 4

$$c) T = 6x^{-3} + x^3 + 5x - 2$$

Solution:

$$\rightarrow \frac{dT}{dx} = \frac{d}{dx} (6x^{-3} + x^3 + 5x - 2)$$

$$\rightarrow \frac{dT}{dx} = -18x^{-4} + 3x^2 + 5 - 0$$

$$\rightarrow \frac{dT}{dx} = -18x^{-4} + 3x^2 + 5 - 0 \quad (\text{Ans})$$

Q# 1:

Find the integration of the following.

$$b) \int (5x^2 + x^{-2} + 15) dx$$

Solution:

$$\rightarrow \frac{5x^{2+1}}{2+1} + \frac{x^{-2+1}}{-2+1} + 15x + C$$

$$\rightarrow \frac{5x^3}{3} + \frac{x^{-1}}{-1} + 15x + C$$

$$\rightarrow \frac{5x^3}{3} - \frac{1}{x} + 15x + C \quad (\text{Ans})$$

PAGE #5

$$\rightarrow \text{c) } \int (x^3 + x^{-2} + 5) dx$$

Solution:

$$\rightarrow \frac{x^{3+1}}{3+1} + \frac{x^{-2+1}}{-2+1} + 5x + C$$

$$\rightarrow \frac{x^4}{4} + \frac{x^{-1}}{-1} + 5x + C$$

$$\rightarrow \frac{x^4}{4} - \frac{1}{x} + 5x + C \text{ (Ans)}$$

$$\text{a) } \int (x^2 e^x) dx$$

Solution:

$$\rightarrow \int (x^2) dx \int e^x dx$$

$$\rightarrow \left[\frac{x^{2+1}}{2+1} \right] e^x dx$$

$$\rightarrow \frac{x^3}{3} e^x + C \text{ (Answer)}$$